

## Comment

# Effective mass decrease due to electron-phonon interaction in heavy fermion systems

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**Abstract.** It is argued that in heavy fermion systems the electron-phonon interaction results in a decrease of the quasiparticle mass. This is in contrast to ordinary metals where this interaction is known to increase the effective mass. A simple expression is derived which relates the effective mass change to the electronic Grüneisen parameter, the Kondo temperature and the bulk modulus. For CeRu<sub>2</sub>Si<sub>2</sub> the effective-mass decrease is estimated to be 25%.

In ordinary metals the quasiparticle mass  $m^*$  increases when the electron-phonon interaction is turned on. The electron with its phonon cloud is heavier than without it and the change is known to be  $m_{ph}^* = m_0^* (1 + \lambda)$  where the subscripts  $ph$  and  $0$  refer to the presence and absence of electron-phonon interactions. The quantity  $\lambda$  is a measure of the ionic contribution to screening and is approximately given by an integral over the Fermi surface of the inverse electronic velocity  $|v(k)|^{-1}$ , multiplied by  $e^2/(2\pi^2 k_0^2)$  where  $k_0$  is the Thomas-Fermi wave vector [1].

In heavy fermion systems the effect of the electron-phonon interaction is quite different. First one must recall the origin of the heavy quasiparticle mass. Considering the system as a Kondo lattice, a singlet is formed at low temperatures at each rare earth or actinide site between the  $f$  electrons and the conduction electrons. The energy gain due to the singlet formation is denoted by  $E_0 = -k_B T^*$  where  $T^*$  is the equivalent of the Kondo temperature for the lattice. It defines the low energy scale of the system. In particular, the quasiparticle mass  $m_0^*$  is proportional to  $(T^*)^{-1}$  [2].

When the electron-phonon interaction is turned on the energy gain due to singlet formation increases. The hybridization of the  $f$  electrons with the conduction electrons on which  $T^*$  crucially depends, increases when the neighbors move closer to an  $f$  site. A measure of this change is provided by the electronic Grüneisen pa-

rameter [3].

$$\eta = -\frac{\Omega}{T^*} \frac{dT^*}{d\Omega} \quad (1)$$

which specifies the change in  $T^*$  which changing volume  $\Omega$ . In heavy fermion systems  $\eta$  is of order 100 [4]. Because the energy gain due to singlet formation is increased by the electron-phonon interaction the effective mass must decrease, because the excitations which break the singlets are spread over a larger energy interval.

In order to quantify the above mentioned effect we assume the zero temperature limit and express the change in the energy of  $N$   $f$ -sites (e.g. Ce ions) in a volume  $\Omega$  as function of a volume change  $\delta\Omega$  as

$$N \delta E_0 = -N k_B \delta T^* + \frac{\Omega}{2} c_B^0 \varepsilon_\Omega^2 \quad (2)$$

where  $\varepsilon_\Omega = \delta\Omega/\Omega$  and  $c_B^0$  is the bulk modulus at  $T=0$ . By making use of (1) we write

$$N \delta E_0 = N k_B T^* \eta \varepsilon_\Omega + \frac{\Omega}{2} c_B^0 \varepsilon_\Omega^2. \quad (3)$$

The energy is minimized by

$$\varepsilon_\Omega = -\frac{n\eta k_B T^*}{c_B^0} \quad (4)$$

where  $n = N/\Omega$  is the density of  $f$  sites. The energy per site in the presence of the electron-phonon interaction is therefore

$$E_0 + \delta E_0 = -k_B T^* \left( 1 + \eta^2 \frac{n k_B T^*}{2 c_B^0} \right). \quad (5)$$

Note the similarity of these findings with the “Kondo volume collapse” [5, 6]. The change in the effective mass is thus given by

$$m_{ph}^* = \frac{m_0^*}{1 + \eta^2 \frac{nk_B T^*}{2c_B^0}} \quad (6)$$

In order to estimate the size of the reduction of  $m_{ph}^*/m_0^*$  we consider  $CeRu_2Si_2$  as an example. The following values are used [7, 8]:

$T^* = 21$  K,  $\eta = 150$ ,  $c_B^0 = 11.2 \cdot 10^{11}$  erg/cm<sup>3</sup>. The volume of the unit cell is  $vol = 171 \text{ \AA}^3$  and contains two Ce ions. When these numbers are inserted into (6) one obtains  $m_{ph}^*/m_0^* = 0.74$ . The effect calculated here is due to a reduction of the strong electron correlations (through an increase of the hybridization of the  $f$  electrons) when one allows for lattice compressions. There will be additional contributions to  $m_{ph}^*$  from phonons with  $q \neq 0$ , which counteract the mass reduction derived here. They are difficult to calculate quantitatively, but we expect them to be relatively small in the systems of interest.

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