

Spin structure of ^3He studied by deuteron and nucleon knockout processes

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Bled Mini-Workshop, 8 July 2014

Experiments covered in this talk

- E05-102 (Gilad, Higinbotham, Korsch, Norum, Širca)
Double-spin asymmetries in quasi-elastic ${}^3\vec{\text{He}}(\vec{e}, e'd)p$
 ${}^3\vec{\text{He}}(\vec{e}, e'p)d$
 ${}^3\vec{\text{He}}(\vec{e}, e'p)pn$
- E05-015 (Averett, Chen, Xiang)
Target single-spin asymmetry in quasi-elastic ${}^3\text{He}^\uparrow(e, e')$
- E08-005 (Averett, Higinbotham, Sulkosky)
Target single-spin asymmetry in quasi-elastic ${}^3\text{He}^\uparrow(e, e'n)$
Double-spin asymmetries in quasi-elastic ${}^3\vec{\text{He}}(\vec{e}, e'n)$
- Project ‘N’ (Sfienti, Pohodzalla, Distler)
Subproject (Distler): triple-polarized ${}^3\vec{\text{He}}(\vec{e}, e'\vec{p})$

Analysis work done by **Elena Long** (Kent State U)

Miha Mihovilovič (U of Ljubljana)
Yawei Zhang (Rutgers)
Markus Weinriefer (Mainz)

Physics motivation for studying processes on ${}^3\text{He}$

- Knowledge of ground-state structure of ${}^3\text{He}$ needed to **extract information on the neutron** from ${}^3\vec{\text{He}}(\vec{e}, e'X)$ or ${}^3\vec{\text{He}}(\vec{e}, e')$. Examples: G_E^n , G_M^n , A_1^n , g_1^n , g_2^n , GDH.
- Complications: protons in ${}^3\text{He}$ partly polarized due to presence of S' - and D -state components.
- Addressing differences in $\sqrt{\langle r^2 \rangle}$ (${}^3\text{H}$, ${}^3\text{He}$).
- Understanding (iso)spin dependence of reaction mechanisms (MEC, IC).
- Understanding role of D and S' states is one of key issues in **“Standard Model” of few-body theory**.
- **Persistent discrepancies among theories** regarding double-polarization observables most sensitive to ${}^3\text{He}$ ground-state structure.

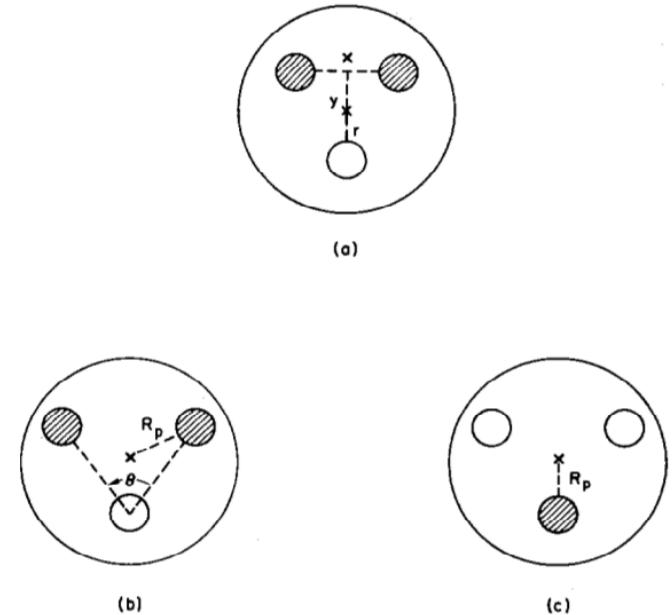
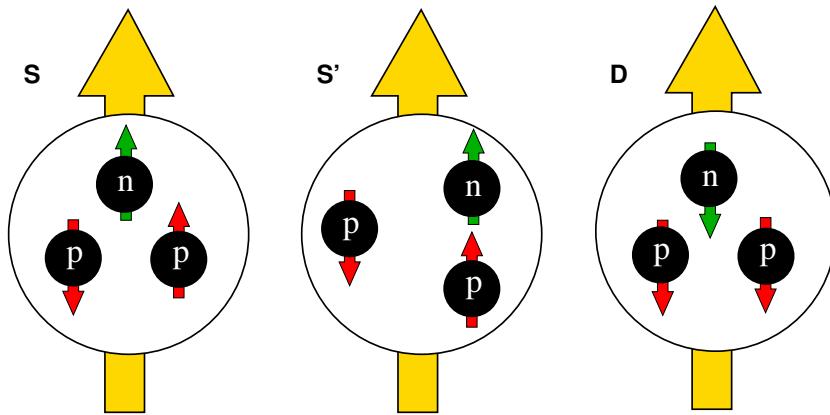


Fig. 1. Schematic picture of trinucleon when all forces are identical is shown in (a). The effect on ${}^3\text{He}$ and ${}^3\text{H}$ when the pp or nn force is weaker than the np force is illustrated in (b) and (c). R_p is the “charge radius”. Shading indicates a proton.

Polarized ^3He : it is easy to draw the cartoon...



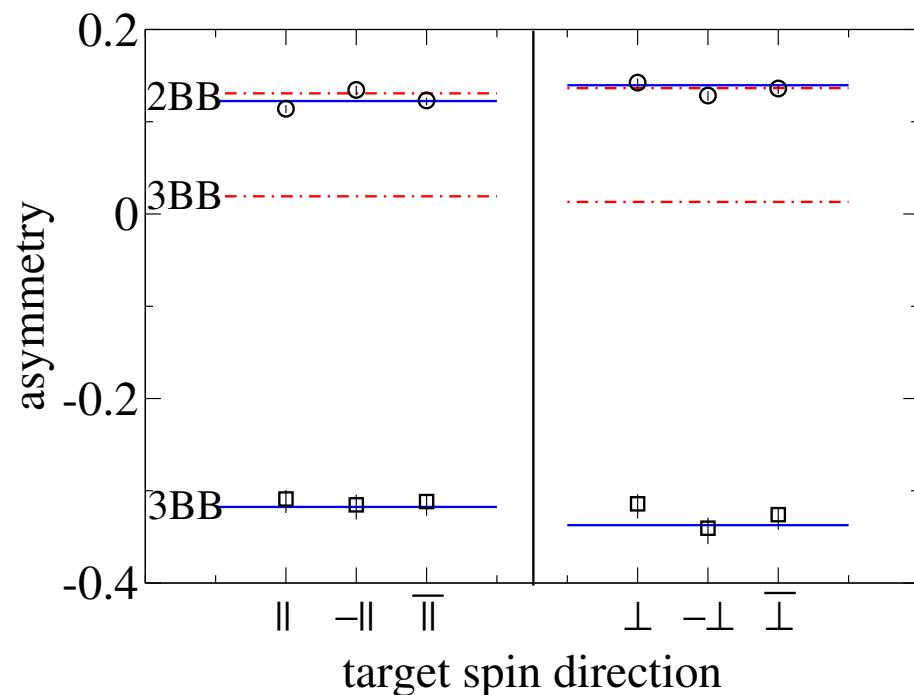
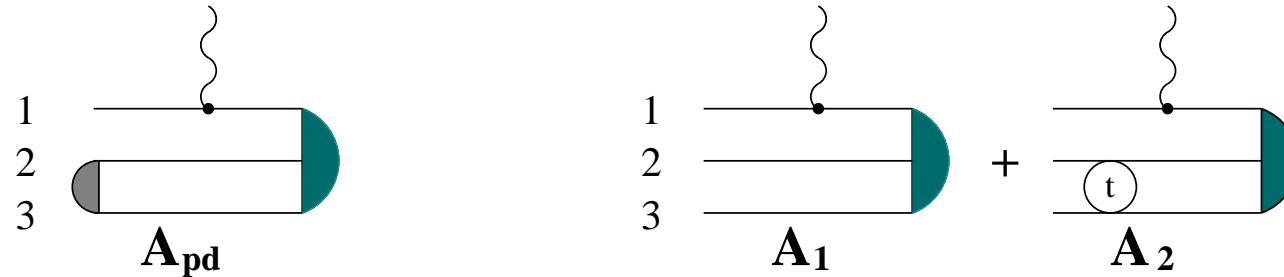
- S : spatially symmetric
≈ 90% of spin-averaged WF;
“polarized neutron”
- D : generated by tensor part
of NN force, ≈ 8.5% .
- S' : mixed symmetry component;
(spin-isospin)-space correlations,
≈ 1.5% . $P'_S \approx E_b^{-2.1}$.
- $P_n^{\text{eff}} \approx +0.86$, $P_p^{\text{eff}} \approx -0.03$

Hamiltonian	S	S'	P	D
AV18	90.10	1.33	0.066	8.51
AV18/TM	89.96	1.09	0.155	8.80
AV18/UIX	89.51	1.05	0.130	9.31
CD-Bonn	91.62	1.34	0.046	6.99
CD-Bonn/TM	91.74	1.21	0.102	6.95
Nijm I	90.29	1.27	0.066	8.37
Nijm I/TM	90.25	1.08	0.148	8.53
Nijm II	90.31	1.27	0.065	8.35
Nijm II/TM	90.22	1.07	0.161	8.54
Reid93	90.21	1.28	0.067	8.44
Reid93/TM	90.09	1.07	0.162	8.68

Schiavilla++ PRC 58 (1998) 1263
 TM = Tucson-Melbourne π - π exchange 3NF
 UIX = Urbana 3NF

...supported e.g. by data on ${}^3\vec{\text{He}}(\vec{e}, e' p)d/\bar{p}n$...

- quasi-elastic ($Q^2 = 0.31$, $\omega = 135$, $q = 570$)
- 3NF, MEC negligible, FSI small in 2bbu, large in 3bbu

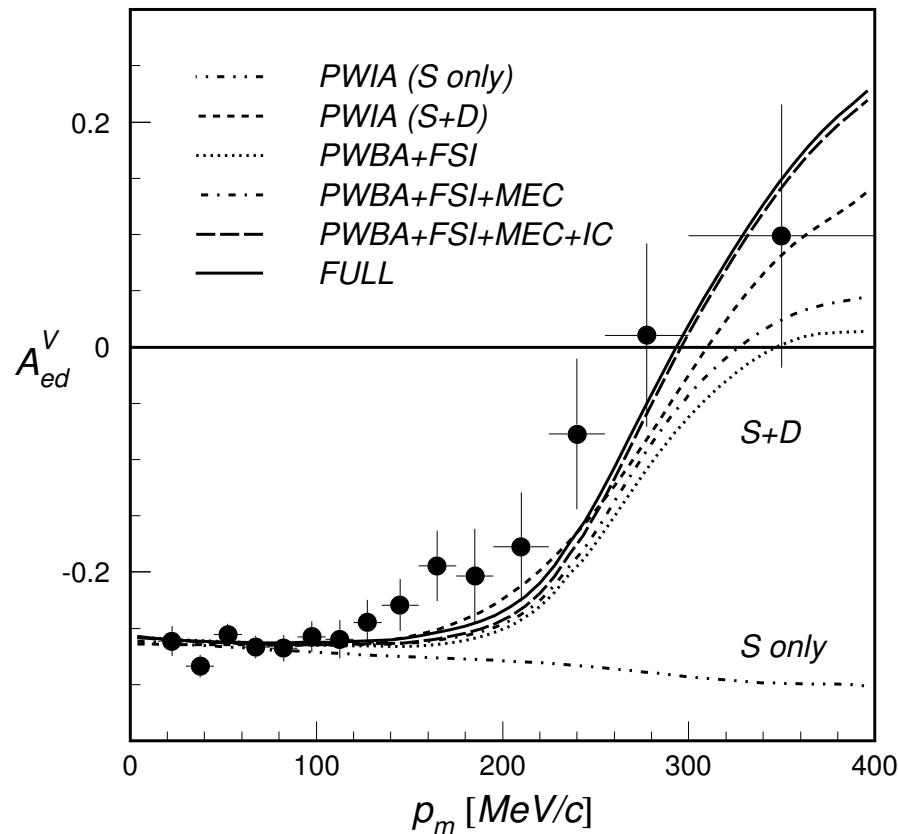


- ▷ **2bbu**
 $A_{\text{PWIA}} \approx A_{\text{PWIA+FSI}}$
 \parallel kinematics + small p_d
 \Rightarrow polarized p target, $P_p \approx -\frac{1}{3}P_{\text{He}}$
- ▷ **3bbu**
 $A_{\text{PWIA}} \approx 0$ ($p \uparrow p \downarrow$)
 $A_{\text{PWIA+FSI}}$ large & negative
not a polarized p target

PRC 72 (2005) 054005, EPJA 25 (2005) 177

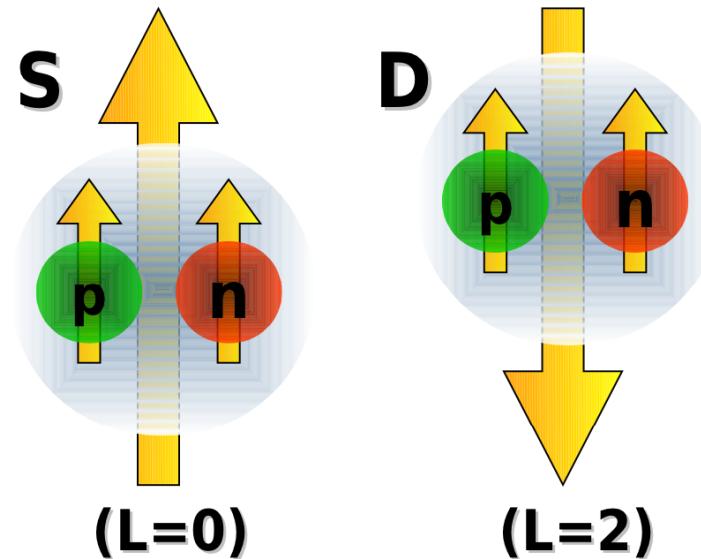
...and which has a nice analogue in the deuteron...

$\vec{d}(\vec{e}, e' p)$



$$\sigma = \sigma_0 \left(1 + h P_1^d A_{ed}^V \right)$$

$$P_z^p = \sqrt{\frac{2}{3}} \left(P_S - \frac{1}{2} P_D \right) P_1^d$$



Passchier++ PRL **82** (1999) 4988

Passchier++ PRL **88** (2002) 102302

...but the true ground state of ${}^3\text{He}$ is like lace

Channel number	L	S	l_α	L_α	P	K	Probability (%)
1	0	0.5	0	0	A	1	87.44
2	0	0.5	0	0	M	2	0.74
3	0	0.5	1	1	M	1	0.74
4	0	0.5	2	2	A	1	1.20
5	0	0.5	2	2	M	2	0.06
6	1	0.5	1	1	M	1	0.01
7	1	0.5	2	2	A	1	0.01
8	1	0.5	2	2	M	2	0.01
9	1	1.5	1	1	M	1	0.01
10	1	1.5	2	2	M	2	0.01
11	2	1.5	0	2	M	2	1.08
12	2	1.5	1	1	M	1	2.63
13	2	1.5	1	3	M	1	1.05
14	2	1.5	2	0	M	2	3.06
15	2	1.5	2	2	M	2	0.18
16	2	1.5	3	1	M	1	0.37

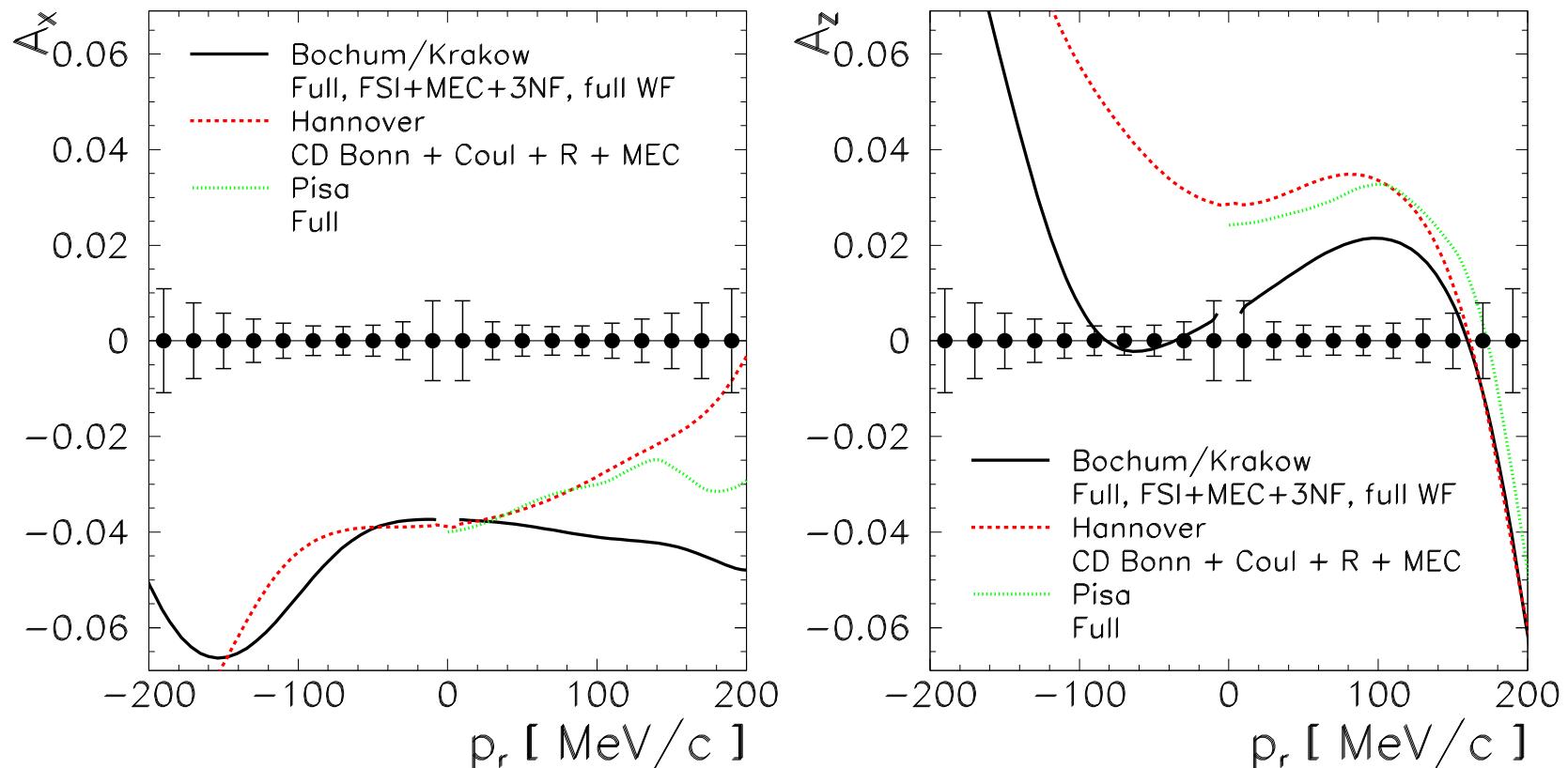
Blankleider, Woloshyn PRC 29 (1984) 538

Meeting point of theory and experiment

e.g. ${}^3\vec{\text{He}}(\vec{e}, e'd)$

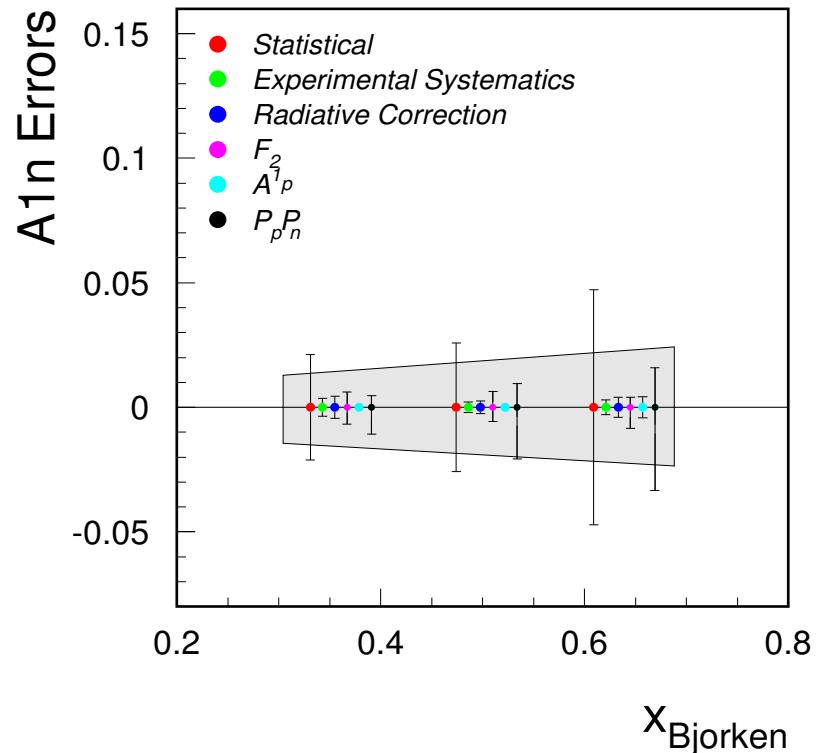
$$\frac{d\sigma(h, \vec{S})}{d\Omega_e dE_e d\Omega_d dp_d} = \frac{d\sigma_0}{\dots} \left[1 + \vec{S} \cdot \vec{A}^0 + h(\mathcal{A}_e + \vec{S} \cdot \vec{A}) \right]$$

$$A_{x,z} = \frac{[d\sigma_{++} + d\sigma_{--}] - [d\sigma_{+-} + d\sigma_{-+}]}{[d\sigma_{++} + d\sigma_{--}] + [d\sigma_{+-} + d\sigma_{-+}]}$$

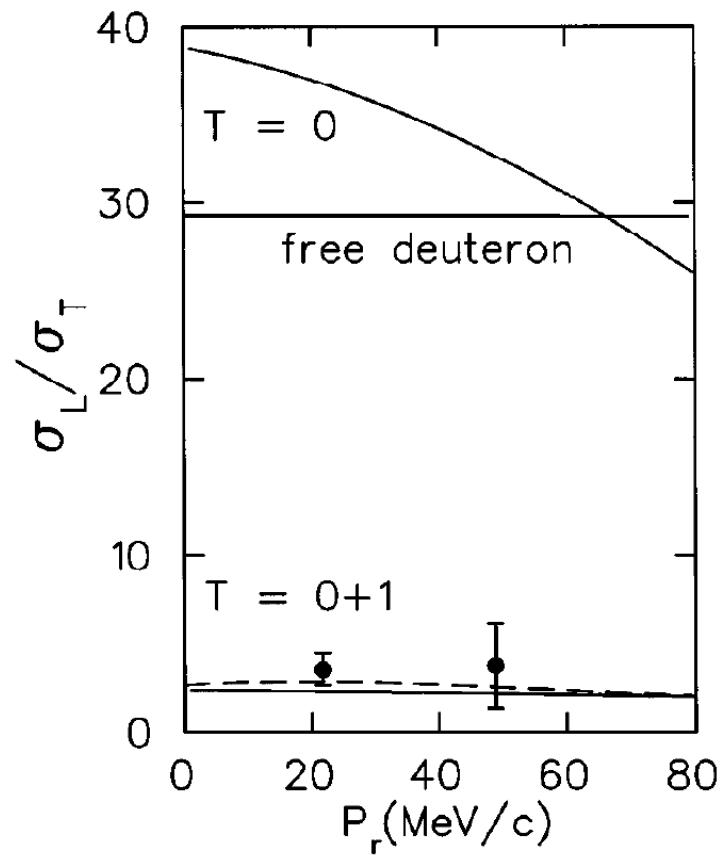


The E05-102 and E08-005 experiments at JLab

- **Benchmark measurement** of A'_x and A'_z asymmetries in ${}^3\vec{\text{He}}(\vec{e}, e'd)$, ${}^3\vec{\text{He}}(\vec{e}, e'p)$, and ${}^3\vec{\text{He}}(\vec{e}, e'n)$.
- **Better understanding of ground-state spin structure of polarized ${}^3\text{He}$** —
 - S, S', D wave-function components.
 - Improve knowledge of ${}^3\text{He}$ rather than using it as an effective neutron target.
- **Direct consequences for all polarized ${}^3\text{He}$ experiments.**
- Distinct manifestations of S, D, S' with changing p_{miss} in $(e, e'\{p/d/n\})$.
- Data at (almost) identical Q^2 for $(\vec{e}, e'd)$, $(\vec{e}, e'p)$, and $(\vec{e}, e'n)$ simultaneously over a broad range of p_{miss} poses **strong constraints on state-of-the-art calculations**.

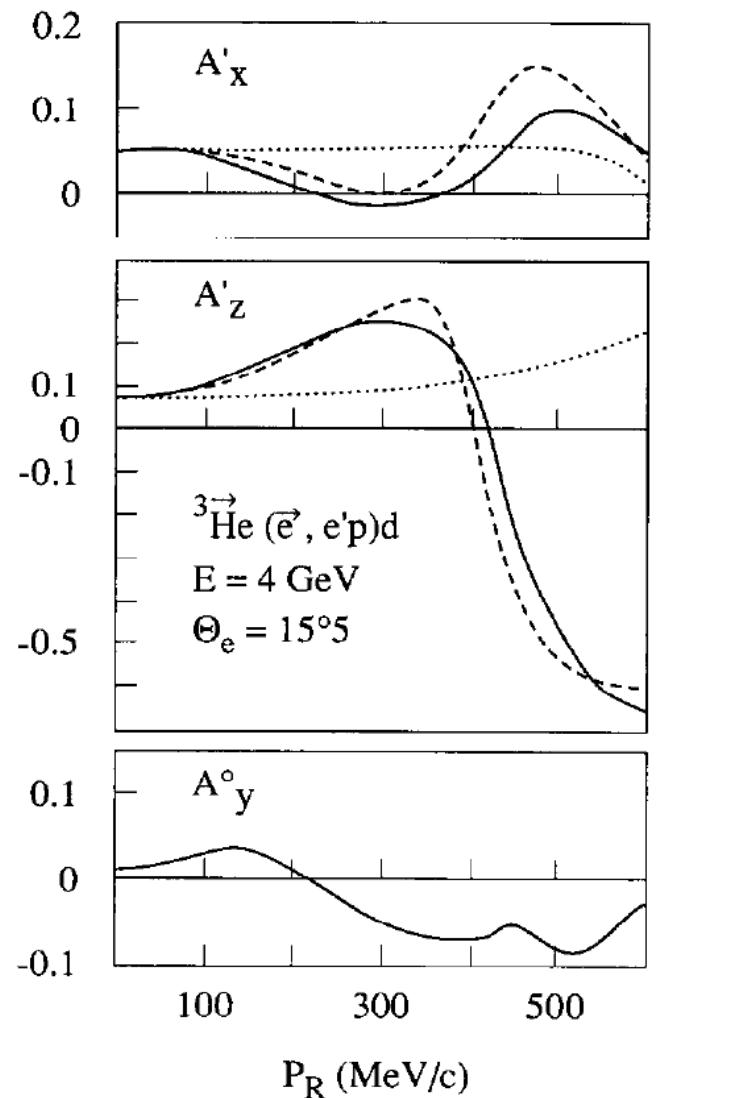


What is so special about ${}^3\text{He}(\text{e}, \text{e}'\text{d})$ and ${}^3\vec{\text{He}}(\vec{\text{e}}, \text{e}'\text{d})$?



**unique isoscalar-isovector
interference in $(\text{e}, \text{e}'\text{d})$**

Tripp++ PRL 76 (1996) 885



**in $(\text{e}, \text{e}'\text{p})$ the D/S' effects
seen only at high p_{miss}**

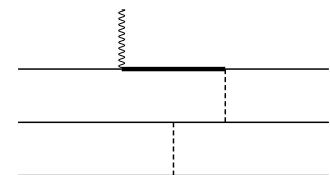
Exploiting state-of-the-art calculations

Bochum/Krakow (full Faddeev)

- AV18 NN-potential (+ Urbana IX 3NF, coming up...)
- Complete treatment of FSI, MEC

Hannover/Lisbon (full Faddeev)

- CC extension and refit of CD-Bonn NN-potential
- Includes FSI, MEC
- Δ as active degree-of-freedom providing effective 3NF and 2-body currents
- Coulomb interaction for outgoing charged baryons



Pisa

PRC 72 (2005) 014001

- AV18 + Urbana IX (or IL7)
- Inclusion of FSI by means of the variational PHH expansion and MEC
- Not Faddeev, but accuracy completely equivalent to it

Trento

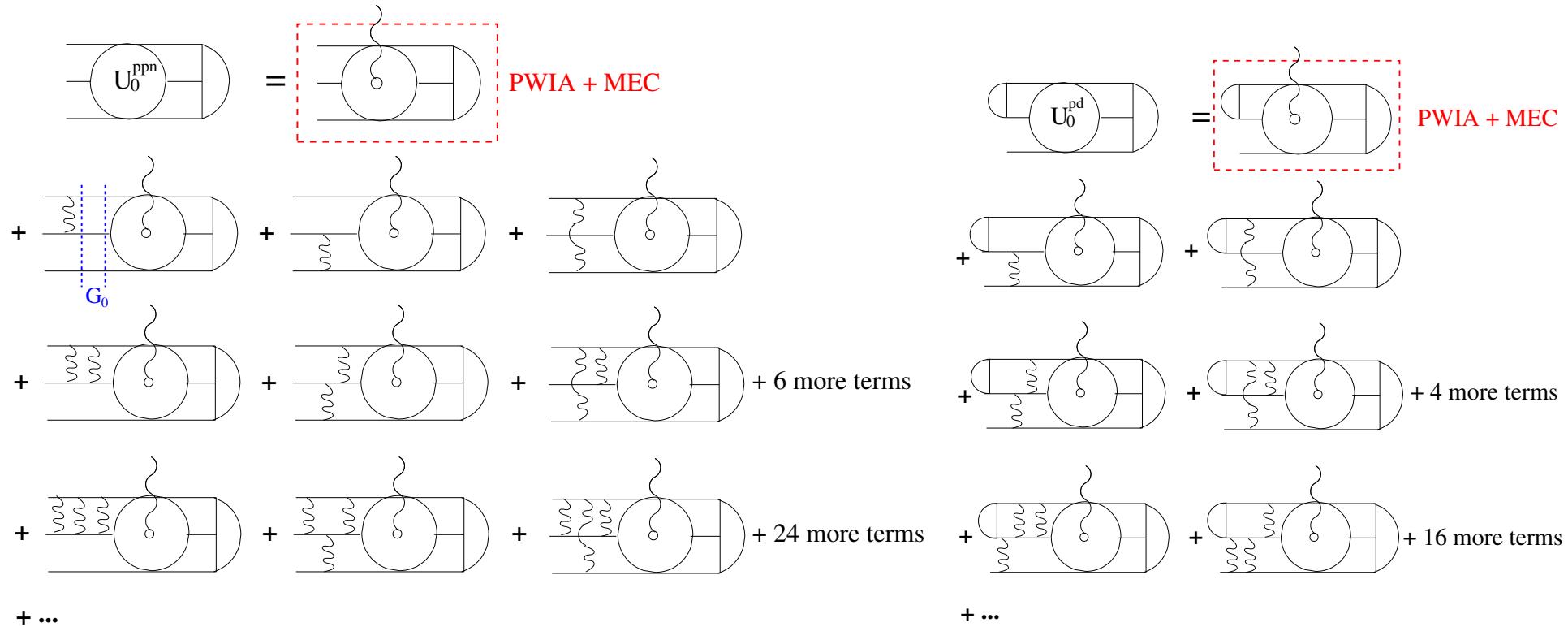
- Coming up

Basic machinery: Faddeev calculations

Nuclear transition current for breakup of ${}^3\text{He}$: $J^\mu = \langle \Psi_f | \hat{\mathcal{O}}^\mu | \Psi_{{}^3\text{He}}(\theta^*, \phi^*) \rangle$

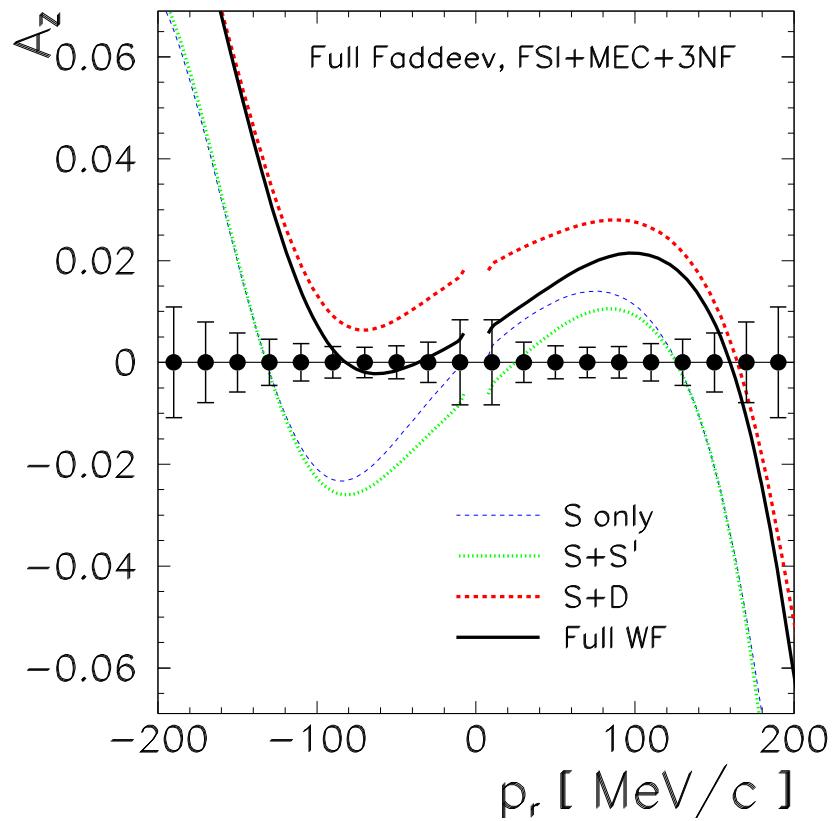
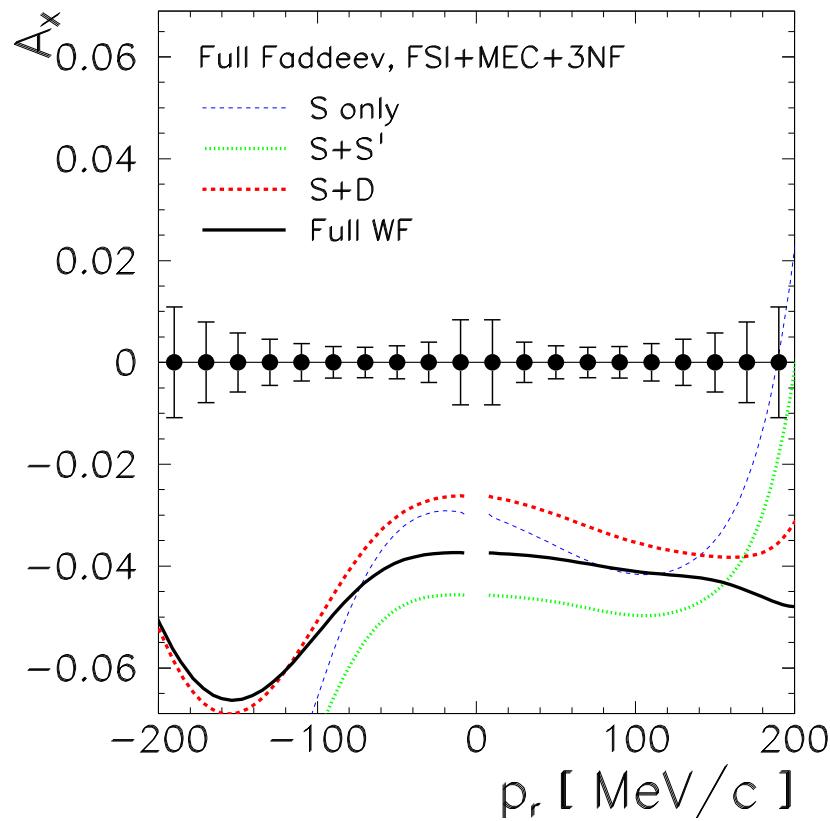
Photon absorption operator: $\hat{\mathcal{O}}^\mu = \sum_{i=1}^3 [\hat{J}_{\text{SN}}(i) + \hat{J}_{\text{MEC}}(i)]$

Final-state interactions (auxiliary states): $\langle \Psi_f | \hat{\mathcal{O}}^\mu | \Psi_{{}^3\text{He}}(\theta^*, \phi^*) \rangle \rightarrow \langle \Psi_f | U_f^\mu \rangle$



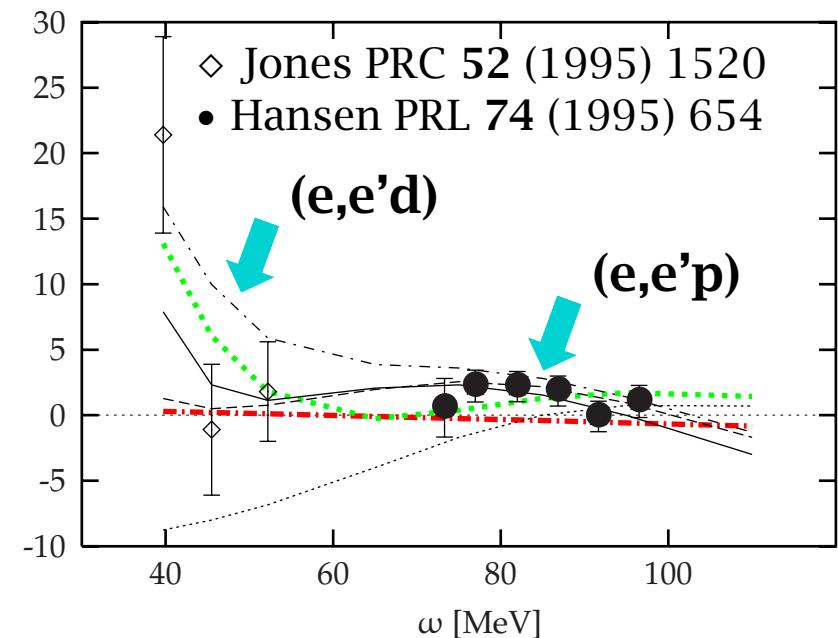
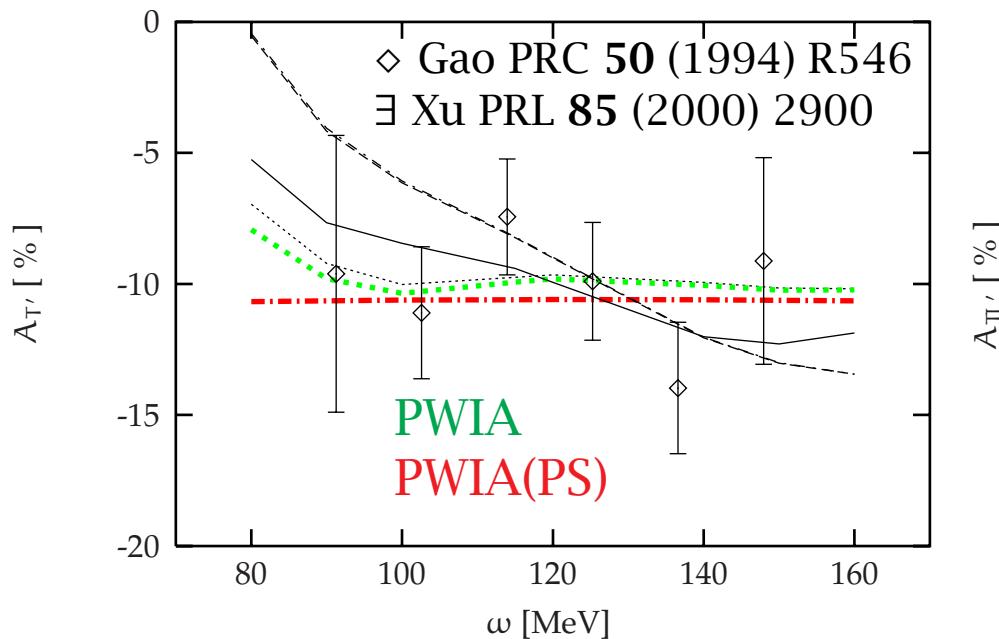
Role of WF components in ${}^3\vec{\text{He}}(\vec{e}, e'd)$

KRAKOW/BOCHUM



Indication of D and S' components in ${}^3\vec{\text{He}}(\vec{e}, e')$

Inclusive $A'_T (= A_z)$ and $A'_{LT} (= A_x)$

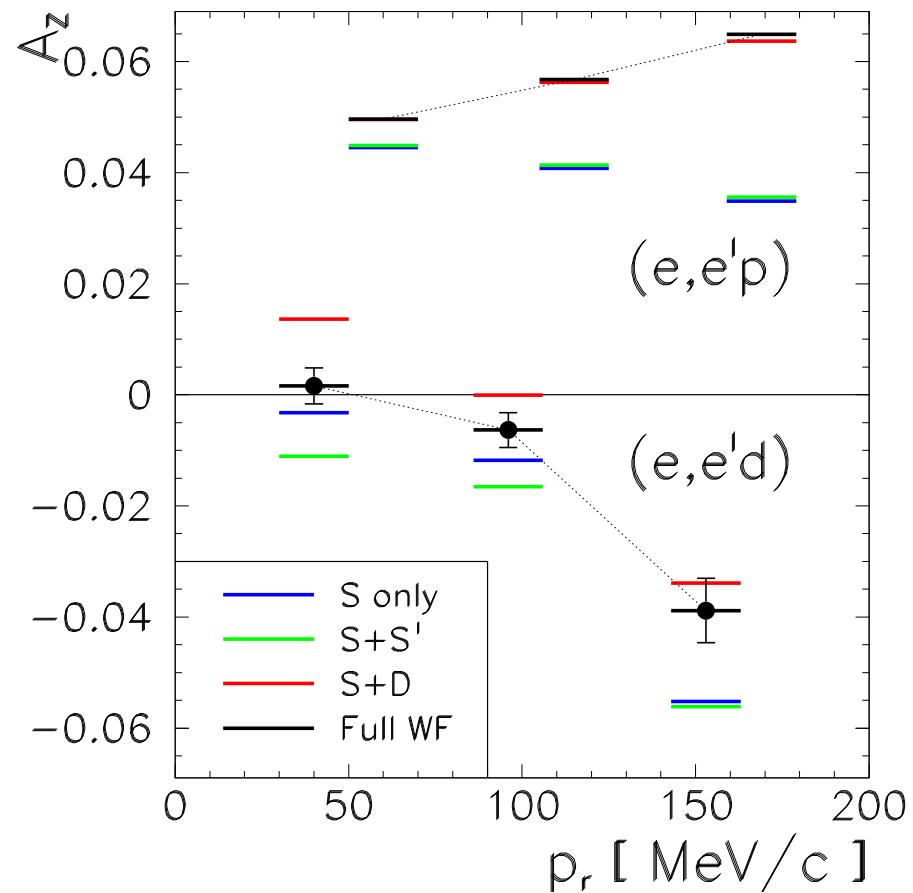
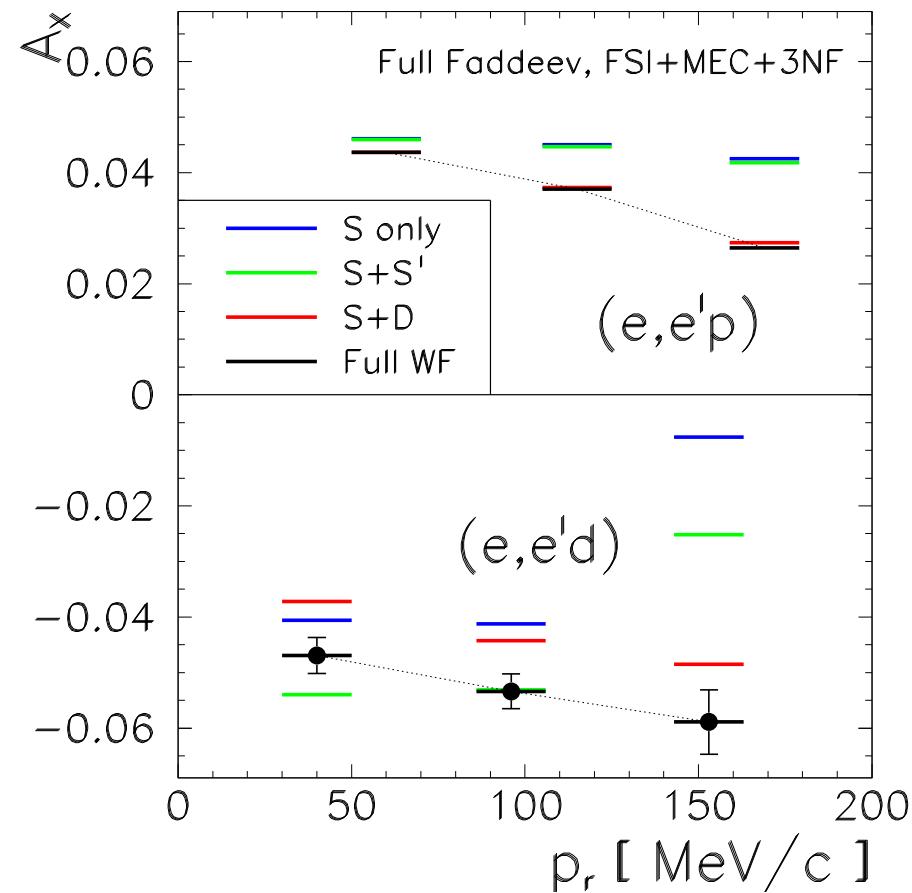


- A'_{LT} receives contributions from ingredients which go beyond most simplistic picture [$F_1^{(n)} = 0$]
- sensitive to replacement PWIA(PS) → PWIA.
- S' - and D -state pieces contribute very strongly to A'_{LT}

Ishikawa, Golak, Glöckle et al. PRC 57 (1998) 39

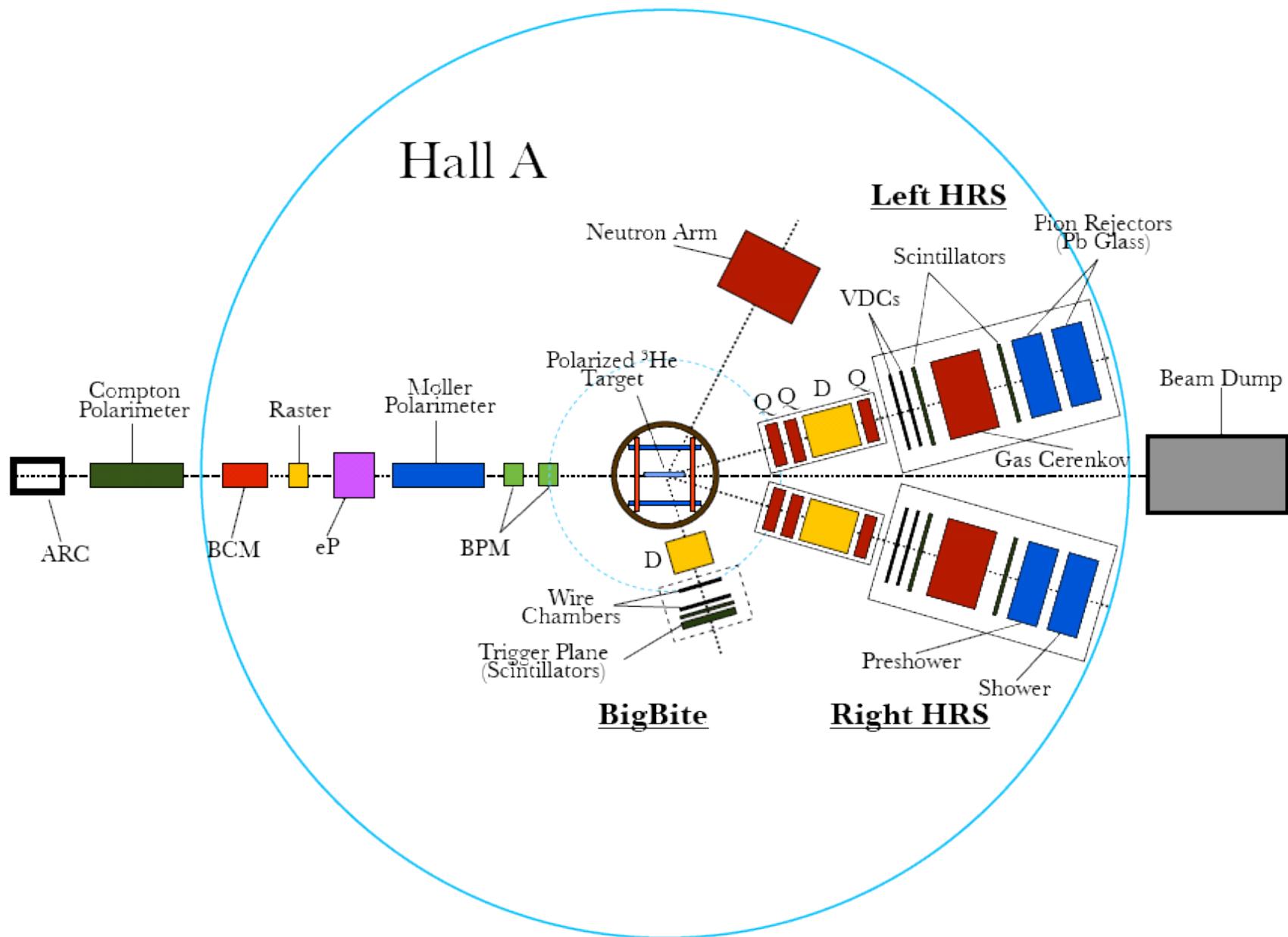
${}^3\vec{\text{He}}(\vec{e}, e'd)$ vs. ${}^3\vec{\text{He}}(\vec{e}, e'p)$

KRAKOW/BOCHUM

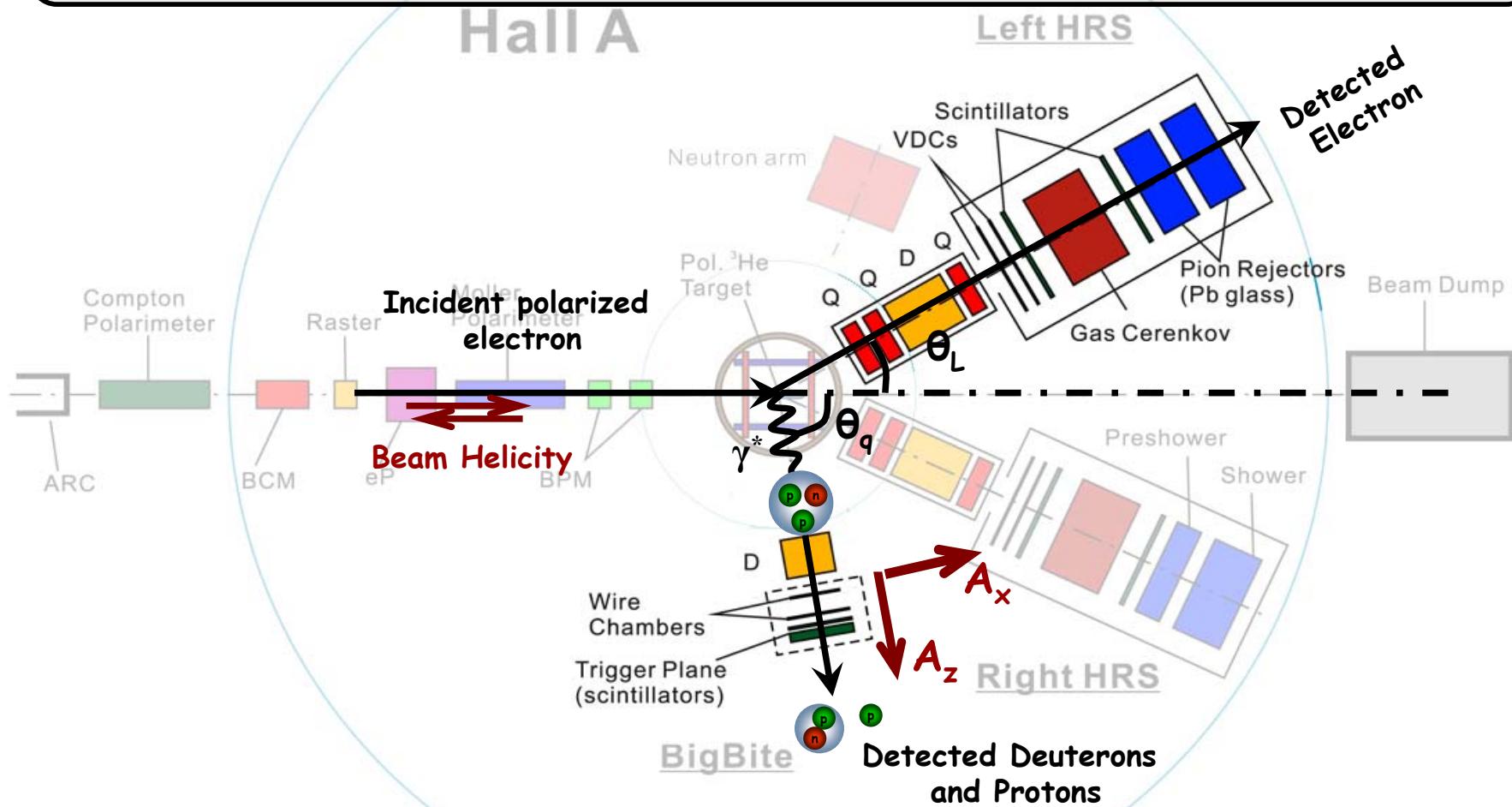


How do we do it?

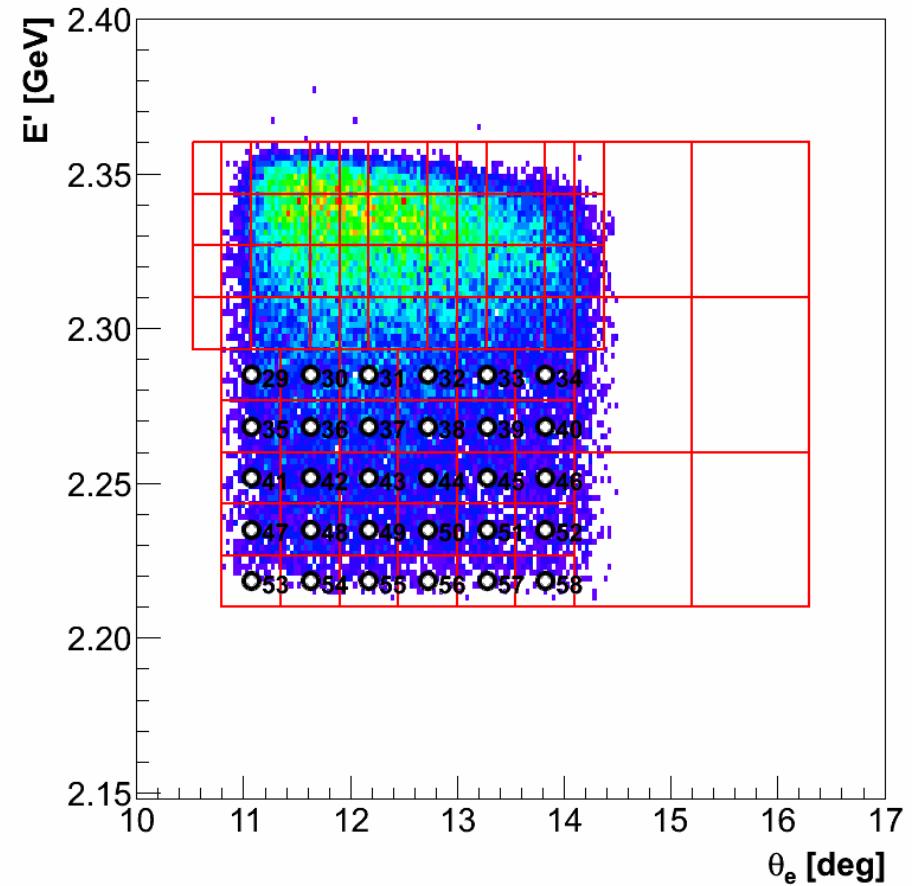
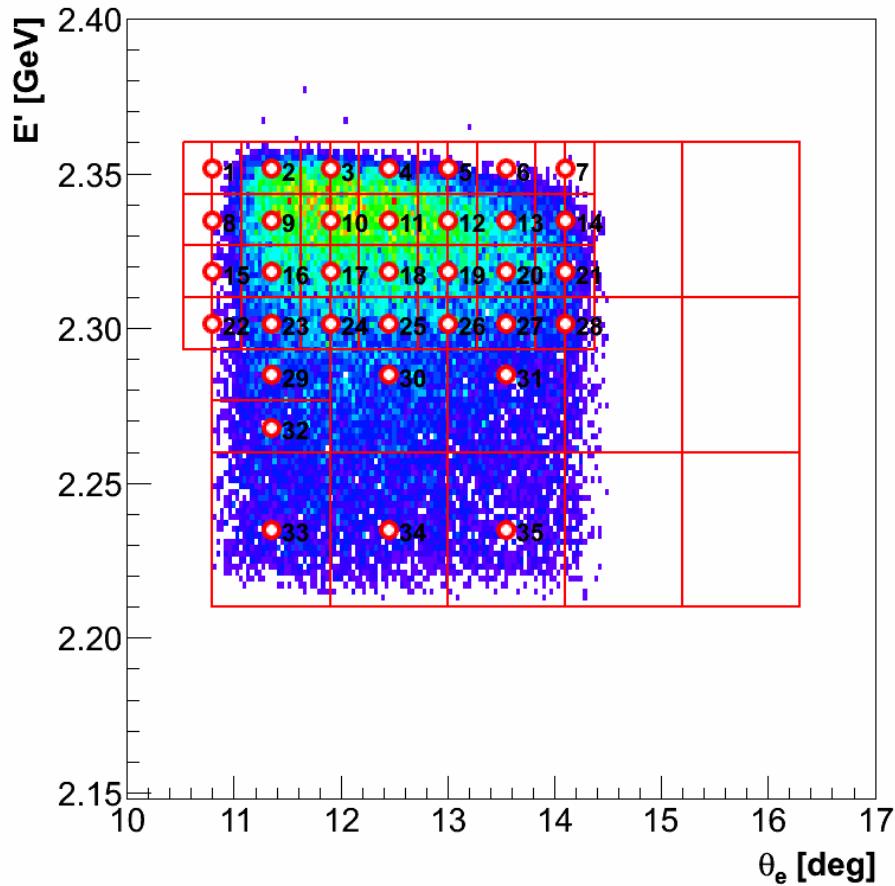
EXPERIMENTAL SETUP



Experiment E05-102 in Hall-A



Acceptance-averaging of ${}^3\text{He}(\vec{e}, e' p)$ and ${}^3\text{He}(\vec{e}, e' d)p$

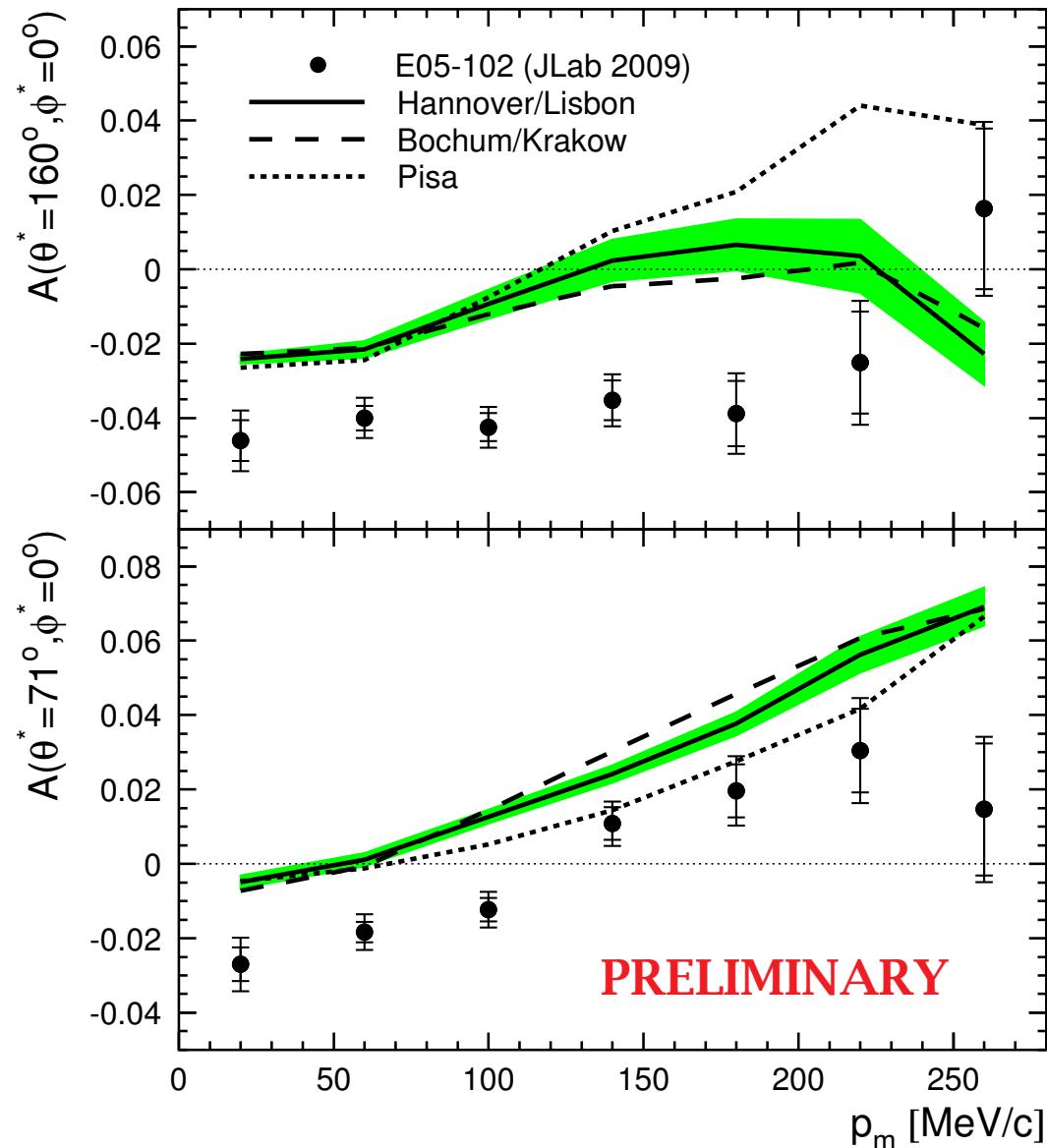


- Krakow/Bochum
- Hannover/Lisbon
- Pisa

- Hannover/Lisbon

Comparison with the theory

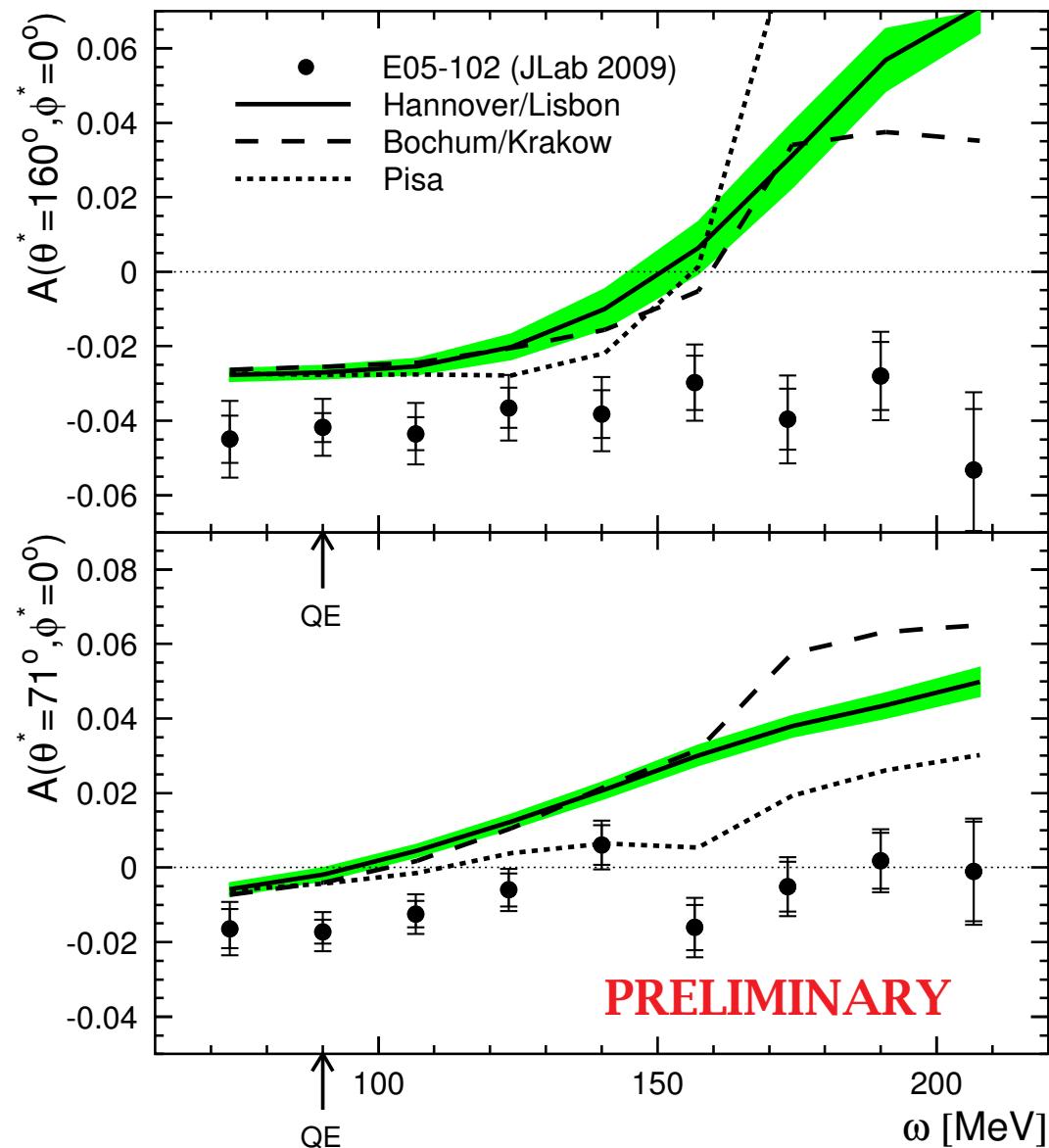
${}^3\vec{\text{He}}(\vec{e}, e'd)p$



PRELIMINARY

Comparison with the theory

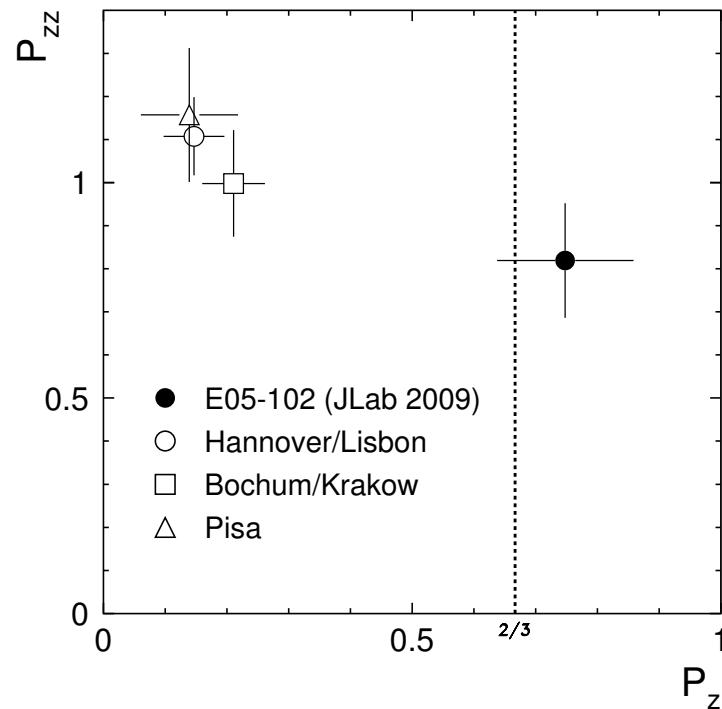
${}^3\vec{\text{He}}(\vec{e}, e'd)p$



The question of P_z and P_{zz}

${}^3\vec{\text{He}}(\vec{e}, e'd)p$

- assume ${}^3\vec{\text{He}}(\vec{e}, e'd)p$ at low p_{miss} is like elastic scattering off polarized d
- use $A_x^{({}^3\text{He})}$, $A_z^{({}^3\text{He})}$ as if they were $A_x^{(\text{ed})}$, $A_z^{(\text{ed})}$ with appropriate deuteron FFs, and extract P_z and P_{zz}
- toy model $|{}^3\text{He}\rangle = |\text{d}\rangle + |\text{p}\rangle$
- spin decomposition $|{}^3\text{He}\rangle = \left| \frac{1}{2}, \frac{1}{2} \right\rangle = \sqrt{\frac{2}{3}} |1, 1\rangle \left| \frac{1}{2}, -\frac{1}{2} \right\rangle - \sqrt{\frac{1}{3}} |1, 0\rangle \left| \frac{1}{2}, \frac{1}{2} \right\rangle$ gives $P_z = \langle I_z \rangle_{{}^3\text{He}} = \frac{2}{3}$, $P_{zz} = \langle 3I_z^2 - 2 \rangle_{{}^3\text{He}} = 0$



Preliminary results for asymmetries in ${}^3\vec{\text{He}}(\vec{e}, e' p)$

$$E = 2.4255 \text{ GeV}$$

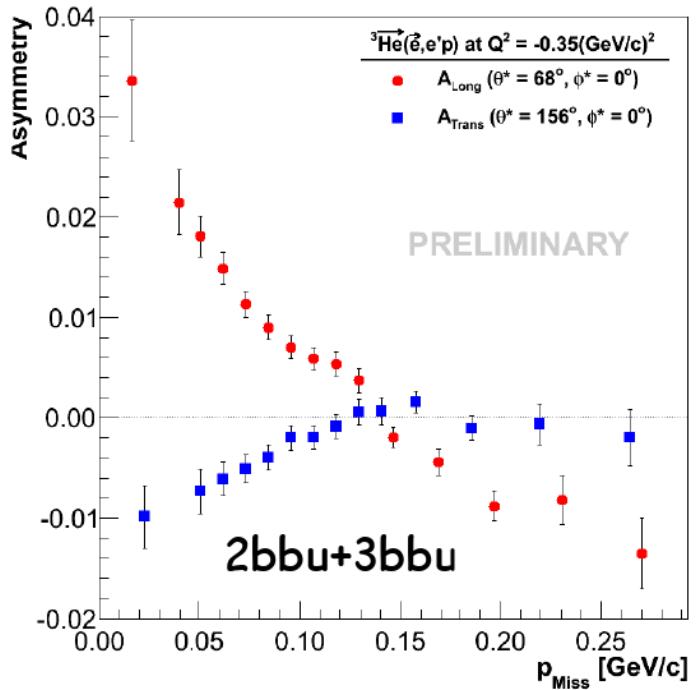
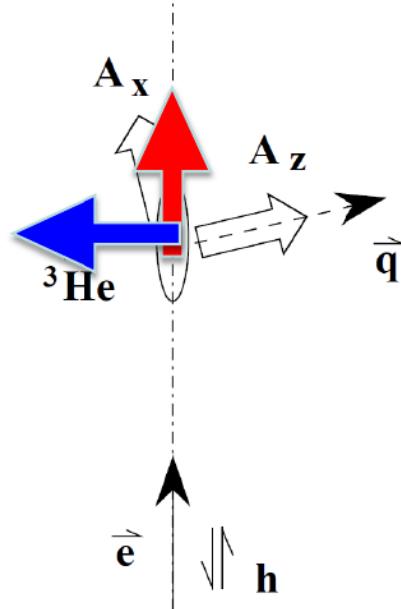
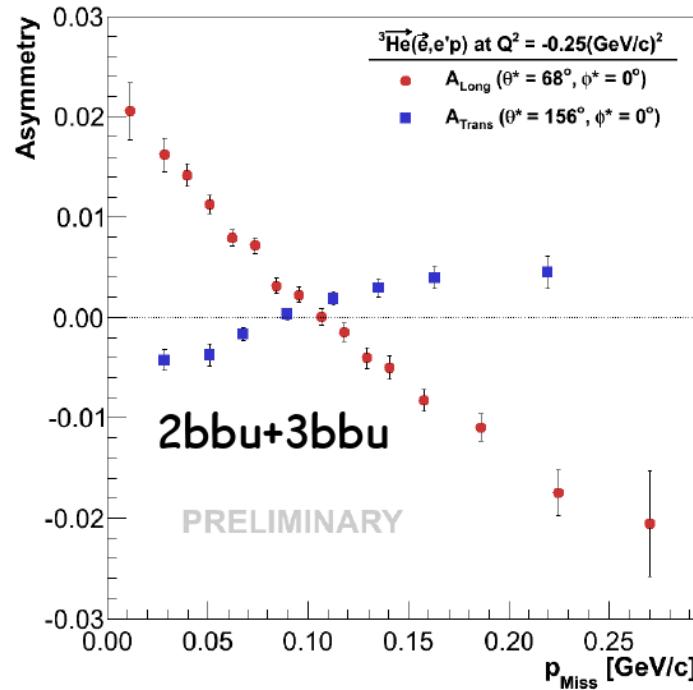
$$\omega = 100 - 200 \text{ MeV}$$

$$Q^2 = 0.2 - 0.3 (\text{GeV}/c)^2$$

$$E = 2.4255 \text{ GeV}$$

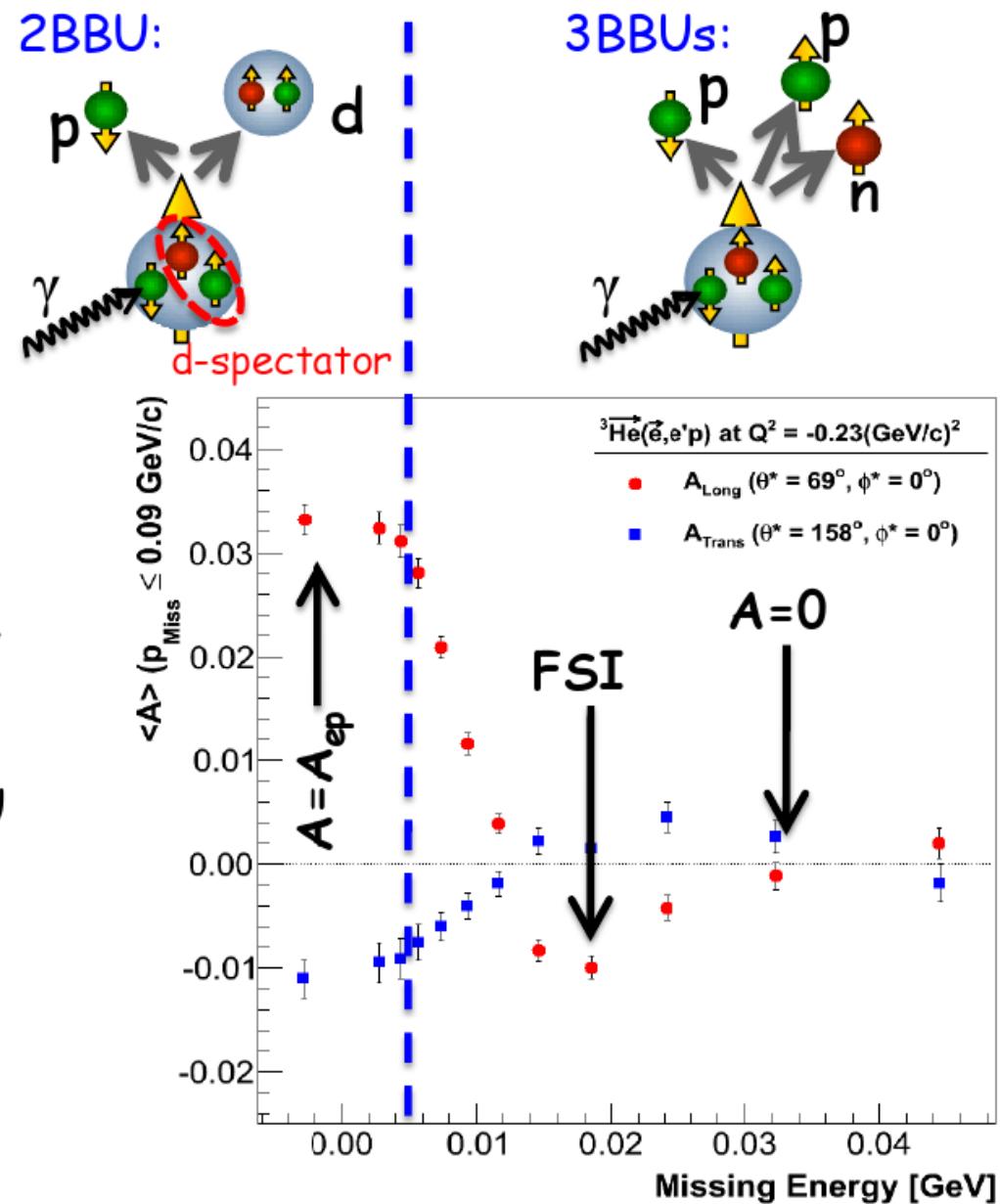
$$\omega = 150 - 250 \text{ MeV}$$

$$Q^2 = 0.3 - 0.4 (\text{GeV}/c)^2$$



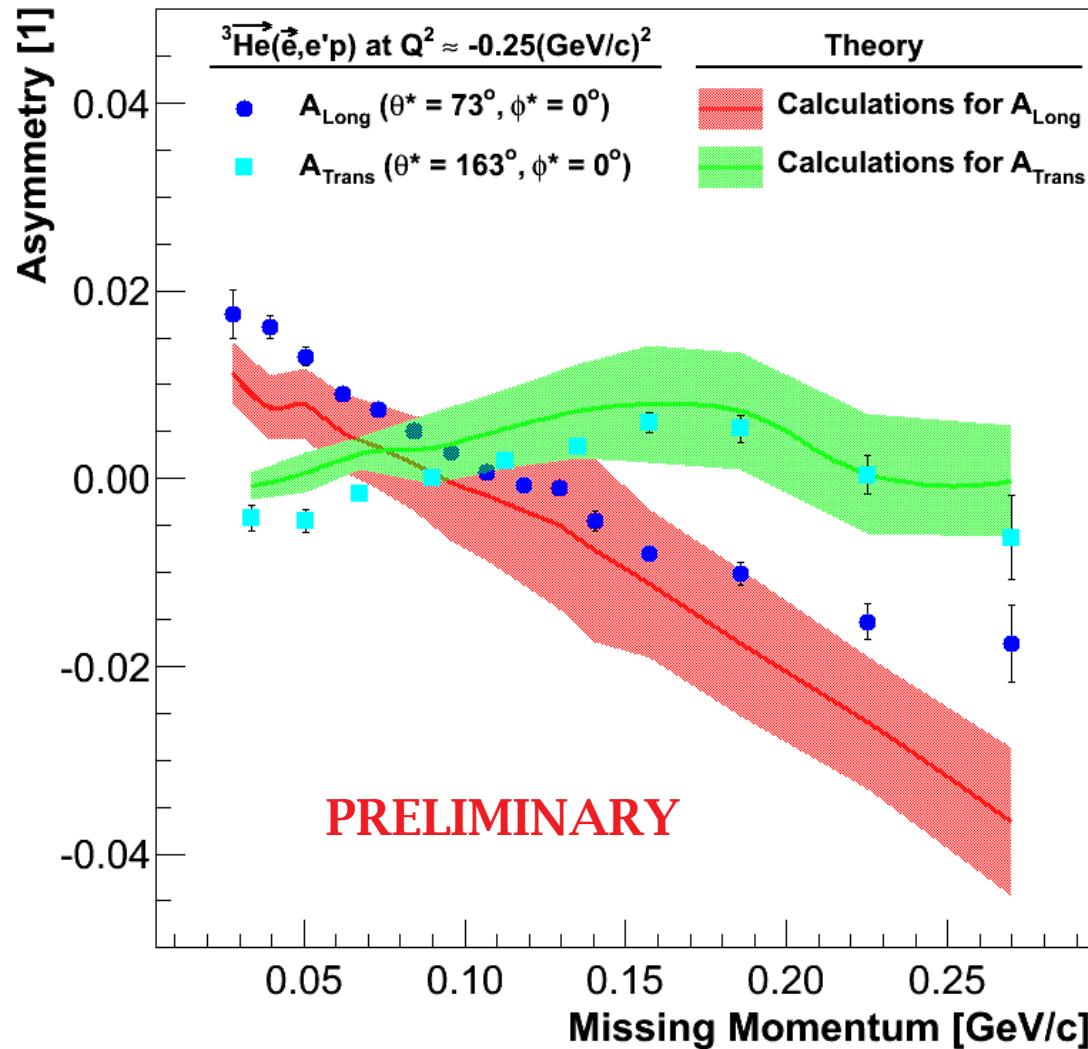
Hand-waving interpretation of ${}^3\vec{\text{He}}(\vec{e}, e' p)$

- Simple picture for $p_{\text{miss}} \sim 0$.
- S-state dominates
- Consider only tree diagram
- Missing Energy = $\omega - T_d - T_p$
- Negative values due to resolution.
- Low E_{Miss} region dominated by 2BBU ($A \rightarrow$ elastic e - p asym.),
- High E_{Miss} dominated by 3BBU ($A \rightarrow 0$).
- Non-zero asymmetry in 3BBU probably caused by FSI.



Comparison with the theory

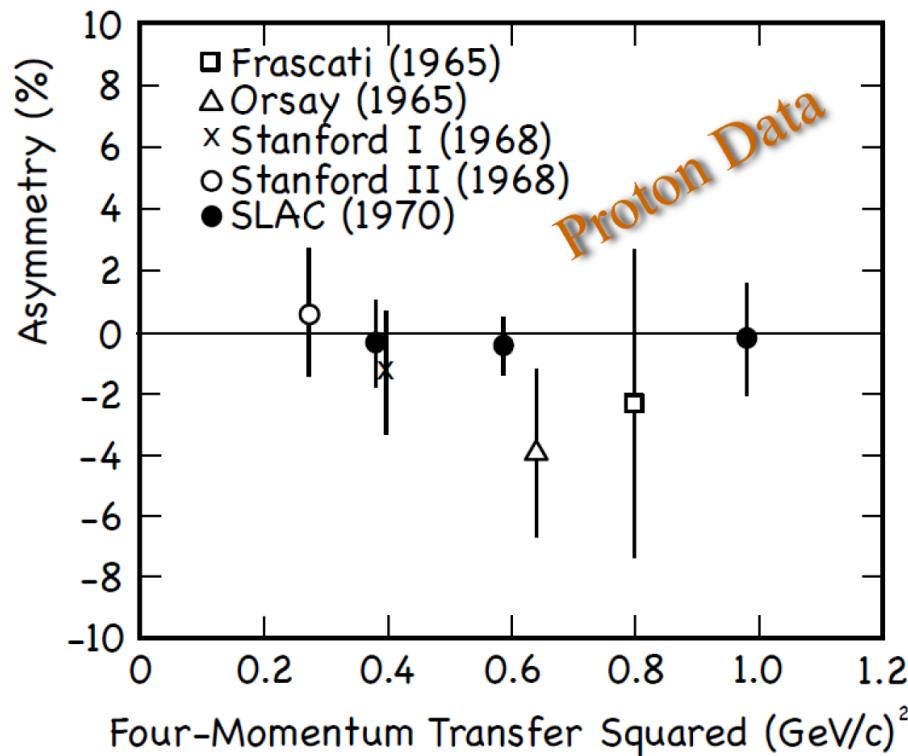
${}^3\vec{\text{He}}(\vec{e}, e' p)$



NB: 2bbu and 3bbu combined, Krakow/Bochum theory only

Single-spin asymmetry in QE ${}^3\text{He}^\uparrow(\text{e}, \text{e}')$

MOTIVATION



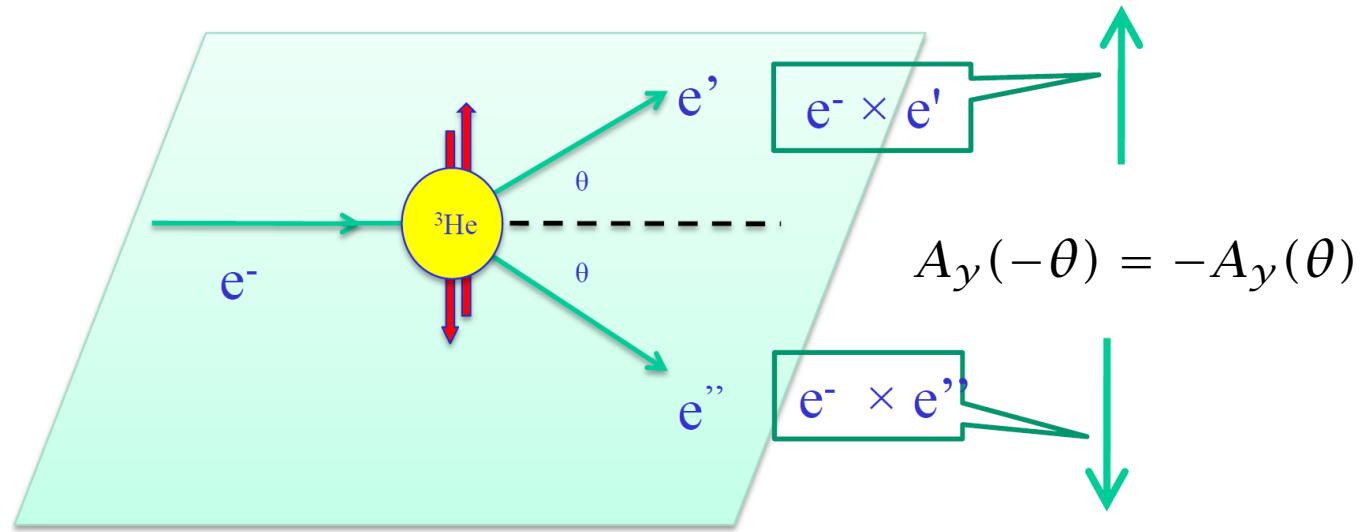
$$A_\gamma = \frac{\sigma^\uparrow - \sigma^\downarrow}{\sigma^\uparrow + \sigma^\downarrow}$$

$$\propto \vec{s} \cdot (\vec{k} \times \vec{k}')$$

- $A_\gamma = 0$ in Born approximation (T -invariance)
- $A_\gamma \neq 0$ indicative of 2γ effects, $\propto \text{Im}\{ T_{1\gamma} T_{2\gamma}^* \}$ interference; relevant for G_E^p/G_M^p , GPDs
- no measurement of comparable precision on **neutron**

Single-spin asymmetry in QE ${}^3\text{He}^\uparrow(\text{e}, \text{e}')$

E05-015



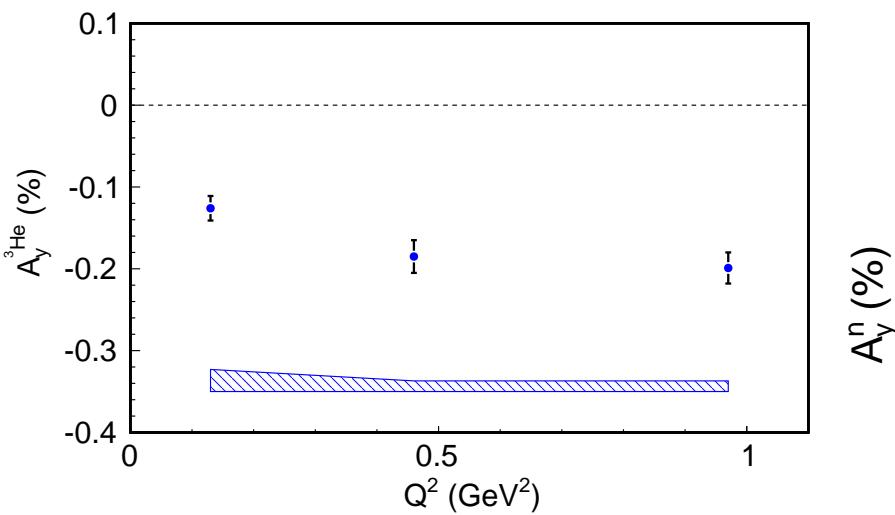
E_0 [GeV]	E' [GeV]	θ_{lab} [Deg]	Q^2 [GeV] ²	$ q $ [GeV]	θ_q [Deg]
1.25	1.22	17	0.13	0.359	71
2.43	2.18	17	0.46	0.681	62
3.61	3.09	17	0.98	0.988	54

Figure & table courtesy of Yawei Zhang, Rutgers

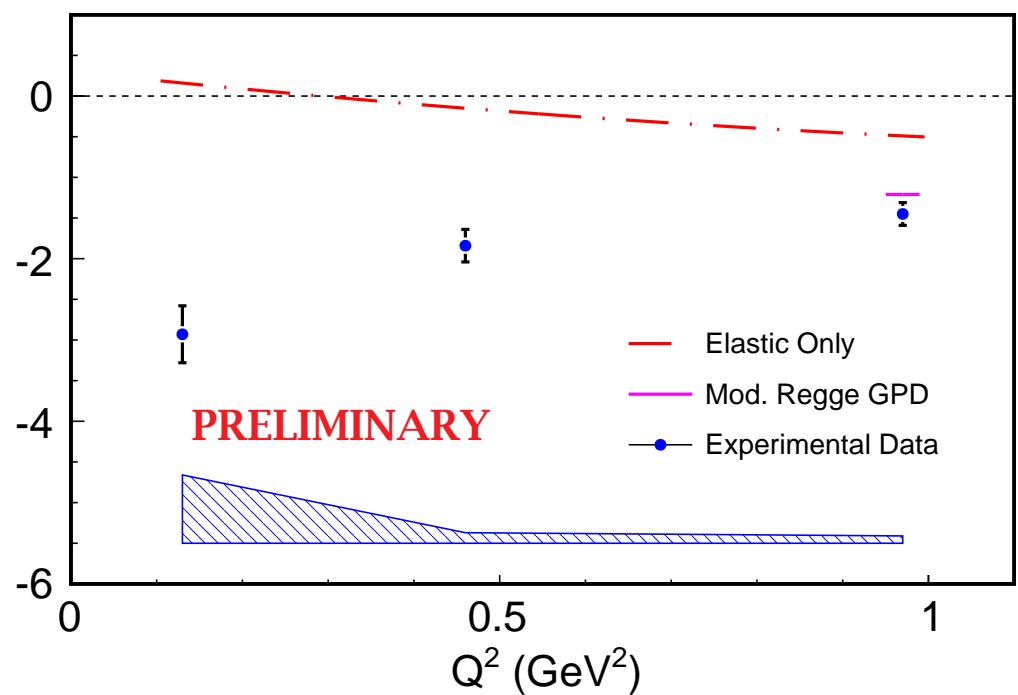
Single-spin asymmetry in QE ${}^3\text{He}^\uparrow(\text{e}, \text{e}')$

E05-015

${}^3\text{He}$



neutron



- first measurement of A_y^n (i.e. extraction from $A_y^{3\text{He}}$)
- uncertainty several times better than previous proton data

Figures courtesy of Yawei Zhang, Rutgers

Single-spin asymmetries in QE ${}^3\text{He}^\uparrow(\vec{e}, e'n)$

E08-005

- a measure of the magnitude of MEC and FSI
- should be zero in PWIA and should die out at high Q^2

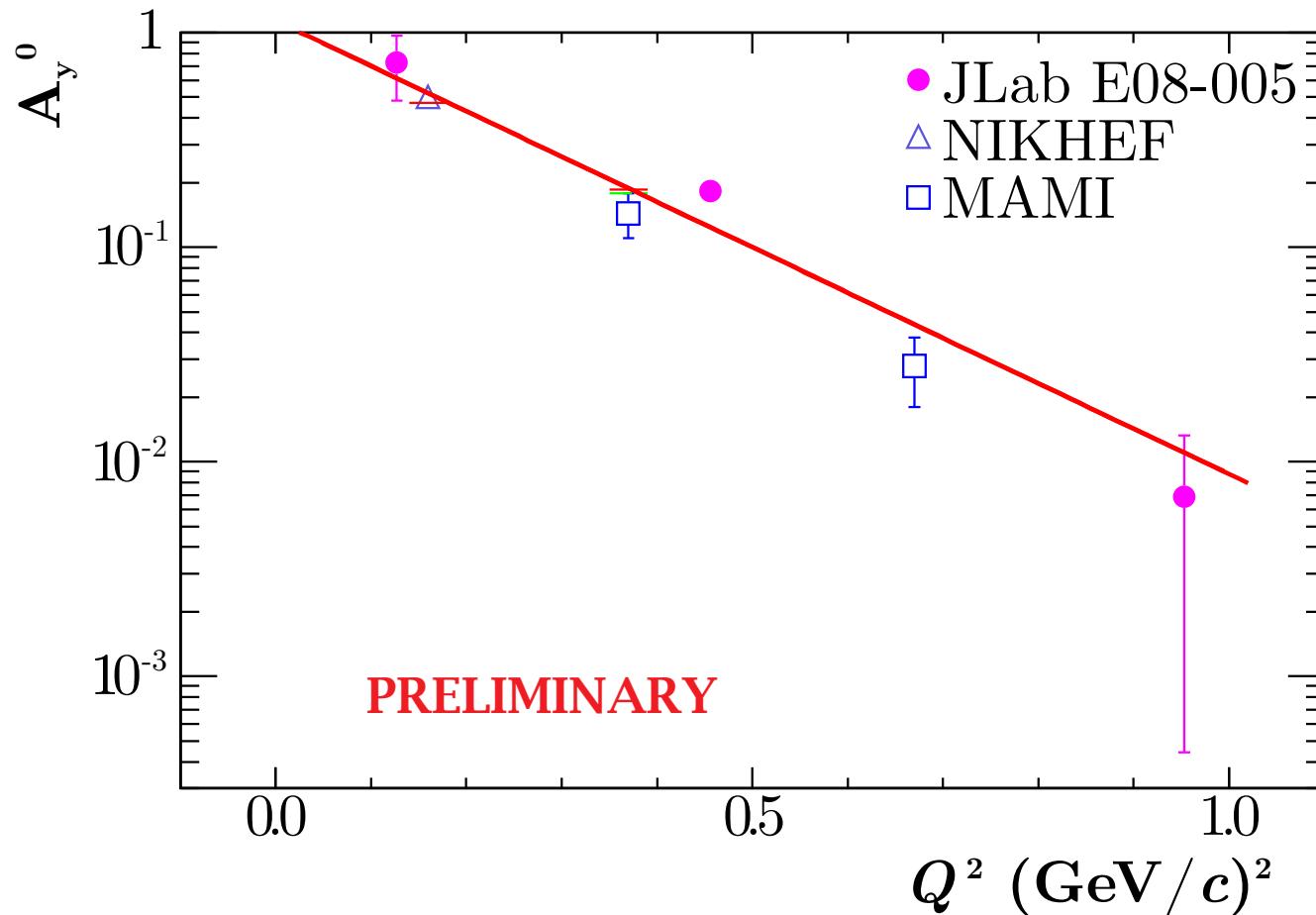
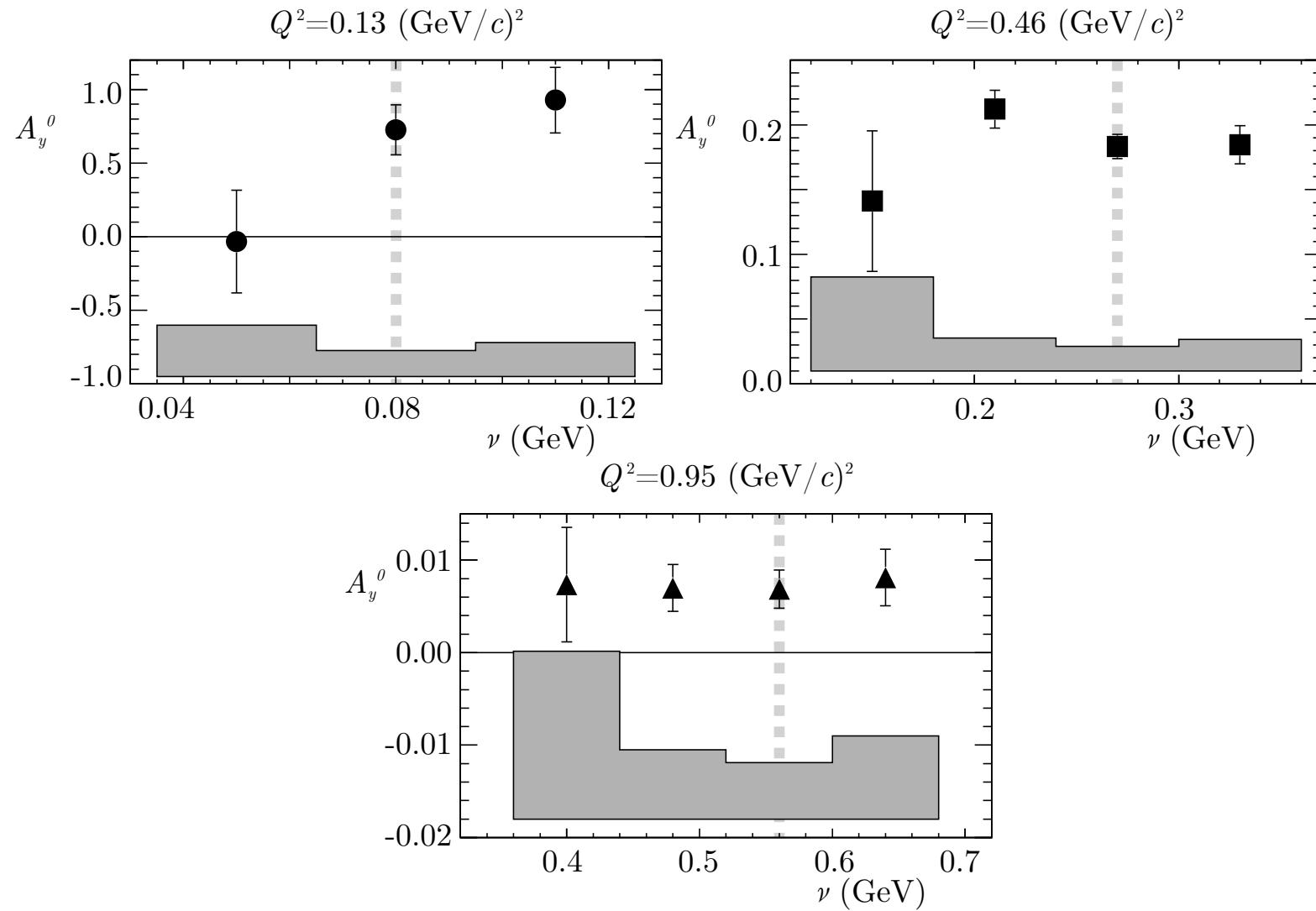


Figure courtesy of Elena Long, UNH

Single-spin asymmetries in QE ${}^3\text{He}^\uparrow(\vec{e}, e'n)$

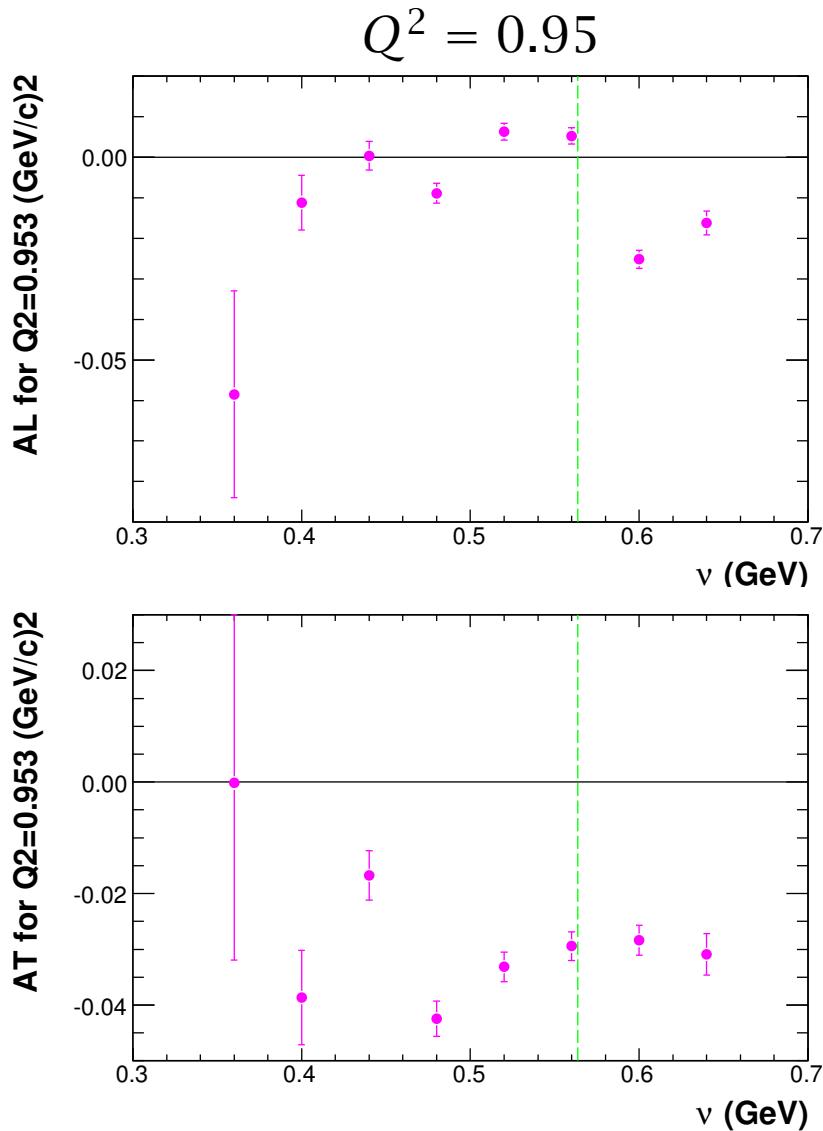
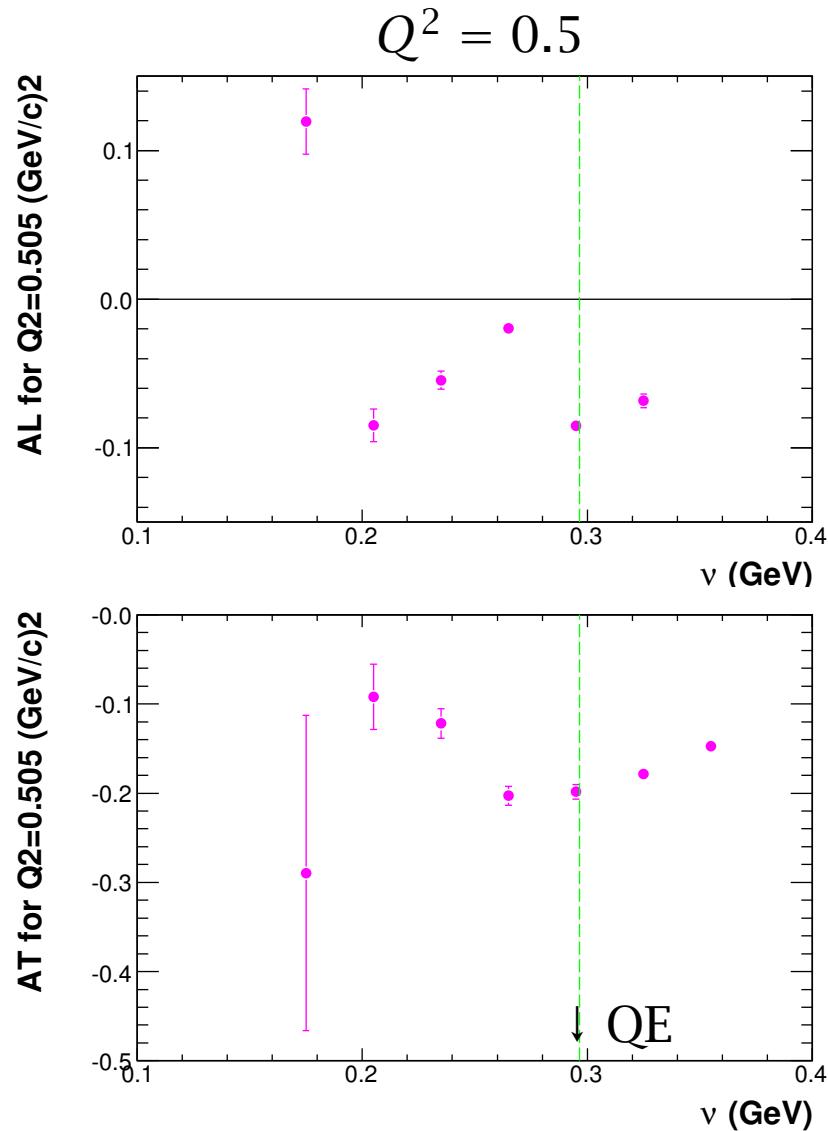
E08-005



PRELIMINARY Figures courtesy of Elena Long, UNH

Double-spin asymmetries in QE ${}^3\vec{\text{He}}(\vec{e}, e'n)$

E08-005



*** VERY PRELIMINARY *** Figures courtesy of Elena Long, UNH

Triple-polarized ${}^3\text{He}(\vec{e}, e' \vec{p})$

MAMI/A1

- PWIA: σ_L , σ_T , $\sigma_{T'}$ yield spin-dependent momentum distribution
- FSI, MEC preclude direct access except at $p_d \lesssim 2 \text{ fm}^{-1}$
- rich interplay \triangleright **final-state symmetrization**: large effect in C_3
 - \triangleright **FSI**: largest in C_2
 - \triangleright **MEC**: most prominent in C_1

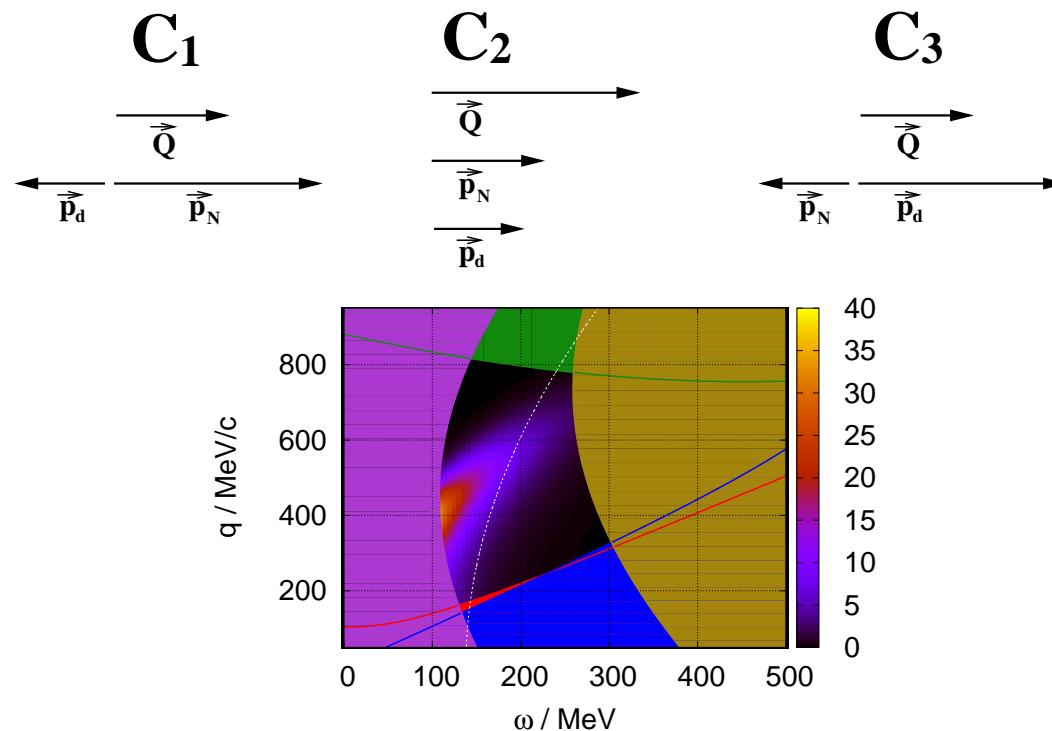


Figure courtesy of Michael Distler, JGU Mainz

Triple-polarized ${}^3\text{He}(\vec{e}, e' \vec{p})$

MAMI/A1

- spin-dependent momentum distributions of $\vec{p}\vec{d}$ clusters in polarized ${}^3\text{He}$
Golak++ PRC **65** (2002) 064004

$$N_\mu = \langle \Psi_{pd}^{(-)} M_d m | \hat{j}_\mu(\vec{q}) | \Psi M \rangle$$

$$\gamma \left(M = \frac{1}{2}, M_d = 0, m = +\frac{1}{2} \right) \propto \left| N_{-1}^{\text{spin PWIA}} \left(\frac{1}{2}, 0, -\frac{1}{2} \right) \right|^2$$

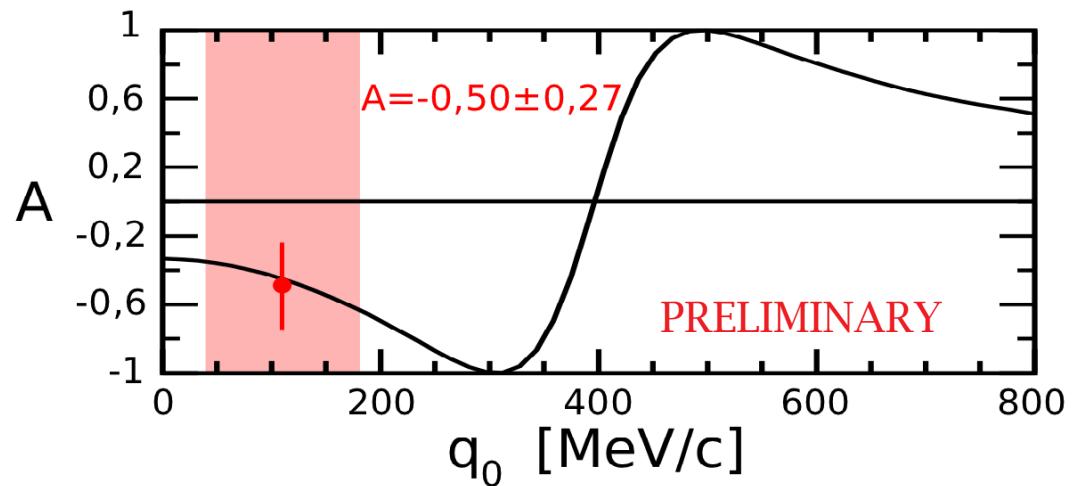
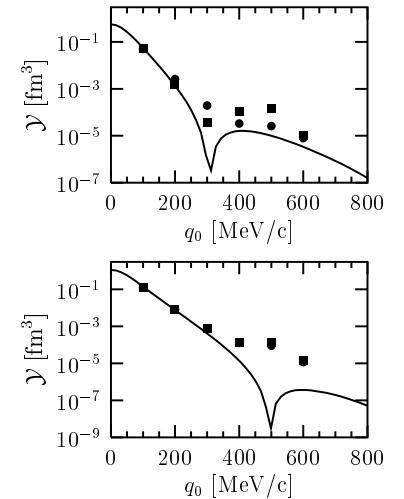
$$\gamma \left(M = \frac{1}{2}, M_d = 1, m = -\frac{1}{2} \right) \propto \left| N_{+1}^{\text{spin PWIA}} \left(\frac{1}{2}, 1, +\frac{1}{2} \right) \right|^2$$

$$A = \frac{\gamma(1/2, 0, 1/2) - \gamma(1/2, 1, -1/2)}{\gamma(1/2, 0, 1/2) + \gamma(1/2, 1, -1/2)}$$

$$\sigma_L \propto |N_0|^2$$

$$\sigma_T \propto |N_{+1}|^2 + |N_{-1}|^2$$

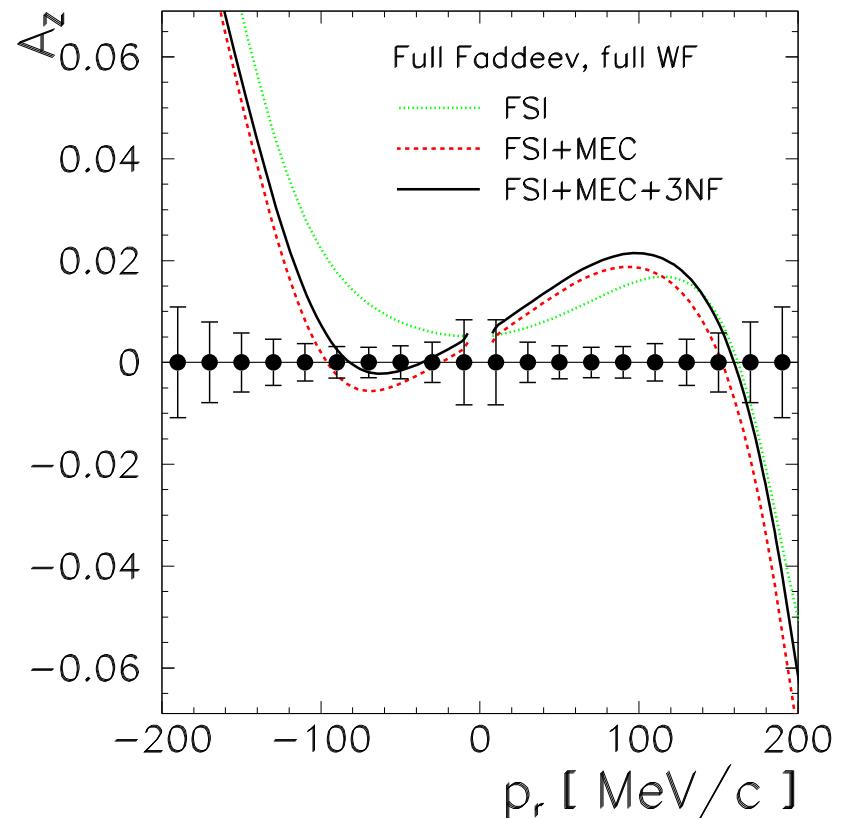
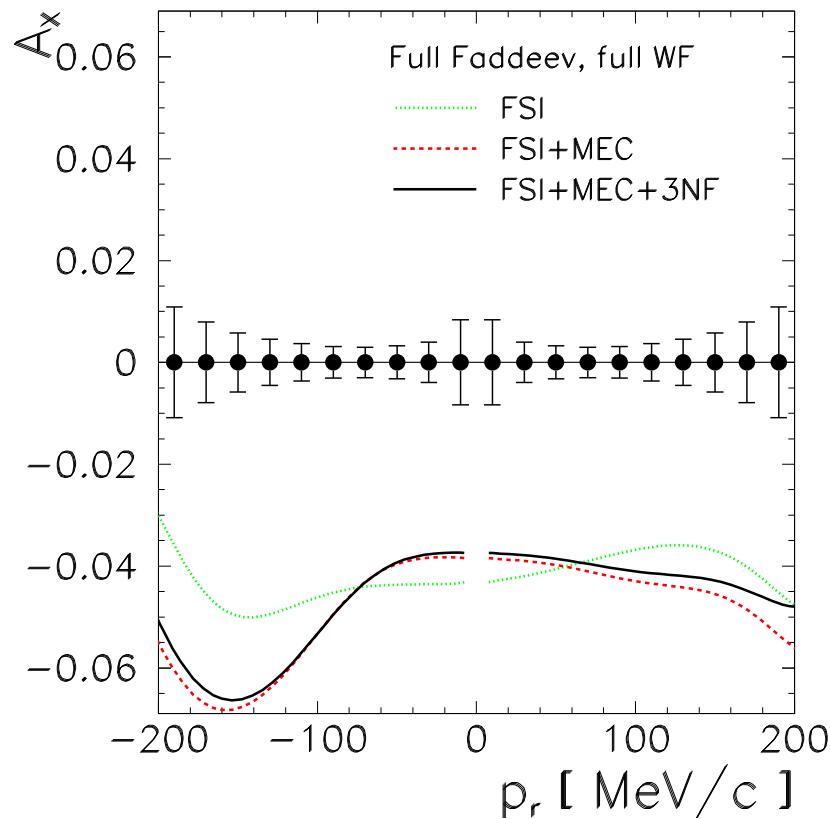
$$\sigma_{T'} \propto |N_{+1}|^2 - |N_{-1}|^2$$



Thank you!

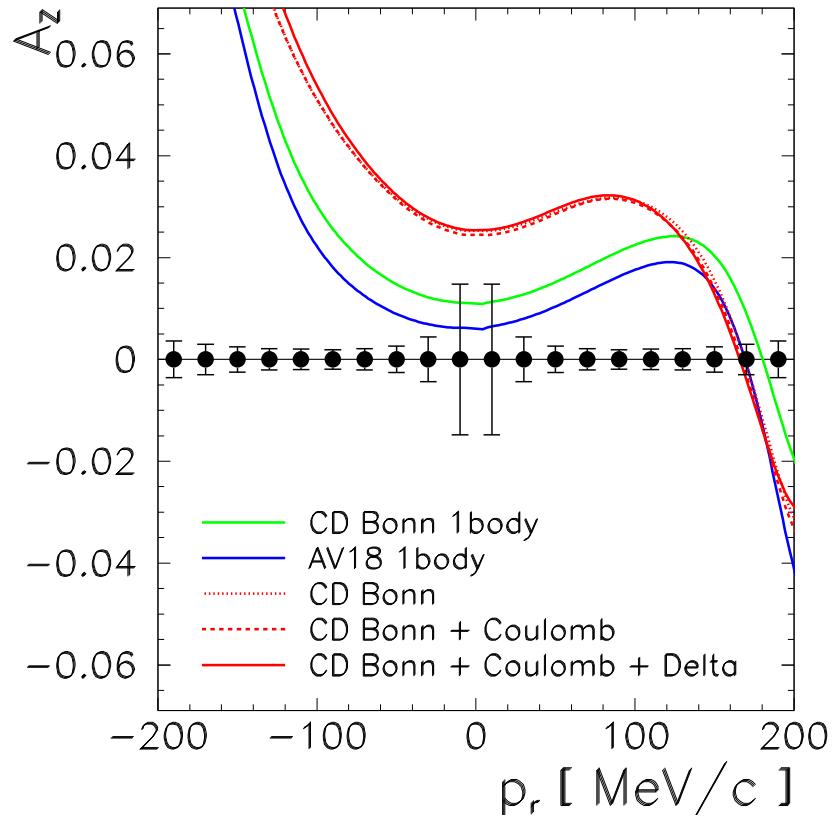
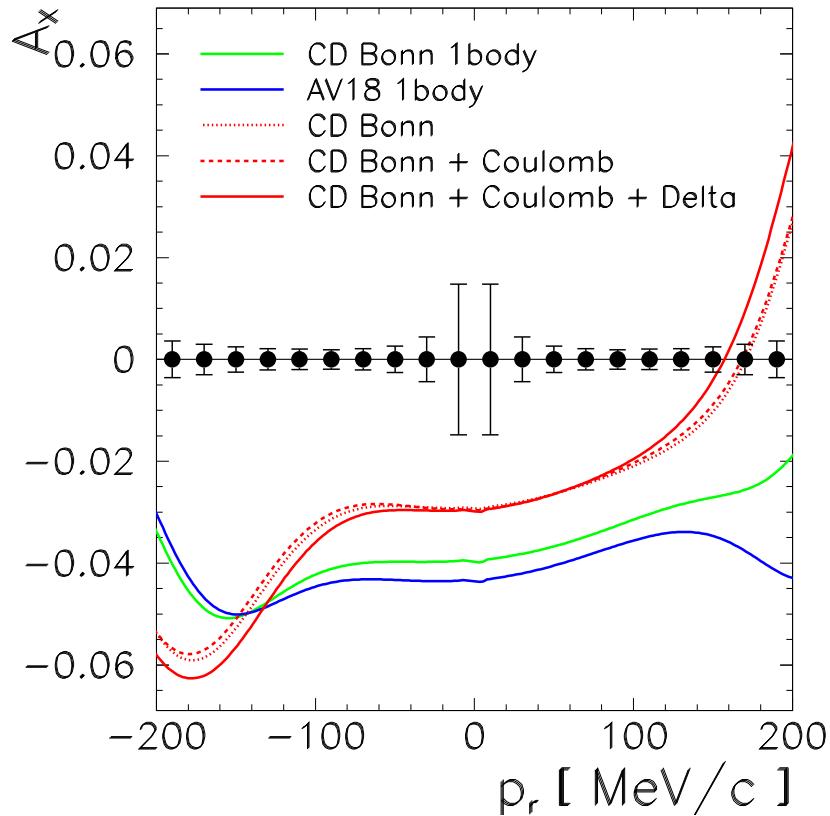
Dynamics ingredients ${}^3\vec{\text{He}}(\vec{e}, e'd)$

KRAKOW/BOCHUM

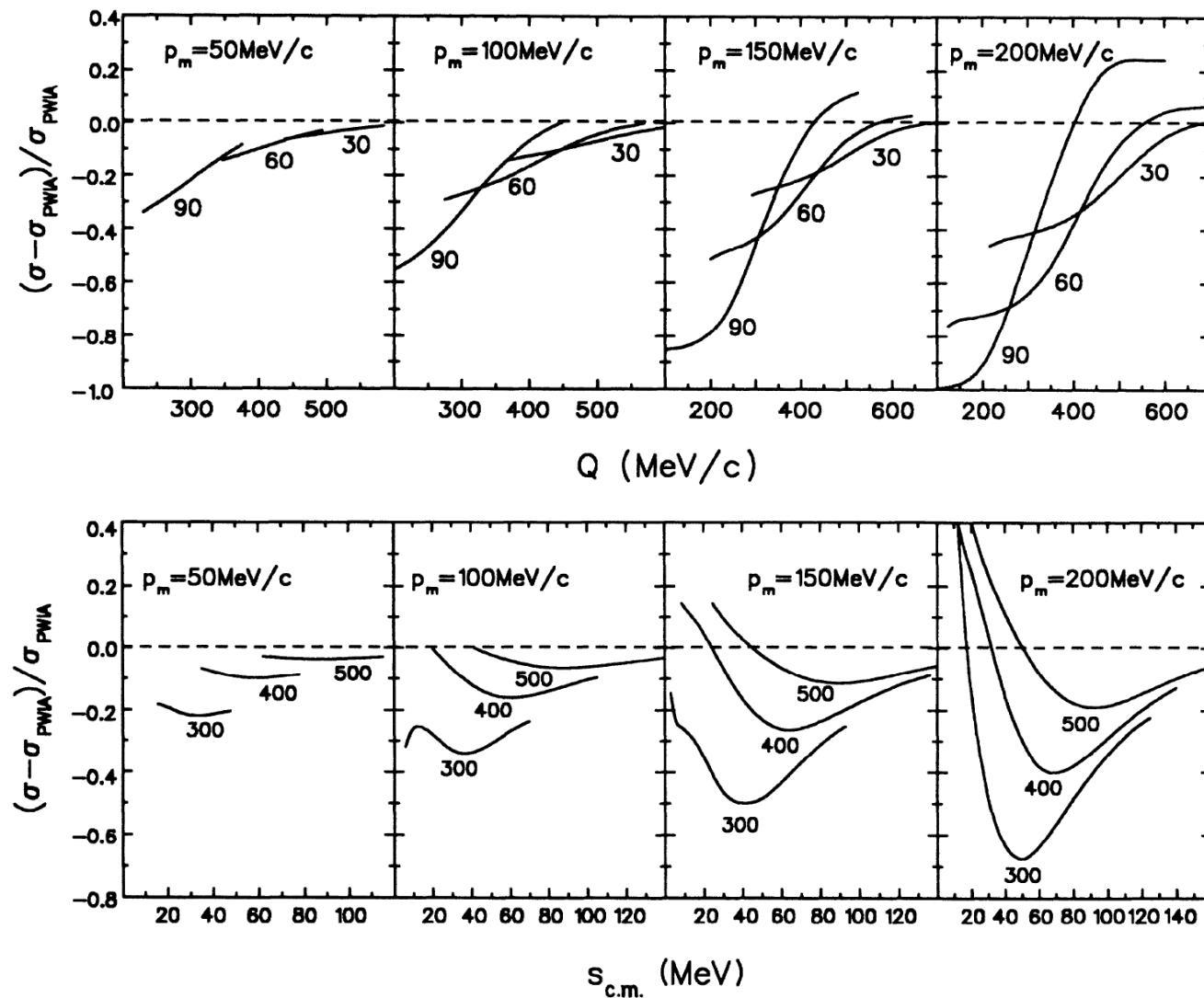


Dynamics ingredients ${}^3\vec{\text{He}}(\vec{e}, e'd)$

HANNOVER/LISBON



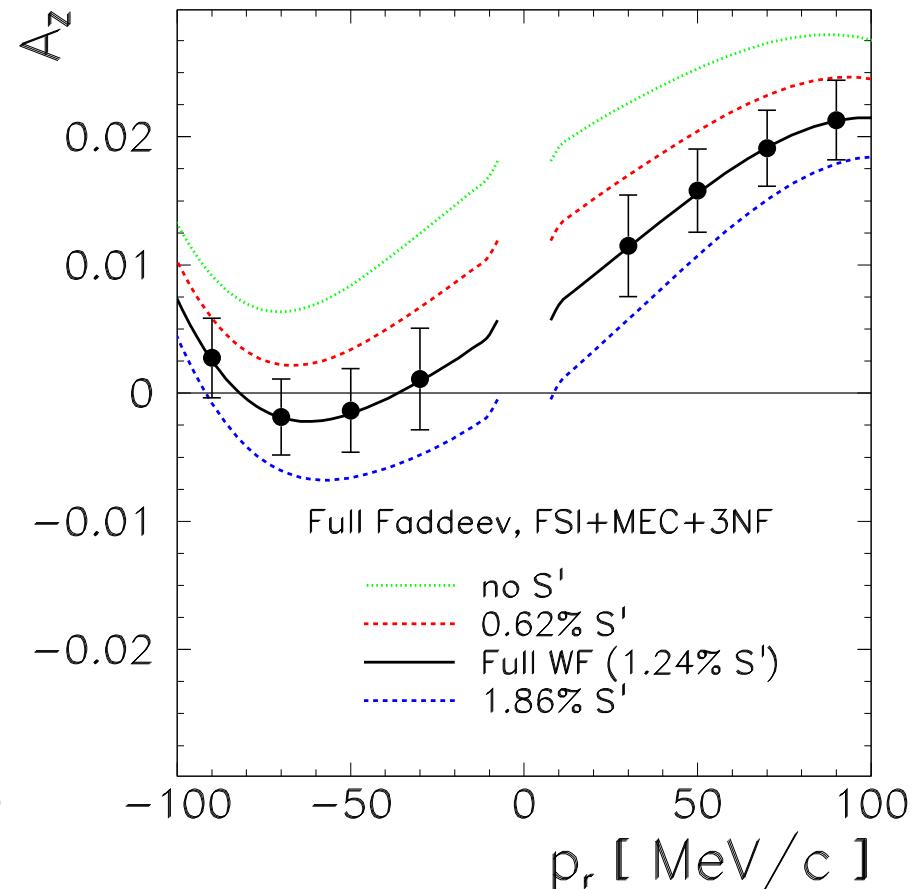
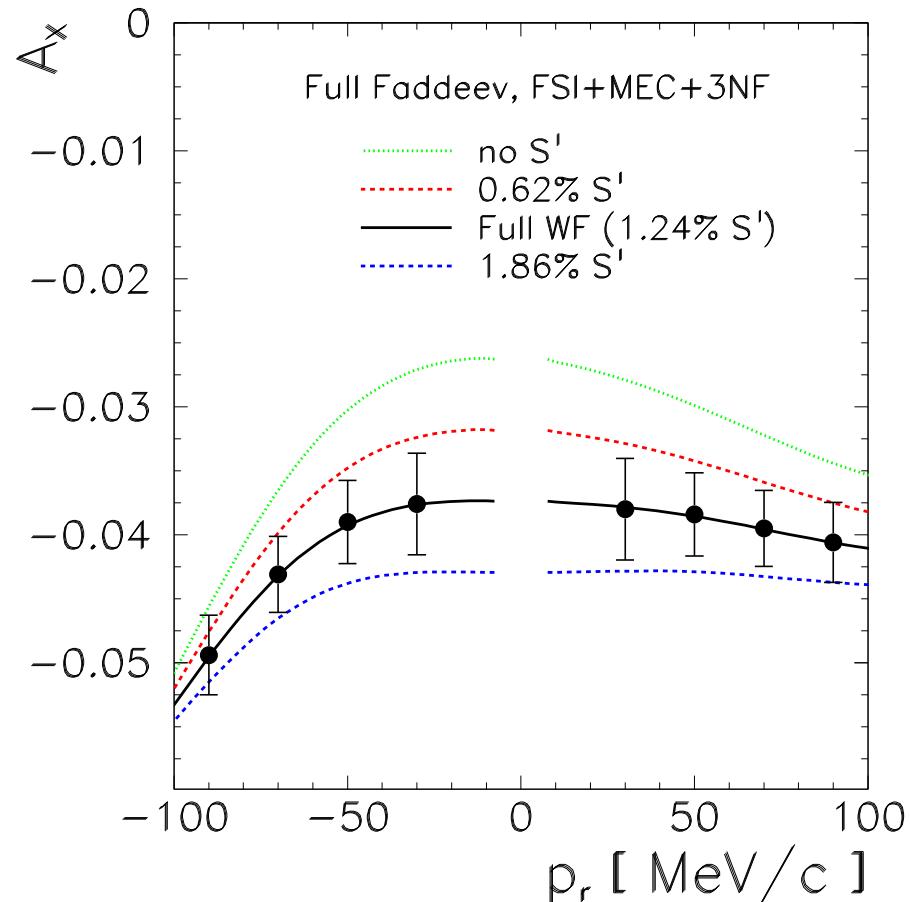
Relative size of FSI effects for ${}^3\text{He}(e, e'd)$



Meijgaard, Tjon PRC **42** (1990) 96

Sensitivity to the S' component

KRAKOW/BOCHUM



Extraction of A_γ^n from $A_\gamma^{{}^3\text{He}}$ — effective polarization approximation:

$$A_\gamma^{{}^3\text{He}} = P_n f_n A_\gamma^n + P_p (1 - f_n) A_\gamma^p$$

$$f_n = \frac{\sigma^n}{\sigma^{{}^3\text{He}}} = \frac{\sigma^n}{2\sigma^p + \sigma^n}$$

$$P_p = 0.86 \pm \dots \quad P_n = -0.028 \pm \dots$$

high Q^2 : f_n computed with Kelly's parameterization of nucleon FFs

low Q^2 : theoretical estimate (due to FSI): $f_n = 0.042$ (A. Deltuva)

A_γ^p computed by Afanasev et al.