

## Segmented Band Mechanism for Itinerant Ferromagnetism

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We introduce a novel mechanism for itinerant ferromagnetism, which is based on a simple two-band model, and, by using numerical and analytical methods, we show that the periodic Anderson model contains this mechanism. We propose that the mechanism, which does not assume an intra-atomic Hund's coupling, is present in both the iron group and some  $f$  electron compounds.

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Even though itinerant ferromagnetism was the first collective electronic phenomena studied quantum mechanically, the microscopic mechanisms driving this phase are still unknown [1,2]. In 1928, Heisenberg [3] formulated his spin model to address this issue, but, as Bloch [4] pointed out, a model of localized spins cannot explain the metallic ferromagnetism observed in Fe, Co, and Ni. After seven decades of intense effort we still do not know what is the minimal model of itinerant ferromagnetism and, more importantly, the basic mechanism of ordering.

In 1963, Hubbard [5] and others introduced the Hubbard model to explain the ferromagnetic (FM) properties of the iron group, incorporating the kinetic energy in a *single nondegenerate band* with an intra-atomic Coulomb repulsion  $U$ . With the exception of Nagaoka's [6] and Lieb's [7] theorems, subsequent theoretical approaches were not controlled enough to determine whether the Hubbard model has a FM phase. The central issue is the precise evaluation of the energy for the paramagnetic (PM) phase. Because it does not properly incorporate the correlations, mean field theory overestimates this energy and predicts a large FM region [1]. In contrast, numerical calculations have narrowed the extent of this phase to a small region around the Nagaoka point [6].

Going beyond the simple one-band Hubbard model is advocated, for example, by Vollhardt *et al.* [1]. They note that the inclusion of additional density-density interactions, correlated hoppings, and direct exchange terms favors FM ordering. A very simple analysis shows that increasing the density of states  $\mathcal{D}(E)$  below the Fermi energy  $E_F$  and placing  $E_F$  close to the lower band edge increases the

FM tendency. One can achieve this by including additional hopping terms. The effectiveness of a next-nearest-neighbor hopping  $t'$  was studied numerically by Hlubina *et al.* [8] for the Hubbard model on a square lattice. They found a FM state when the van Hove singularity in  $\mathcal{D}(E)$  occurred at  $E_F$ . However, this phase was not robust against very small changes in  $t'$ .

Years ago, Slater [9] and van Vleck [10] speculated that band degeneracy is an essential precondition for itinerant ferromagnetism. They suggested that the intra-atomic Hund coupling in open shells could be transmitted from one atom to another by the conduction electrons. However, there are FM metals, such as Ni, where the influence of the Hund's coupling is not clear. In Ni, Hund's coupling is associated with the  $3d^8$  configuration which has low probability because the main configurations are roughly 40% of  $3d^{10}$  and 60% of  $3d^9$  [10]. The relevant question for some transition metals is thus whether a model involving just the two configurations is sufficient, or are other orbitals and Hund's exchange necessary to explain ferromagnetism. Furthermore, there are  $f$  electron itinerant ferromagnets, such as  $\text{CeRh}_3\text{B}_2$  [11], whose only local magnetic coupling is Kondo-like, i.e., antiferromagnetic.

The novel mechanism we now introduce emerges from a two-band model, such as the periodic Anderson model (PAM). The basic ingredient is an uncorrelated dispersive band hybridized with a correlated and a narrow band. Missing is an explicit intra-atomic Hund's exchange. We show that the PAM supports our mechanism by interpreting the results of quantum Monte Carlo (QMC) simulations with an effective model derived from it.

We will discuss our mechanism in the context of

$$H = -t_b \sum_{\langle \mathbf{r}, \mathbf{r}' \rangle, \sigma} (b_{\mathbf{r}\sigma}^\dagger b_{\mathbf{r}'\sigma} + b_{\mathbf{r}'\sigma}^\dagger b_{\mathbf{r}\sigma}) + V \sum_{\mathbf{r}, \sigma} (b_{\mathbf{r}\sigma}^\dagger a_{\mathbf{r}\sigma} + a_{\mathbf{r}\sigma}^\dagger b_{\mathbf{r}\sigma}) \\ - t_a \sum_{\langle \mathbf{r}, \mathbf{r}' \rangle, \sigma} (a_{\mathbf{r}\sigma}^\dagger a_{\mathbf{r}'\sigma} + a_{\mathbf{r}'\sigma}^\dagger a_{\mathbf{r}\sigma}) + \epsilon_a \sum_{\mathbf{r}, \sigma} n_{\mathbf{r}\sigma}^a + \frac{U}{2} \sum_{\mathbf{r}, \sigma} n_{\mathbf{r}\sigma}^a n_{\mathbf{r}\bar{\sigma}}^a,$$

where  $b_{\mathbf{r}\sigma}^\dagger$  and  $a_{\mathbf{r}\sigma}^\dagger$  create an electron with spin  $\sigma$  in  $b$  and  $a$  orbitals at lattice site  $\mathbf{r}$  and  $n_{\mathbf{r}\sigma}^a = a_{\mathbf{r}\sigma}^\dagger a_{\mathbf{r}\sigma}$ . The  $t_b$  and  $t_a$  hoppings are only to nearest-neighbor sites. When  $t_a = 0$ , the Hamiltonian is the standard PAM. For the  $f$

electron compounds, the  $a$  and  $b$  orbitals play the role of the  $f$  and  $d$  orbitals, and  $t_a \approx 0$ . For transition metals, they correspond to the  $3d$  and  $4s$  orbitals. For  $U = 0$ , the resulting Hamiltonian  $H_0$  is easily diagonalized:

$$H_0 = \sum_{\mathbf{k}, \sigma} (E_{\mathbf{k}}^+ \beta_{\mathbf{k}\sigma}^\dagger \beta_{\mathbf{k}\sigma} + E_{\mathbf{k}}^- \alpha_{\mathbf{k}\sigma}^\dagger \alpha_{\mathbf{k}\sigma}) \quad (1)$$

$$E_{\mathbf{k}}^\pm = \frac{1}{2} \left[ e_{\mathbf{k}}^b + e_{\mathbf{k}}^a \pm \sqrt{(e_{\mathbf{k}}^b - e_{\mathbf{k}}^a)^2 + 4V^2} \right],$$

with  $e_{\mathbf{k}}^b = -2t_b \sum_{i=1}^D \cos k_{x_i}$  and  $e_{\mathbf{k}}^a = \epsilon_a - 2t_a \times \sum_{i=1}^D \cos k_{x_i}$  for a hypercubic lattice in dimension  $D$ . The operators which create quasiparticles in the lower and upper bands are

$$\alpha_{\mathbf{k}\sigma}^\dagger = u_{\mathbf{k}} a_{\mathbf{k}\sigma} + v_{\mathbf{k}} b_{\mathbf{k}\sigma}^\dagger, \quad \beta_{\mathbf{k}\sigma}^\dagger = -v_{\mathbf{k}} a_{\mathbf{k}\sigma}^\dagger + u_{\mathbf{k}} b_{\mathbf{k}\sigma}^\dagger$$

$$u_{\mathbf{k}} = \frac{E_{\mathbf{k}}^+ - e_{\mathbf{k}}^a}{\sqrt{(E_{\mathbf{k}}^+ - e_{\mathbf{k}}^a)^2 + V^2}}, \quad v_{\mathbf{k}} = \frac{-V}{\sqrt{(E_{\mathbf{k}}^+ - e_{\mathbf{k}}^a)^2 + V^2}}. \quad (2)$$

In Fig. 1, we illustrate the (one-dimensional) noninteracting bands for the case of interest:  $\epsilon_a$  close to  $E_F$  and above the bottom of the  $b$  band. If  $|V| \ll |t_b|$ , we can identify two subspaces in each band where the states have either predominantly  $b$  ( $\psi$  subspace) or  $a$  ( $\phi$  subspace) character. The size of the crossover region around the points where the original unhybridized  $b$  and  $a$  bands crossed is proportional to  $|V/t_b|$ ; that is, it is very small. The creation operators for the Wannier orbitals  $\psi_{\mathbf{r}\sigma}$  and  $\phi_{\mathbf{r}\sigma}$  associated with each subspace are

$$\psi_{\mathbf{r}\sigma}^\dagger = \frac{1}{\sqrt{N}} \left[ \sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} \beta_{\mathbf{k}\sigma}^\dagger + \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} \alpha_{\mathbf{k}\sigma}^\dagger \right], \quad (3)$$

$$\phi_{\mathbf{r}\sigma}^\dagger = \frac{1}{\sqrt{N}} \left[ \sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} \alpha_{\mathbf{k}\sigma}^\dagger + \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} \beta_{\mathbf{k}\sigma}^\dagger \right].$$

where  $N$  is the number of sites. The subsets  $\mathbf{K}^>$  and  $\mathbf{K}^<$  are defined by  $\mathbf{K}^> = \{\mathbf{k}: |u_{\mathbf{k}}| \geq |v_{\mathbf{k}}|\}$  and  $\mathbf{K}^< = \{\mathbf{k}: |v_{\mathbf{k}}| > |u_{\mathbf{k}}|\}$ . In this new basis,

$$H_0 = H_0^\psi + H_0^\phi$$

$$= \sum_{\mathbf{r}, \mathbf{r}', \sigma} \tau_{\mathbf{r}-\mathbf{r}'}^\phi \phi_{\mathbf{r}\sigma}^\dagger \phi_{\mathbf{r}'\sigma} + \sum_{\mathbf{r}, \mathbf{r}', \sigma} \tau_{\mathbf{r}-\mathbf{r}'}^\psi \psi_{\mathbf{r}\sigma}^\dagger \psi_{\mathbf{r}'\sigma},$$

with  $\tau_{\mathbf{r}}^\phi = \frac{1}{N} [\sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} E_{\mathbf{k}}^- + \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} E_{\mathbf{k}}^+]$  and  $\tau_{\mathbf{r}}^\psi = \frac{1}{N} [\sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} E_{\mathbf{k}}^+ + \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} E_{\mathbf{k}}^-]$ .

Because the  $U$  term in  $H$  involves only the  $a$  orbitals, the matrix elements of  $H$  connecting the  $\phi$  and  $\psi$  subspaces

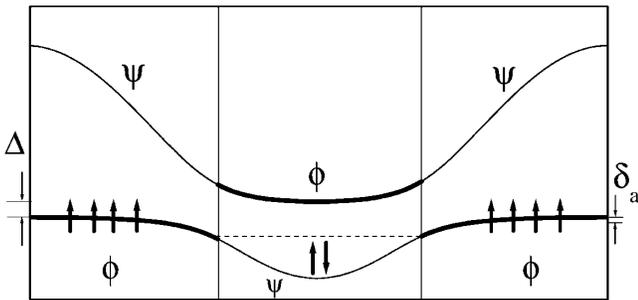


FIG. 1. Illustration of the effective model and the FM mechanism.  $\Delta$  is the hybridization gap and  $\delta_a$  is the interval of energy where the electrons are polarized.

are small compared to the characteristic energy scales of the problem (the matrix elements of  $H$  within the subspaces). To see this we express  $a_{\mathbf{r}\sigma}^\dagger$  as a function of  $\phi_{\mathbf{r}\sigma}^\dagger$  and  $\psi_{\mathbf{r}\sigma}^\dagger$  by first inverting Eqs. (2) and (3) to find

$$a_{\mathbf{r}\sigma}^\dagger = \sum_{\mathbf{r}'} W_{\mathbf{r}-\mathbf{r}'} \phi_{\mathbf{r}'\sigma}^\dagger + w_{\mathbf{r}-\mathbf{r}'} \psi_{\mathbf{r}'\sigma}^\dagger, \quad (4)$$

with  $W_{\mathbf{r}} = \frac{1}{N} [\sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} u_{\mathbf{k}} - \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} v_{\mathbf{k}}]$  and  $w_{\mathbf{r}} = \frac{1}{N} [-\sum_{\mathbf{k} \in \mathbf{K}^>} e^{i\mathbf{k} \cdot \mathbf{r}} v_{\mathbf{k}} + \sum_{\mathbf{k} \in \mathbf{K}^<} e^{i\mathbf{k} \cdot \mathbf{r}} u_{\mathbf{k}}]$ . However, because the  $\phi$  orbitals have predominantly  $a$  character, while the  $\psi$  orbitals have predominantly  $b$  character,  $a_{\mathbf{r}\sigma}^\dagger \approx \sum_{\mathbf{r}'} W_{\mathbf{r}-\mathbf{r}'} \phi_{\mathbf{r}'\sigma}^\dagger$ . If  $|V| \ll |t_b|$ , then  $|w_{\mathbf{r}}| \ll |W_{\mathbf{r}}|$ . Consequently, the  $\phi$  subspace becomes invariant under the application of  $H$ . In addition, because  $|W_0| \gg |W_{\mathbf{r} \neq 0}|$ , we can establish a hierarchy of terms where the lowest order one corresponds to a simple on-site repulsion:

$$H_{\text{eff}}^U = \tilde{U} \sum_{\mathbf{r}} n_{\mathbf{r}\uparrow}^\phi n_{\mathbf{r}\downarrow}^\phi, \quad (5)$$

with  $\tilde{U} = U|W_0|^4$  and  $n_{\mathbf{r}\sigma}^\phi = \phi_{\mathbf{r}\sigma}^\dagger \phi_{\mathbf{r}\sigma}$ . The next order terms, containing three and two  $W_0$  factors, are much smaller and are essentially the same as the intersite interactions which in the past were added to the Hubbard model to enhance the ferromagnetism [1]. Adding  $H_{\text{eff}}^U$  to  $H_0$  we get the effective Hamiltonian

$$H_{\text{eff}} = \sum_{\mathbf{r}, \mathbf{r}', \sigma} (\tau_{\mathbf{r}-\mathbf{r}'}^\psi \psi_{\mathbf{r}\sigma}^\dagger \psi_{\mathbf{r}'\sigma} + \tau_{\mathbf{r}-\mathbf{r}'}^\phi \phi_{\mathbf{r}\sigma}^\dagger \phi_{\mathbf{r}'\sigma})$$

$$+ \tilde{U} \sum_{\mathbf{r}} n_{\mathbf{r}\uparrow}^\phi n_{\mathbf{r}\downarrow}^\phi. \quad (6)$$

The  $\psi$  and  $\phi$  orbitals form uncorrelated and correlated nonhybridized bands:  $H_{\text{eff}} = H^\psi + H^\phi$ . For the  $\phi$  orbitals we obtain an effective one-band Hubbard model with the peculiar double shell-like dispersion relation shown by the thick lines in Fig. 1.

Particularly for  $t_a = 0$ ,  $H^\phi$  has a very large density of states in the lower shell of the  $\phi$  band [1] which is located near  $\epsilon_a$ . From Fig. 1 it is also clear that the electrons first doubly occupy the uncorrelated  $\psi$  band states which are below  $\epsilon_a$ . However, when  $E_F$  gets close to  $\epsilon_a$ , i.e., the system is in the mixed valence regime, the electrons close to the Fermi level go into some of the correlated  $\phi$  states. Then, the interaction term  $H_{\text{eff}}^U$ , combined with the double shell band structure of  $H_0^\phi$ , gives rise to a FM ground state (GS): The electrons close to  $E_F$  spread to higher unoccupied  $\mathbf{k}$  states and polarize, which causes the spatial part of their wave function to become antisymmetric, eliminating double occupancy in real space and reducing the Coulomb repulsion to zero. The cost of polarizing is just an increase in the kinetic energy proportional to  $\delta_a \sim \hbar v_F \delta_k$ , where  $v_F$  is the Fermi velocity and  $\delta_k$  is the interval in  $\mathbf{k}$  space in which the electrons are polarized.

To determine the stability of this unsaturated FM state, we compare its energy with that of the PM (nonmagnetic) state. If we were to build a nonmagnetic state with only the states of the lower  $\phi$  shell, we would find a restricted delocalization for each electron because of the exclusion

of the finite set of band states ( $\mathbf{k}$  states) in the upper shell. To avoid the Coulomb repulsion  $U$  for double occupying a given site, the electrons need to occupy all  $\mathbf{k}$  states. This means they have to occupy the  $\phi$  states in the upper and lower shells. This restricted delocalization is a direct consequence of Heisenberg's uncertainty principle, and the resulting localization length depends on the wave vectors, where the original  $b$  and  $a$  bands crossed, that define the size ( $\Delta\mathbf{k}$ ) of each shell. The energy cost for occupying the  $\phi$  states in the upper shell is proportional to the hybridization gap  $\Delta$ . Therefore if  $U$  is the dominant energy scale in the problem and  $\Delta \gg \delta_a$ , the FM state lies lower in energy than the nonmagnetic state. Under these conditions, the effective FM interaction is proportional to the hybridization gap  $\Delta$ .

This mechanism for ferromagnetism on a lattice is analogous to intra-atomic Hund's mechanism polarizing electrons in atoms. In atoms, we also have different degenerate (the equivalent of  $\delta_a$  is zero) shells separated by an energy gap. If the valence shell is open, the electrons polarize to avoid the short range part of the Coulomb repulsion (again reflecting the Pauli exclusion principle). The energy of an eventual nonmagnetic state is proportional either to the magnitude of the Coulomb repulsion or to the energy gap between different shells. The interplay between both energies sets the scale of Hund's intra-atomic exchange coupling.

The FM mechanism just described applies to any finite dimension. For a chain of 16 sites we calculated, by the Lanczos method, the exact GS of  $H_{\text{eff}}$  for  $\epsilon_a = -t_b$ , infinite  $\tilde{U}$  ( $\tilde{U} \gg |\tau_r^\phi|$ ), and different values of  $V$  as a function of electron concentration  $n = N_e/4N$ . We found that the GS is a nonsaturated ferromagnet between  $n = 1/4$  (one electron per site in the PAM) and  $n = 3/8$ . In the local momentum regime, QMC [12] and density matrix renormalization group [13] calculations report a FM phase in a very similar range of  $n$ , in contrast to the much broader range found by dynamical mean field theory calculations [14]. The largest magnetization  $M$  is obtained when  $n$  is such that the lower shell of the  $\phi$  band is completely filled and the upper one is nearly empty, i.e., when  $E_F \approx \epsilon_a$ .

In Fig. 2a we plot the PAM's energy per site  $E/N$ , computed by our QMC method [12], as a function of the total spin per site  $S/N$  for chains of varying length  $N$  and fixed electron density  $n$  [15]. Over these chain lengths the data collapse, with  $E(S)/N$  showing the minimum  $E_{\text{GS}}/N$  at a nonzero value of  $S/N$  that represents a very good estimate of the magnetization  $M/N$  for the PAM in the thermodynamic limit (TL). In Figs. 2b and 2c, we show  $\Delta E/N \equiv [E_{\text{GS}} - E(S=0)]/N$  and  $M/N$  for one- and two-dimensional systems as a function of  $1/N$ . In both cases  $M/N$  smoothly varies to nonzero values in the TL. The nonsmooth variation of  $\Delta E/N$  in two dimensions is a consequence of shell effects still present in a finite sized system, but is clearly suggestive of its likely extrapolation to a non-negative value for very large  $N$ . In Fig. 2d we plot our QMC results for  $[E(\text{FM}) - E(0)]/E(0)$  as a function

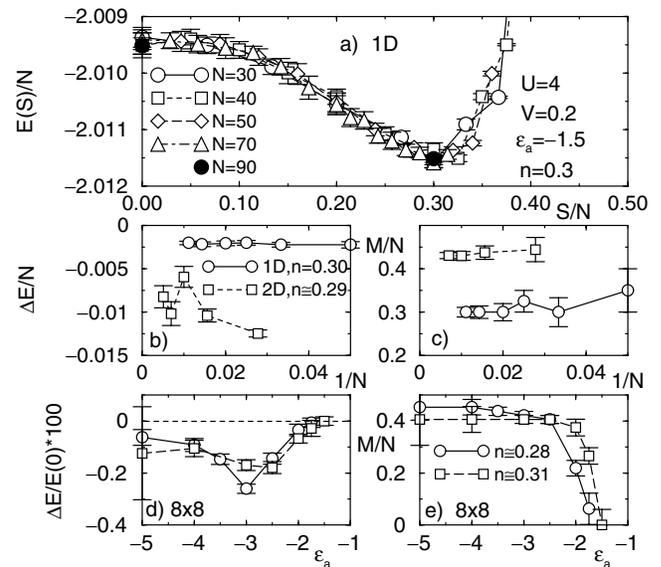


FIG. 2. (a) Energy of the PAM as a function of total spin for different chain lengths. (b) Scaling of the energy difference between the FM and the PM GS's of the PAM in 1D (same parameters as in (a) and 2D ( $V = 0.5$ ,  $\epsilon_a = -0.3$ , and  $U = 4$ ). (c) Scaling of the GS magnetization, otherwise the same as (b). (d) Relative energy difference  $\Delta E/E(0)$  vs  $\epsilon_a$  for  $V = 0.5t_b$ ,  $t_a = 0$  and  $V = 0.5$ ,  $U = 4$ , and  $n = 0.29$  (circles),  $n = 0.31$  (squares). (e) Magnetization as a function of  $\epsilon_a$  for 2D, otherwise the same as (d).

of  $\epsilon_f$  for an  $8 \times 8$  cluster and two different electron densities. As we increase  $\epsilon_a$  (starting from below the bottom of the  $b$  band),  $\Delta E$  decreases and then increases. The most stable FM state occurs when  $E_F \approx \epsilon_a$ , as expected from our discussion of the effective model. Increasing  $\epsilon_a$  even further,  $\Delta E$  approaches zero indicating that the spin of the GS decreases (see Fig. 2e) and the system becomes a paramagnet.

By changing  $\epsilon_a$  we can evolve the system from the localized ( $\epsilon_a \ll E_F$ ) to the itinerant case ( $\epsilon_a \approx E_F$ ). From Figs. 2d and 2e we see that the itinerant and localized FM phases are apparently continuously connected. With decreasing  $\epsilon_a$ ,  $|\Delta E|$  decreases while the zero temperature magnetization  $M$  increases. The strong reduction of  $|\Delta E|$  is a result of the very small effective magnetic interaction in the localized limit ( $J_{\text{RKKY}}$  is order  $V^4$  [16]). Decreasing  $\epsilon_a$  increases the population of the lower  $\phi$  shell. Since most of the electrons in the lower  $\phi$  shell are polarized when  $\epsilon_a \leq E_F$ , this leads to an increase of  $M$ . These results are consistent with the observed behavior of  $M$  and the Curie temperature  $T_c$  in  $\text{La}_x\text{Ce}_{1-x}\text{Rh}_3\text{B}_2$  as a function of  $x$  [17].

Even though we cannot do finite temperature calculations with our present version of the QMC method, we can discuss, at least qualitatively, the predictions of our mechanism for finite temperatures. If we move  $\epsilon_a$  above  $E_F$ , the number of  $a$  electrons decreases together with the magnetization  $M$ . A new energy scale  $\epsilon_a - E_F$  emerges. We propose that this scale is responsible for the finite temperature peak in the magnetization of  $\text{Ce}(\text{Rh}_{1-x}\text{Ru}_x)_3\text{B}_2$  [18] that suggests an ordered state with high entropy. At  $T = 0$ ,

$M$  is small because of the reduced number of  $a$  electrons. When the temperature is of the order of  $\epsilon_a - E_F$ , electrons are promoted from the doubly occupied  $b$  states to the unoccupied  $a$  states which have a large entropy (large density of states). These  $a$  electrons polarize because of the energy considerations discussed above. The source of the large entropy is thus associated with charge and not with spin degrees of freedom, which explains why a state with larger  $M$  has a higher entropy. From this analysis we predict that the entropy below  $T_c$  contains a considerable contribution from the *charge* degrees of freedom.

We can also connect our mechanism with the hydrostatic pressure dependence of  $T_c$ . To do this we calculated  $|\Delta E|/N$  by the QMC method as a function of increasing  $t_b$  (Fig. 3a). Here we assume that the main effect of the hydrostatic pressure is to increase  $t_b$  and to leave the other parameters unchanged. The order of magnitude of  $|\Delta E|/N$ , which should be proportional to  $T_c$ , and its qualitative behavior in Fig. 3a are in good agreement with the experimental results in  $\text{CeRh}_3\text{B}_2$  [11]. We see from Fig. 3a that, for the itinerant FM case,  $|\Delta E|/N$  is of the order of 100 K. This scale is much larger than the typical magnitude of the RKKY interaction [19] ( $\sim 1$  K for  $\text{CeRh}_3\text{B}_2$ ) which is commonly used to explain the origin of the magnetic phase when the  $a$  electrons are localized. We also find that the FM state appears close to quarter filling and disappears for  $n$  close to  $3/8$ .

We used a nonzero  $t_a$  to study the stability of the FM phase when  $\delta_a$  is varied. This study is also important because, in contrast to  $f$  electron compounds, in the FM transition metals both bands are dispersive. In Fig. 3b we see that the FM phase is even more stable for  $t_a \sim -0.1t_b$  than for  $t_a = 0$  and becomes unstable for  $t_a \sim 0.05t_b$ . The reason for this asymmetric behavior is easy to understand in terms of the variation of  $\delta_a$ : If  $t_a$  is negative, then the effect of  $t_a$  on the dispersion of the  $\phi$  band is opposite to that of the hybridization  $V$ . When  $t_a \sim -0.1t_b$  we get, for the given  $\epsilon_a$  and  $V$ , the minimum value

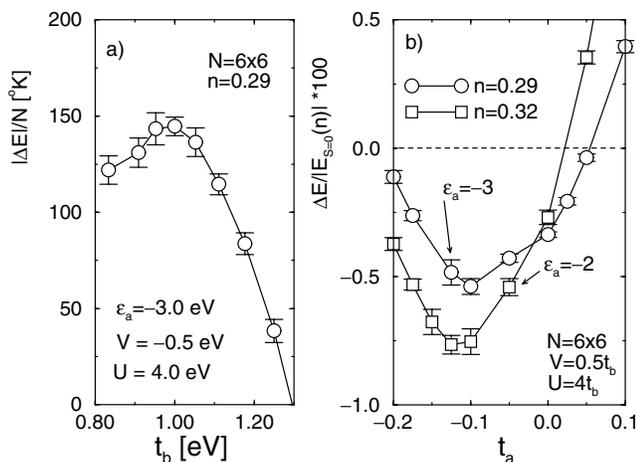


FIG. 3. (a) Energy difference per site between the FM and PM states as a function of  $t_b$ . (b) Influence of the hopping  $t_a$  on the FM state. The lattice size is in unit cells.

for  $\delta_a$  and therefore the most stable FM case. When we depart from this value of  $t_a$ ,  $\delta_a$  increases,  $|\Delta E|$  decreases, and the FM state becomes less stable.

In summary, we introduced a novel mechanism for itinerant ferromagnetism which is present in a simple two-band model. The picture just presented, combined with our previous results [16], allows a reconciliation of the localized and delocalized ferromagnetism pictures painted by Heisenberg [3] and Bloch [4]. The hybridization between bands plays a crucial role. We have also considered the case relevant for the iron group, where the dispersion of the lower band is not negligible. The fact that the ferromagnetism is even more stable for finite values of  $t_a$  indicates that our mechanism is relevant to explain the ferromagnetism of the transition metals, such as Ni, where a correlated and narrow  $3d$  band is hybridized with the  $4s$  band. It suggests that the ferromagnetism in the transition metals can originate, at least in part, in the interplay between the correlations and the particular band structure, and not solely in the intra-atomic Hund's exchange [10]. In addition, our results explain several qualitative features observed in the ferromagnet  $\text{CeRh}_3\text{B}_2$  [11,17,18]. Elsewhere we will discuss the relation of our mechanism to  $\text{Re}(\text{Co}_{1-x}\text{Si}_x)_2$  ( $\text{Re} = \text{Ho}, \text{Er}$ ) and the uranium monochalcogenides (US, USe, and UTe) which are ferromagnets [20].

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