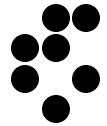


Institut „Jožef Stefan”, Ljubljana, Slovenija



IJS delovno poročilo
DP-8100

CFHHM CODE PARALLELIZATION ON SMP MACHINES 1995-1999

R. Krivec
Department of Theoretical Physics

CFHHM CODE PARALLELIZATION ON SMP MACHINES 1995-1999

R. Krivec,
Department of Theoretical Physics,
J. Stefan Institute,
POB 3000, 1000 Ljubljana, Slovenia

99/08/02

ABSTRACT

Parallelization of a high-precision physics code for solving coupled systems of differential equations with piecewise matrix expansions is presented. The transition from vector-type code to parallel code is accomplished by partially inverting a loop nest. The implementation is by compiler directives on an SMP machine. Because of piecewise algorithm, the parallel code is slower than vector code on a single thread, but overtakes it with more than 4 processors used. The presented example is extremely elegant because only a small piece of code is changed, and no redundant calculations are introduced.

SUMMARY

This report presents a case of code parallelization using mathematical insight rather than MPI or redundant distributed calculations, originally performed in 1995. The starting point is code with vector and superscalar efficiency in single-threaded mode of up to 80%.

The presented measurements are for the He atom ground state (the simplest CFHHM example), in which matrix operations use up to 70% of CPU time. Because of matrix recursion formulas, single matrix operations cannot be efficiently parallelized.

Part I of the report presents a description of CFHHM. Part II reports the parallelization done in 1998 on a SGI Power Challenge. Part III reports the first parallelization done in 1995 on a SPP-1000. The basic code rewriting was done in 1995 for the SPP-1000. However, this machine had its problems, so the relevant results are the Power Challenge ones. The basic trend is the same in both cases.

The result is that on a single processor, the modified and parallelized code runs 2-3 times slower than the original code. To reach the same speed, 4 processors are necessary.

The main reason that the parallelized code runs 2-3 times slower in single-threaded mode is not redundant calculations, but the fact that in the calculations the recursion process must be repeated on many subintervals, between which some matrices must be rejoined and inverted. If only one such interval could be used, parallelization would be almost perfect.

FILES

The information in this report is extracted from the following files:
sgi98_cfhhm_mp_preliminary.txt, bench_bm_cfhh1.txt, cfhhoptsppt.txt.

PURPOSE

- (1) To convert a program with predominantly matrix operations, and optimized for vector and superscalar machines, to parallel using coarse-grained parallelization obtained with explicit code rearrangement, based on mathematical insight, possibly without introducing repetition of intermediate calculations.
- (2) Find the most suitable program loop topology on different machines, and possibly a topology efficient on several machines.

PART I

DESCRIPTION

CFHHM (Correlation Function Hyperspherical Harmonic Method) originated and developed by V.B. Mandelzweig (Hebrew University, Jerusalem), M.I. Haftel (Naval Research Laboratory, Washington) and R. Krivec (J. Stefan Institute, Ljubljana) is a method to calculate very precise values of observables in the quantum nonrelativistic three body problem, especially in atomic physics.

Selected results:

- The best value of annihilation rate of positronium negative ion [1]
- Sticking probability and fusion rate for the muon-deuteron-triton mesomolecule in the muon-catalyzed fusion process; the results pointed out several inconsistencies in the literature [2]
- Resonances in the doubly excited He atom [3], showing that in CFHHM, in contrast to the variational calculations, no stabilization is needed [3]
- The best calculation of hyperfine splitting in the muonic Helium atom, and discovery of wrong convergence of variational calculations [4,5,6]

The main programs in CFHHM are M2MK and EWF2P. M2MK calculates matrix elements and EWF2P solves a system of coupled ordinary differential equations in one variable (hyperradius), which represent the three-body Schroedinger equation. At the origin, the exact analytic form including logarithmic terms is represented as matrix recursion relations. On the rest of the interval, the solution is expressed as matrix Taylor series on small subintervals, calculated via matrix recursion relations, and joined at the boundaries [7].

M2MK

Calculates matrix elements (runs once, has negligible CPU time in the complete CFHHM calculation).
m2mk is a mixed integer/REAL*8 program, written for clarity, and not optimized. MFLOPS is meaningless for it. Its speed is presented as an example of how catastrophically low efficiency such "nice" programs can have, especially on superscalar machines.

Dimension declarations:

NDMU = 33, NDP0 = 104, NDP = 102,
NDGO = 32, NNQSI = 8.

Km = 2*MUU (input), where Km is the maximum global angular momentum.

This program is not parallelized.

EWF2P

Solves the coupled system of differential equations in one variable [7] by prescribing the energy E, propagating the solution from two sides towards a matching hyperradius (ZMATCH), calculating a "joining determinant" D(E), and iterating E until D(E) = 0. Typically 7 iterations with fixed values of E are necessary to find the zero to more than 10 significant digits, which assures the wave function accuracy of at least 6-7 significant digits.

The CPU times quoted are for one iteration (complete integration with fixed energy parameter).

ewf2p is a "vector" floating-point (REAL*8) program.

Dimension declarations:

NDMU variable, ISYM = 0, NDP = 102, NDP0 = 104, NDCN = 22 (size is 790 MB at NDMU = 33).

NSU is the number of coupled equations (matrix size) in the recursive calculation of a matrix Taylor expansion of the solution on sub-intervals.

NDMU is the main dimension and is varied to see its effect at small NSU.

The relations are $NDMU \geq Km / 2$, $NSU = const * Km^{**2}$.

CPU time model:

in the first approximation we count only the main part of RRP* (recursion relations, see below):

$$T = C(IPWUU) * NSU^{**3} * Nint * (JMAX^{**2})/2 + T0$$

where C is a constant, NSU is the number of coupled equations, Nint is the number of hyperradial intervals, JMAX is the number of powers in the matrix Taylor expansion of the solution, and T0 is the time spent on the first interval (small for He atom). C depends on IPWUU because the power expansion of the effective potential introduces additional summations whose CPU time is proportional to $NSU^{**2} * IPWUU * JMAX$, and changes the geometry of the most important loops.

Nint can be approximated as follows. Interval boundaries are determined by $Z(n) = \min((1 + TOL)^{**n} * ZMATCH, DZU)$, whence we get that the lengths $Z(n+1) - Z(n)$ increase up to $Z(n1) = DZU / TOL$, and $n1 = (1 / TOL) * \ln [DZU / (TOL * ZMATCH)]$. Then if $Z(n1) < ZTOP$, $Nint = n1 + (ZTOP - Z(n1)) / DZU$. The actual Nint values were calculated by a trivial program (aux700.f), because the CFHMM program does not enumerate them.

Recursion formulas evaluation:

ewf2p subroutine ddca calls several variants of rrp* subroutines which evaluate the recursion formulas with different loop topologies, and with and without calls to DAXPY and DGEMM. Some rrp* routines are also completely reordered for parallelization. The list of the most important versions is as follows (index M1 =< JMAX runs over Taylor terms in the solution, index IPX =< IPWUU runs over powers in the effective potential):

Name	Originating rrpsm version	IRRPV (ddca)	Short description
rrp11	1.1	1	Single M1 loop outside, IPX inside
rrp30	3.0	30	as rrp11, eliminated power evaluation
rrp30a	3.0V	301	as rrp30, but calls DGEMM
rrp30b	3.0V1	302	as rrp30a, but calls DAXPY
rrp31c	3.1.1V1	314	M1 loop distributed and moved inside
rrp31e		316	as rrp31c, but DO-loops only

References

- [1] R. Krivec and V.B. Mandelzweig, Phys. Rev. A47, 911 (1993).
- [2] R. Krivec and V.B. Mandelzweig, Phys. Rev. A52, 221 (1995).
- [3] S. Berkovic, R. Krivec, V.B. Mandelzweig and L. Stotland, Phys. Rev. A55, 988 (1997).
- [4] R. Krivec and V.B. Mandelzweig, Phys. Rev. A56, 3614 (1997).
- [5] R. Krivec and V.B. Mandelzweig, Phys. Rev. A57, 4976 (1998).
- [6] R. Krivec and V.B. Mandelzweig, Proc. XVI-th European Few-Body Conference, Autrans, June 1-6, 1998.
- [7] R. Krivec, M.I. Haftel and V.B. Mandelzweig, Journal of Computational Physics 123, 149 (1996).

PART II
CFHHM CODE PARALLELIZATION
SGI POWER CHALLENGE
98/11/19

For this work the starting point are the routine versions written in 1995 (Part III).

PROBLEM

CFHHM He atom ground state energy search. We solve a NxN coupled system of ordinary differential equations in one variable on about 100 intervals of the variable. On each interval, the system is propagated by expanding the solution in matrix Taylor series. This results in matrix recurrence formulas in which the column index (I) is memory-contiguous, and columns of the solution matrix are independent.

As explained below, most of the CPU time is consumed using linear algebra either by DO loops or by Blas routines. Therefore the speed as measured by the total program CPU time is a good measure of the level of optimization of the central part of the code.

PROGRAM STRUCTURE

EWf2P calls DDCA which in turn calls RRP* where recursion formulas are evaluated. There are two basic possibilities: RRP31C and RRP41C. (Other possibilities are less optimized single-threaded versions.)

RRP31C calculates recursions by having the index I in several innermost loops (vector style). The central part of the program is as follows:

```

DO 100 N1 = 3,JMAX1
C   RESET CNT (CNT(...,1), CNT(...,2) ARE INPUT PARAMETERS).
DO 62 J = 1,MM
    DO 60 I = 1,MM
        CNT(I,J,N1) = ZERO
60    CONTINUE
62    CONTINUE
    JP = N1 - 1
C   SUM OVER R (R = -1,..., JP-2).
    IF (IRTC0 .EQ. 0) THEN
C   FIRST LOOP: EXCLUDE CNT(...,1). THIS ASSUMES THAT RT
C   WAS CALCULATED ON THE PREVIOUS INTERVAL,
C   AND THAT CNT(...,1) = I.
        JP1 = JP - 1
    ELSE
C   FIRST LOOP: DO NOT EXCLUDE CNT(...,1) (DO ALL).
        JP1 = JP
    ENDIF
DO 74 M1 = 1,JP1
    JR = M1 - 2
    ZZZ72 = JP - JR - 2
    DO 72 K = 1,MM
        DO 70 J = 1,MM
            RR(J,K) = ZZZ72 * PP(J,K,M1) + QQ(J,K,M1)
70    CONTINUE
72    CONTINUE
        CALL DGEMM('N', 'T', MM, MM, MM,
&                ONE, CNT(1,1,N1-JR-2), NCDS,
&                RR, NCDS,
&                ONE, CNT(1,1,N1), NCDS)
74    CONTINUE
    IF (IRTC0 .EQ. 0) THEN
C   SECOND LOOP: CNT(1) = I (IMPLICIT). SEE ABOVE.
        M1 = JP
        DO 82 J = 1,MM
            DO 80 I = 1,MM
                CNT(I,J,N1) = CNT(I,J,N1) + QQ(J,I,M1)
80    CONTINUE
82    CONTINUE
    ENDIF
C   FINISH C(JP) .
DO 92 J = 1,MM
    DO 90 I = 1,MM
        CNT(I,J,N1) = ZZZ71 * CNT(I,J,N1)
90    CONTINUE
92    CONTINUE
100 CONTINUE

```

RRP41C calculates recursions by having the index I in a single outermost loop, to exploit independence of matrix columns for the parallelization of the code. RRP41C is executed once per interval, therefore threads are generated and rejoined on each interval. The inner loops are

```

C$DOACROSS LOCAL(CNTX, CNTY, N1, J, JP, JP1, JR, ZZZ71)
      DO 122 I = 1,MM
C      INITIALIZE CNTX(,,2); CNTX(,,1) NOT NEEDED.
      DO 70 J = 1,MM
        CNTX(J,2) = CNT(I,J,2)
70      CONTINUE
C      THE WEIGHTED COPY.
      DO 71 J = 1,MM
        CNTY(J,2) = CNTX(J,2)
71      CONTINUE
      DO 120 N1 = 3,JMAX1
        JP = N1 - 1
C      RESET CURRENT CNTX.
      DO 72 J = 1,MM
        CNTX(J,N1) = ZERO
72      CONTINUE
C      SUM OVER R (R = -1,..., JP-2).
C      FIRST LOOP: EXCLUDE CNT(,,1).
      JP1 = JP - 1
      DO 90 M1 = 1,JP1
        JR = M1 - 2
        CALL DGEMV('N', MM, MM, ONE, PP(1,1,M1), NCDS,
&                CNTY(1,N1-JR-2), 1,
&                ONE, CNTX(1,N1), 1)
        CALL DGEMV('N', MM, MM, ONE, QQ(1,1,M1), NCDS,
&                CNTX(1,N1-JR-2), 1,
&                ONE, CNTX(1,N1), 1)
90      CONTINUE
C      SECOND LOOP: CNT(,,1) = I (IMPLICIT).
      M1 = JP
      DO 92 J = 1,MM
        CNTX(J,N1) = CNTX(J,N1) + QQ(J,I,M1)
92      CONTINUE
C      FINISH CNT(JP) .
      ZZZ71 = - ONE / DBLE(JP * (JP - 1))
      DO 100 J = 1,MM
        CNTX(J,N1) = ZZZ71 * CNTX(J,N1)
100     CONTINUE
C      THE WEIGHTED COPY.
      DO 102 J = 1,MM
        CNTY(J,N1) = (N1 - 1) * CNTX(J,N1)
102     CONTINUE
C      STORE INTO CNT, LEAVE CNTX FOR ITERATION.
      DO 110 J = 1,MM
        CNT(I,J,N1) = CNTX(J,N1)
110     CONTINUE
120     CONTINUE
122 CONTINUE

```


PROGRAM PROFILES

Profiles were generated using pixie. It was checked that a single pass (DDCA call) gives the same percentages as a full run (about 7 calls).

Single threaded mode:

Block	N	Percentage of total EWF2P CPU time
COMPLIB_DGEMM_HOISTC *1	49	79.7
RRP31C		90.9 *2
(Other)		9
COMPLIB_DGEMM_HOISTC *1	121	88.0
COMPLIB_DGEMM_HOISTC *1	225	

*1 /usr/lib64/libblas.so:/vince/6.2-mar09/work/cmplrs/libblas/complib_dgemm_hoistc.f
*2 ewf2p.e__usr_bin_f77_r8000_mips4_64_03_lcomplib.sgimath:rrp31c.f;
cumulative percentage.

Multi threaded mode:

Block	N	Threads	Percentage of total EWF2P CPU time
DGEMV_MV *1	49	4	82.9
RRP41C *2			99.7
DGEMV_MV *1	121	6	82.9 (?)

*1 /usr/lib64/libblas.so:/vince/6.2-mar09/work/cmplrs/libblas/dgemv.f
*2 ewf2p.e__usr_bin_f77_r8000_mips4_64_03_mp_lcomplib.sgimath:
rrp41c_mp.f; cumulative precentage.

RUNS

Single threaded:

RRP31C (IRRPV = 314)
R8000 75 or 90 MHz
/usr/bin/f77 -r8000 -mips4 -64 ... -lcomplib.sgimath

Multi threaded:

RRP41C (IRRPV = 414) (c\$doacross),
R8000 mixed frequency (2 x 90 MHz, 4 x 75 MHz)
/usr/bin/f77 -r8000 -mips4 -64 -mp ... -lcomplib.sgimath
/usr/bin/f77 -r8000 -mips4 -64 -mp ... -lcomplib.sgimath_mp

(The latter seem both equivalent; any differences would only be felt in minor parts of program. But to measure the hand optimization speed, it is better to link the non-parallel complib.sgimath.)

RESULTS

Table II.1. Km = 24, N = 49. 75 MHz.

```

=====
RRP*** version      Threads  Library linked      CPU time
                    explicitly  per determinant*   RRP31C  RRP41C
-----
RRP31C (vectorized)  1      complib.sgimath    10
                    1
RRP41C (parallelized) 1      complib.sgimath    24      0.4      1
                    2      14      0.7      1.7
                    4      10      1        2.4
                    6      8.5     1.2     2.8

RRP41C (parallelized) 1      complib.sgimath_mp
                    2      16
                    4      10
                    6      8.1
=====

```

* One DDCA call (all intervals). There are about 7 calls per run. The CPU time is the average of all calls in a run. It was verified that the run for a single pass gives the CPU time which is very close to this averaged time. 80% of the CPU time is used by DGEMM.

Table II.2. As Table II.1, but Km = 40, N = 121. 75 MHz.

```

=====
RRP*** version      Threads  Library linked      CPU time
                    explicitly  per determinant*   RRP31C  RRP41C
-----
RRP31C (vectorized)  1      complib.sgimath    111
                    1
RRP41C (parallelized) 1      complib.sgimath
                    2
                    4
                    6      148
=====

```

APPENDIX II.A. CONTROL FILES

(1) M2MK control files:

```

-----
98/11/19  f77
T          LSTORE (UNFORMATTED OUTPUT)
1          INUSEL (0: UNSYMMETRIC; 1: SYMMETRIC)
TT        PCFC, PVC (PRINT F, V POWER EXPANSIONS)
          1.0          -1.0 M1/2/3 (-1: INF)
20  0  F          MUU, IPOS, PSYM
1  1  -1  -1  0    IPFL, IPFU, IPVL, IPVU, IPWU
1
1          -2.0          -2.0          1.0  J, FPAR(.,J)
2          MODF (INTERPRETATION OF FPAR BY CFC...)
1
1          -2.0          -2.0          1.0  J, VPAR(.,J)
0          MODV (INTERPRETATION OF VPAR BY VC...)
16 16          (NGOA(I), I = 1,2)
4  4          (NSUBA(I), I = 1,2)
16 16 16 16 16 16 16 16 16 16  (NGOL(I,1), I = 1,10)
4  4  4  4  4  4  4  4  4  4  (NSUBL(I,1), I = 1,10)
16 16 16 16 16 16 16 16 16 16  (NGOL(I,2), I = 1,10)
4  4  4  4  4  4  4  4  4  4  (NSUBL(I,2), I = 1,10)
0.100  0.030          DAS, DLS
TT        POMEGA, POTHER (WORKING RUNS: TT)
TFFFF    PCON, PTEST, PTEST1, PRES (WORKING RUNS: TFFF), PCONTR
FFTFFFF  PT00, PT10, PRESO, PTG, PTGA, PTGL, PTJ (WRKNG RUNS: F...F)
4          NSPR (MAX. NO. ROWS/COLUMNS OF MATRICES TO BE PRINTED)
0          itestq
-----

#!/bin/csh -f
# m2mk-

set pro = m2mk
set do = "~/sgi98/out"
set ds = "/dsk3/tmp/krivec"

set fi = "1a0"
set fo = "1aa4001"

set eex = "56p120a6432a_773"
set zzzexe = "~/cfhh/pd/${pro}.e${eex}"
limit stacksize 500000
set nicev = 10

source M2MK0000.csh
-----

```

(2) EWF2P control files (example):

```
-----  
98/11/19 f77 Km = 24 test  
314 IRRPV (314: 3.1.1V1)  
FFFFFFFF LTDD,LTDDR,LTVICD,LTRRPS,LPRBIN,LPRZ0M,LTCPU,LTCRU,LPRPQ  
FFFFFF LPRCV0, LPRXX, LPRCV, *LPRCVM, LPRMAT, LPRWF  
TFT LTZE, LTZEIF, LXLAST (IPROG = 200)  
T LTDET  
FF LDOUBL, LDOUBM  
8 IINTPR  
20 200 LM, IPROG  
0 IENXL (LMOD = 5, 6 ONLY)  
0 IOD  
0 IRTCO  
0 49 1 IPWUU, NSU, INUSEL  
20 16 NM, JMAX  
0.50 0.50 9999.0 BC0, BC1, RHOUB  
2.8000 3.0000 A, B  
+1.0000000D-14 0.1000000D+00 5.00000000D+00 EPSP, TOL, DZU  
0.50 5.00 120.00 ZM, ZMATCH, ZTOP  
0 NHH  
1 LMOD  
2.9 3.00 1.00 ENXL, ENXU, ENXS  
1 IPIO (0: M1M-, 1: M2M-)  
0.00 999.00 1 1 ZOMTTT, ZOMTTD, IPRTTT, IPCTTT  
-----
```

```
#!/bin/csh -f
```

```
setenv MP_SET_NUMTHREADS 1
```

```
set pro = "ewf2p"  
set prl = "m2mk"  
set di = "~/sgi98/inp"  
set do = "~/sgi98/out"  
set ds = "/dsk3/tmp/krivec"
```

```
# All blas/linpack routines from system libraries.  
set eex = "_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath"
```

```
set km = "6"
```

```
set fm = "1a64001"  
set fi = "1a${km}0"
```

```
set irr = cat $pro$fi.i|grep IRRPV|awk '{print $1}'  
set fo = "0${km}cfeci555b33a"  
set fol = "${pro}${fm}${fo}_${eex}_${irr}_t${MP_SET_NUMTHREADS}"  
set fool = ""
```

```
set zzzexe = "~/sgi98/pd/${pro}.e_${eex}"  
limit stacksize 300000  
set nicev = 0
```

```
set sigrun = "${do}/${prl}${fm}.sig" # start signal file
```

```
source EWF2P0000.csh
```

```
\rm -f $FLU30 $FLU40  
-----
```

APPENDIX II.B. OUTPUT FILES

These runs were done without pixie. Multi-pass runs are listed; the purpose was to check that the zero is found to the same precision in all cases.

Km = 24, N = 49:

75 MHz:

```
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_lcomplib.sgimath_314.2
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP31C- 2.0, 96/08/05. -1.0; -RRPSM 3.1.1V1. -3.1V1S -3.0V1S -3.0VS
DET:      -7.6262076063431188 10** 37 ENERGY      2.7999999999999998
DET:      6.5711433071813374 10** 37 ENERGY      2.9999999999999996
DET:      2.0077284429255133 10** 36 ENERGY      2.9065738535396579
DET:      3.7022999515154980 10** 33 ENERGY      2.9037282905579587
DET:      -1.7360133514077343 10** 29 ENERGY      2.9037230387903326
DET:      -3.8760312384817515 10** 23 ENERGY      2.9037230390365769
DET:      1.9216012805935490 10** 23 ENERGY      2.9037230390365778
1 0.1921601280593552E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 10.11 SEC.
USER      70.79      DIF      70.79      REF      0.00      SYS      0.44
```

```
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_41
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY      2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY      2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY      2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY      2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY      2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY      2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY      2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 24.10 SEC.
USER      168.72      DIF      168.72      REF      0.00      SYS      0.64
```

```
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_41
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY      2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY      2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY      2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY      2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY      2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY      2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY      2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 13.67 SEC.
USER      95.73      DIF      95.73      REF      0.00      SYS      0.64
```

```
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_41
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY      2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY      2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY      2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY      2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY      2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY      2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY      2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 10.19 SEC.
USER      71.35      DIF      71.35      REF      0.00      SYS      0.71
```

```

-----
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_41
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY 2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY 2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY 2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY 2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY 2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY 2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY 2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 8.49 SEC.
USER 59.46 DIF 59.46 REF 0.00 SYS 0.74
-----

```

```

-----
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_mp
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY 2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY 2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY 2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY 2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY 2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY 2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY 2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 16.92 SEC.
USER 118.49 DIF 118.49 REF 0.00 SYS 0.89
-----

```

```

-----
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_mp
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY 2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY 2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY 2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY 2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY 2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY 2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY 2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 10.00 SEC.
USER 70.04 DIF 70.04 REF 0.00 SYS 0.73
-----

```

```

-----
ewf2pla6400106cfeci555b33a_usr_bin_f77_r8000_mips4_64_O3_mp_lcomplib.sgimath_mp
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P
DET:      -7.6262076063431072 10** 37 ENERGY 2.7999999999999998
DET:      6.5711433071813330 10** 37 ENERGY 2.9999999999999996
DET:      2.0077284429255240 10** 36 ENERGY 2.9065738535396579
DET:      3.7022999514429218 10** 33 ENERGY 2.9037282905579587
DET:      -1.7360127395319718 10** 29 ENERGY 2.9037230387903326
DET:      -3.8867156868107071 10** 23 ENERGY 2.9037230390365769
DET:      2.0731391735528364 10** 23 ENERGY 2.9037230390365778
1 0.2073139173552839E-13 H 0.0000E+00 2.9037230390365778
5 + 2 DET. EVALUATIONS OF 8.12 SEC.
USER 56.83 DIF 56.83 REF 0.00 SYS 0.70
-----

```

Km = 40, N = 121:

```
-----  
ewf2plaa40010acfec1555b33a_usr_bin_f77_r8000_mips4_64_03_lcomplib.sgimath_314.2  
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)  
-RRP31C- 2.0, 96/08/05. -1.0; -RRPSM 3.1.1V1. -3.1V1S -3.0V1S -3.0VS  
DET: -3.8792406013834837 10**120 ENERGY 2.7999999999999998  
DET: 3.3885222831668278 10**120 ENERGY 2.9999999999999996  
DET: 7.8304525751813507 10**118 ENERGY 2.9058935917048259  
DET: 1.7534098087577488 10**116 ENERGY 2.9037293025731787  
DET: -7.4871922634738519 10**111 ENERGY 2.9037244482953235  
DET: -3.9514242780718138 10**106 ENERGY 2.9037244485025955  
DET: 8.1751020746561931 10**105 ENERGY 2.9037244485025968  
1 0.8175102074656207E-14 H 0.0000E+00 2.9037244485025968  
5 + 2 DET. EVALUATIONS OF 110.93 SEC.  
USER 776.57 DIF 776.57 REF 0.00 SYS 2.37  
-----
```

```
ewf2plaa40010acfec1555b33a_usr_bin_f77_r8000_mips4_64_03_mp_lcomplib.sgimath_mp  
-RRLSDE- 1.1, 96/08/02. 1.0, 93/05/18. 1.4, 91/03/13 (VICDF)  
-RRP41C-1.0 98/11/09 RRPSM 4.1.1V1S 96/02/09 -4.1PV1S 4.1PV1 -M_4.1P  
DET: -3.8792406013834846 10**120 ENERGY 2.7999999999999998  
DET: 3.3885222831668256 10**120 ENERGY 2.9999999999999996  
DET: 7.8304525751813880 10**118 ENERGY 2.9058935917048259  
DET: 1.7534098086924912 10**116 ENERGY 2.9037293025731787  
DET: -7.4871715111870980 10**111 ENERGY 2.9037244482953235  
DET: -7.4444938456006433 10**106 ENERGY 2.9037244485025946  
DET: 8.3176068643449401 10**105 ENERGY 2.9037244485025968  
1 0.8317606864344954E-14 H 0.0000E+00 2.9037244485025968  
5 + 2 DET. EVALUATIONS OF 147.73 SEC.  
USER 1034.16 DIF 1034.16 REF 0.00 SYS 11.68
```

PART III

PARALLELIZATION OF THE CFHHM PROGRAMS ON SPP-1000 October 1995, IJS/NSC SPP-1000 (borg)

The SPP-1000 machine was beset by hardware and software failures. In addition, the best libraries available were not utilized, therefore the results have only qualitative meaning. See Part II for more recent results, which are qualitatively consistent with the present ones.

III.1. Short description of benchmark: -----

See Appendix III.C for benchmark input file (He atom ground state). RRPSM is called 61 times. I-loop has MM = 49 iterations. C3860: vectorization only.

SPP-1000: all routines -O2 -nore -cxpa ... except RRPSM which is as indicated. -nore is used until the reason for program failure without -nore is determined. The program also fails if -cxpa is not included, even if -nore is used.

III.2. Description of initial modifications -----

To enable parallelization, the I loop (innermost in RRPSM 1.0) was taken out of the loop nest to be the outermost. Physically this means each column of the matrix solution of the system of differential equations was treated independently and in parallel, on each z interval (RRPSM is called once per interval).

Versions 1.1, 4.1 and 4.2 were made on C3860 (see cfhhopt1.txt). Main changes were as follows:

Version	Changes
1.1	Second recursion loop simplified (only QQ appears)
3.0	Streamlined: eliminated calls to BINA and POWA
4.0	Moved I loop outside, RR remains inside, although independent of I
4.1	Factor (p - r - 2) incorporated into a copy of array CNT
4.2	RR outside, factor (p - r - 2) incorporated in RR (RRX)
4.2.1	As 4.2, but RRX 3-dimensional (save half space)
4.2.2	As 4.2.1, but RRX loop parallelized (J outermost)
4.*P*	Explicit parallelization directives
4.*PV*	Explicit parallelization directives, VecLib in innermost

III.3. Results -----

The programs were transferred from marvin. They mostly fail to run without cxpa, reporting errors like "bus error" or "error unwinding stack." One of the reasons could be that there are DATA statements in many routines. In this test, all of the routines were compiled with -nore (except where noted) although this did not prevent the program from failing occasionally. There is conflicting information in the books whether -nore really prevents the parallelization.

File names were changed a few times. For example, output files of the form ewf2n*_2*_3*_16a.2ff correspond to old tests without -peel -mrl; the files ewf2n*_2*_3*_16xa.2ff and ewf2n*_2*_3x*_16a.2ff should mean the same, namely including -peel -mrl in the rrpsm*.f only.

Table III.1: Execution times. Times are those with cxxpa running, as reported by cxxpa. The reference value (routine before optimizations) is rrpsm.f (RRPSM 1.0). Compiler options for all routines except RRPSM: fc -O2 -nore -cxxpa ...; RRPSM: fc -O3 -nore -cxxpa ... (exceptions indicated). (The total CPU time in the output file (routine tempd) is almost twice as large as the cxxpa-reported time; cxxpa also shows rrpsm to use about 96% CPU time.)

```

=====
Version                               Time
-----                               -
                C3860 (-O2)
                -----
                CPU
                ---
                Total RRPSM loops
                -----
                No.
                proc.
                -----
                SPP-1000 (-O2, -O3)
                -----
                CPU
                ---
                Total RRPSM loops
                -----
                WALL
                ----
                Total RRPSM loops
                -----
-----
1.0          28    22    22
1.1          29    22    22
4.1          49    44    44          1+
                                     8          81    77
                                     139   134    1*2    83
                                     221
                                     80*2
4.1P1
                                     32    160   155   145    38
                                     32    158   152   142    37    30    21
                                     16    140   134   127    40
                                     16    141   136   129    38    31    24++
                                     16    142   137   130    34    28    21+++*
                                     16    134   129   122    38    31    24+x
                                     16    139   134   127    28
                                     16    128   124   117    34    28    14+v
                                     21+v*
                                     8    107   103   101    49
                                     8    110   105   103    37    32    42
                                     29++
4.1P3
                                     8    106   102   100    42
                                     34+r
4.1PV1
                                     32    118   113   103    33
                                     32    112   107   97     33    27    16
                                     17++
                                     16    73    68    62    29
                                     16    81    76    69    30    23    17++
                                     16    79    74    68    30    24    17+x
                                     16    78    73    67    35    28    22+v
                                     8    56    51    49    25
                                     8    57    52    50    25    20    17
                                     18++
4.1P2
                                     32    166   161   152    44
                                     28
                                     16    137   132   126    44
                                     16    135   130   124    50
                                     31
                                     37++
                                     8    110   106   104    46
                                     8    112   107   105    52
                                     39
                                     45++

```

4.2	29	24	23	1+	168	164		172		
				8	277	272	234*1	68		39*1
4.2P1				32	442	436	394	76		27
				32	440	434	392	75	68	25++
				16	282	277	248	80		44
				16	280	275	246	64	57	28++
				8	184	180	170	80		65
				8	182	177	167	41	35	25++
4.2.1P1				32	498	492	450	86		36++
				16	303	298	269	78		41++
				8	202	198	187	45		28++
4.2.2P1				32	error unwinding stack					
				16	383	378	281	75		52++ *4
				8	227	223	201	102		89++ *3

=====

*1 Innermost parallel loop (374a). Only loop 335 is reported by fc as parallel, and the innermost loops look like having been simply replicated on all 8 processors (see the cxxpa report).

*2 Only loop 284 is parallelized by fc; also, cxxpa reports only on its optimization time; the innermost loops are not parallel, and even 284 seems to have been simply replicated. This was the reason to introduce 4.1P1 (directive to force parallelization of 334).

+ Compiled with -O2.

++ Unlimited optimization (fc ... -mrl -peel ...) in rrrpsm..., but not in other routines.

+++ A repeated "++" run at another time.

+x Unlimited optimization (fc ... -mrl -peel ...) in all routines.

+v Borg VecLib called instead of the CFHH package VecLib sources; unlimited optimization (fc ... -mrl -peel ...) in all other routines.

+v* A repeated "+v" run at another time.

+r -nore removed (reentrant compilation), unlimited optimization. The variable LCALL0 eliminated (assumed that it makes problems with reentrancy, but that may not be true).

*3 The RRX loop is also parallelized and takes 20 (5) sec. The main loop increases enormously against 4.2P1.

*4 The RRX loop takes 92 (12) sec.

*5 On one occasion, first run failed, second (exact repetition) successful.

NOTES

Syspic shows that during parallel execution, the CPU usage is 100% only on gsm8 (single hypernode); on gsm16, gsm32 it is progressively smaller. This is reflected in the small speedup on more than 8 processors.

The program sometimes fails which means there is some error (probably in the machine). This is independent of whether cxa is running or not.

Unlimited optimization (-mrl -peel) can help significantly on 8 processors (see especially 4.2P1 on 8 processors).

On more processors, in all cases, CTI (internode) communication becomes a severe limiting factor for speed.

4.1P1: total wall time better than with 4.2P1; loops wall time worse. So 4.1P1 is the better topology of the two; see also 4.2.2P1: because two loop nests cannot be efficiently parallelized in RRPSM, the gain in main loop time by 4.2P1 is lost in the auxiliary loop which should not be parallelized.

On the other hand, 4.1 is bad on C series.

4.2.2P1: two loops parallelized in RRPSM make the time increase; also, a lot of the time the system is using 100% CPU, which reminds of the situation when the entire package was naively compiled under -O3.

4.1 and 4.2 could not be compiled under fc -mrl -peel; compiler error.

Appendix III.A

Thread distribution of I from:
ewf2nla6400106cfeci555b320_2_nr_p_4.1P1_3_nr_p_32b.2ff

(I = 1,... 49; threads 0...32)

-RRPSM	-	I	1	THREAD	0
-RRPSM	-	I	2	THREAD	1
-RRPSM	-	I	3	THREAD	2
-RRPSM	-	I	4	THREAD	3
-RRPSM	-	I	5	THREAD	4
-RRPSM	-	I	6	THREAD	5
-RRPSM	-	I	7	THREAD	6
-RRPSM	-	I	8	THREAD	7
-RRPSM	-	I	9	THREAD	8
-RRPSM	-	I	10	THREAD	9
-RRPSM	-	I	11	THREAD	10
-RRPSM	-	I	12	THREAD	11
-RRPSM	-	I	13	THREAD	12
-RRPSM	-	I	14	THREAD	13
-RRPSM	-	I	15	THREAD	14
-RRPSM	-	I	16	THREAD	15
-RRPSM	-	I	17	THREAD	15
-RRPSM	-	I	18	THREAD	16
-RRPSM	-	I	19	THREAD	16
-RRPSM	-	I	20	THREAD	17
-RRPSM	-	I	21	THREAD	17
-RRPSM	-	I	22	THREAD	18
-RRPSM	-	I	23	THREAD	18
-RRPSM	-	I	24	THREAD	19
-RRPSM	-	I	25	THREAD	19
-RRPSM	-	I	26	THREAD	20
-RRPSM	-	I	27	THREAD	20
-RRPSM	-	I	28	THREAD	21
-RRPSM	-	I	29	THREAD	21
-RRPSM	-	I	30	THREAD	22
-RRPSM	-	I	31	THREAD	22
-RRPSM	-	I	32	THREAD	23
-RRPSM	-	I	33	THREAD	23
-RRPSM	-	I	34	THREAD	24
-RRPSM	-	I	35	THREAD	24
-RRPSM	-	I	36	THREAD	25
-RRPSM	-	I	37	THREAD	25
-RRPSM	-	I	38	THREAD	26
-RRPSM	-	I	39	THREAD	26
-RRPSM	-	I	40	THREAD	27
-RRPSM	-	I	41	THREAD	27
-RRPSM	-	I	42	THREAD	28
-RRPSM	-	I	43	THREAD	28
-RRPSM	-	I	44	THREAD	29
-RRPSM	-	I	45	THREAD	29
-RRPSM	-	I	46	THREAD	30
-RRPSM	-	I	47	THREAD	30
-RRPSM	-	I	48	THREAD	31
-RRPSM	-	I	49	THREAD	31

Appendix III.B

File: /users/krivec/cfhh/pd/opt_rrpsm_borg.csh:

```
# Borg rrpsm optimization ``make`` routine.
# opt_rrpsm: exchanges of rrpsm*.o in ol_O2....a, relink.
# rrpsm is compiled with fc -$opt1 -$nore1 -$pax1,
# other routines with fc -$opt -$nore -$pax.
# (nore should be "nr" or empty, pax should be "p" or empty.)
# CPU and wall times may vary due to different loads and profiling.
# R. Krivec 95/10/17.
# R. Krivec 95/10/20.
# R. Krivec 95/10/27.

# set verbose
unset rrpsmonly
unset linkonly
unset setonly

set rrpsmonly # careful: the first time ddaa_2.0 has to be compiled
# set linkonly
# set setonly

set vl=vb
set eex0=24p0s

set opt=2x
set nore=nr
set pax=p
set lib="ol_`echo ${opt} ${nore} ${pax} | sed 's/ /_/g`"

set ver=4.1P1
set opt1=3x
set nore1=nr
set pax1=p
set eex="_opt_rrpsm_`echo $lib $ver $opt1 $nore1 $pax1 $vl | sed 's/ /_/g`"

echo "--" $vl
echo "--" $eex0 $opt $nore $pax
echo "--" $ver $opt1 $nore1 $pax1
echo -n "Return to continue... "; set zzz=$<
echo "--" $lib
echo "--" $eex
echo -n "Return to continue... "; set zzz=$<
if ( $vl == 'vb' ) then
    set lib=${lib}_nv # modify lib #####
    if ( ! -e ${lib}.a ) exit
    echo "--" $lib
    echo -n "Return to continue... "; set zzz=$<
endif
if ( $test == 'test' ) goto _TEST

if ( $?setonly ) then
    unset setonly
    exit
endif

if ( $?linkonly ) goto _LINK

# Cleanup the libraries
ar tv ${lib}.a | grep -E 'ddaa|rrpsm\|.rrpsm_'
ar dv ${lib}.a rrpsm.o |& grep -v 'not found'
ar dv ${lib}.a rrpsm*.o |& grep -v 'not found'
ar dv ${lib}.a `echo rrpsm*.o | sed 's/\./\./g` |& grep -v 'not found'
# the above works for one character too much
if ( $vl == 'vb' ) then
    source ewf2n_veclib_lib_remove.csh
```

```

endif
if ( $?rrpsmonly ) goto _C1
  ar dv ${lib}.a ddaa.o |& grep -v 'not found'
  ar dv ${lib}.a ddaa*.o |& grep -v 'not found'
_C1:
ar tv ${lib}.a | grep -E 'ddaa|rrpsm\.|rrpsm_'

pro rrpsm_${ver}
echo $pro
alias zzz fc${opt1}${nore1}${pax1}
zzz
~/bin/para.csh $pro
xpr

if ( $?rrpsmonly ) goto _LINK

_TEST:
if ( $ver == '1.0' || $ver == '1.1' ) then
  pro ddaa
else
  pro ddaa_2.0
endif
echo $pro
alias zzz fc${opt}${nore}${pax}
zzz
xpr

pro ewf2n
echo $pro
alias zzz fc${opt}${nore}${pax}
zzz

_LINK:
ar tv ${lib}.a | grep -E 'ddaa|rrpsm\.|rrpsm_'
pro ewf2n
alias zzz ldu${v1}${pax}
zzz

# grep ', rrpsm' ewf2n.m$eex
kk ewf2n.e$eex ewf2n.m$eex
unset rrpsmonly
unset linkonly

```

Appendix III.C

File: /users/krivec/cfhh/inp/ewf2n1a_opt_rrpsm.i:

```
95/10/06 He opt_rrpsm
FFFFFFFF      LTDD,LTDDR,LTVICD,LTRRPS,LPRBIN,LPRZ0M,LTCPU,LTCRU
TFFTFT      LPRCV0, LPRXX, LPRCV, *LPRCVM, LPRMAT, LPRWF
TFT         LTZE, LTZEIF, LXLAST (IPROG = 200)
T           LTDET
FF          LDOUBL, LDOUBM
9999        IINTPR
 20 200     LM, IPROG
  0         IENXL (LMOD = 5, 6 ONLY)
  0         IOD
  0  49    1          IPWUU, NSU, INUSEL
 20 16      NM, JMAX
  0.50     0.50  9999.0    BC0, BC1, RHOEW
2.9000     3.0000      A, B
+1.0000000D-14 0.10000000D+00 5.00000000D+00  EPSP, TOL, DZU
  0.50     5.00  120.00   ZM, ZMATCH, ZTOP
  0         NHH
  2         LMOD
2.9         3.00         1.00  ENXL, ENXU, ENXS
  1         IPIO (0: M1M-, 1: M2M-)
  0.00    999.00    1    1    ZOMTTT, ZOMTTD, IPRTTT, IPCTTT
-----
```

File: /users/krivec/cfhh/inp/ewf2nla_opt_rrpsm_borg.c:

```
#!/bin/csh -f

echo $ver                # this must be set
echo $opt $nore $pax    # this must be set
echo $opt1 $nore1 $pax1 # this must be set
echo $vl                # this must be set
echo $paxe              # this must be set
echo $repv              # this must be set
echo -n "Return to continue... "; set zzz=$<

set xxx="`echo $opt $nore $pax | sed 's/ /_/g`'"
set xxx1="`echo $ver $opt1 $nore1 $pax1 $vl | sed 's/ /_/g`'"

set pil = 'xxx'; set fo3 = 'xxx'; set fo4 = 'xxx'
set pi2 = 'xxx'; set fo5 = 'xxx'; set fo6 = 'xxx'
set rr = 'xxx'; set best = 'xxx'; set work = 'xxx'

set rr = 0      # 0: original run;
                # 1: restart (LMOD = 5, --> w.f.);
                # 2: re-restart (LMOD = 51, --> w.f.);
                # 3: tabulation (LMOD = 7, E from iteration file).
set xer = 0     # 0: previous run wrote best E value file
                # 1: previous run stopped before writing best E value file
                # (this overrides value of best if previous run had error)

if ($rr == 1 || $rr == 2) set best = 1 # restart E: best value
if ($rr == 3) set best = 0             # tabulation E; iteration file
if ($xer == 1) set best = 0           # override best: use iteration file

set work = 1   # 1: ewf2-
                # 2: av3m-
                # 3: both

set fi = 'la_opt_rrpsm' # 8
set fo1 = 'la64001'    # 9
set fo2 = "06cfeci555b320_${xxx}_${xxx1}_${repv}" # 10
echo $fo2
echo -n "Return to continue... "; set zzz = $<

if ($rr >= 1) then
    set pil = 'ewf2n' # 11 initial run
    set fo3 = 'laa4001' # 12
    set fo4 = '0acfec5555b33a' # 13
    echo '---- pil: ' $pil
endif

if ($rr == 2) then
    set pi2 = 'ewf2n' # 14 previous restart run
    set fo5 = 'laa4001' # 15
    set fo6 = '0acfec5555b33a' # 16
    echo '---- pi2: ' $pi2
endif

set de = "~/cfhh/pd" # 1
set di = "~/cfhh/inp" # 2
set do = "~/cfhh/out/opt_rrpsm"
set ds = "~/cfhh/out/opt_rrpsm"
set pe = 'ewf2n' # 5
set pi = 'm2mk' # 6
set fe = "e_opt_rrpsm_ol_${xxx}_${xxx1}" # 7
```



```

if ( $work == 1 || $work == 3 ) then
  echo '---- work' $work

  if ( $paxe != 'p' ) set paxe = '0'
  $di/${pe}00${paxe}.csh \
    $de $di $do $ds $pe $pi $fe $fi $fo1 $fo2 $pil $fo3 $fo4\
    $pi2 $fo5 $fo6 $rr $best

  # 1 2 3 4 5 6 7 8 9 10 11 12 13
  # 14 15 16 17 18

endif
set zzzrep=$do/ewf2n${fo1}${fo2}.report
if ( -e ewf2n.report ) mv ewf2n.report $zzzrep

if ( $work > 1 ) then

  set dol = ''
  set pi = $pe
  set pil = 'n' # see $pi
  set pe = 'av3mj'
  set fe = 'e'

  set fil = '2222224'
  set fi2 = 'a'
  set fi = 'md'$fil$fi2
  set fo3 = '0a'$fil${fi2}$pil

  $di/${pe}000.c $de $di $do $ds $pe $pi $fe $fi $fo1 $fo2 $fo3 $dol

  # 1 2 3 4 5 6 7 8 9 10 11 12

endif

```

Appendix III.D

Optimized versions of RRPSM with comments filtered out.

File: rrpasm_1.0.fnoc

```

SUBROUTINE  RRPSM(NCDS, NCDP, NCDCN, NDBIN1, NDBIN2, NDZOMP,
1           WS, WD, MM, MU, IPXU, IPOFF, ZOM, JMAX, AA,
2           RHOEW, PP, QQ, RR, BIN, ZOMPPOW,
3           LTEST, LPRBIN, LPRZOM, NOUT,
4           CNT)
IMPLICIT   REAL*8 (A - H, O - Z)
LOGICAL    LTEST, LPRBIN, LPRZOM
DIMENSION  WS(NCDS,NCDS,NCDS), WD(NCDS,NCDS,NCDS),
1          MU(NCDS),
2          PP(NCDS,NCDS,NCDCN), QQ(NCDS,NCDS,NCDCN),
3          RR(NCDS,NCDS), BIN(NDBIN1,NDBIN2), ZOMPPOW(NDZOMP),
4          CNT(NCDS,NCDS,NCDCN)
CHARACTER*6 NAME / 'RRPSM ' /
CHARACTER*60 VERS
*/ ' 1.0, 93/05/14 (RRPSL 2.0) STREAMLINED; DISTR. M1 LOOP ' /
LOGICAL    LCALL0
DATA       LCALL0 / .TRUE. /
DATA       ZERO, ONE, TWO / 0.D0, 1.D0, 2.D0 /
IF (LCALL0) WRITE (NOUT,4000) NAME, VERS
IF (MM .GT. NCDS) CALL ERR2(NAME, 1, 1, NOUT)
IF (IPXU .GT. NCDP) CALL ERR2(NAME, 2, 1, NOUT)
IF (JMAX+1 .GT. NCDCN) CALL ERR2(NAME, 3, 1, NOUT)
IF (ABS(AA) .LT. CDXTOL()) CALL ERR2(NAME, 4, 1, NOUT)
IF (LCALL0 .AND. IPOFF .GT. 2) CALL ERR2(NAME, 11, 0, NOUT)
IF (LCALL0 .AND. JMAX .LT. 2) CALL ERR2(NAME, 21, 0, NOUT)
IF (LCALL0) LCALL0 = .FALSE.
IF (JMAX .LT. 2) RETURN
IF (RHOEW .GE. ZERO) ZUW = TWO * AA * RHOEW
IF (RHOEW .LT. ZERO) ZUW = -RHOEW
JMAX1 = JMAX + 1
ZZZ4 = ONE / (TWO * AA)
IPU = IPXU - IPOFF
JRU = JMAX - 2 + 1
CALL BINA(NDBIN1, NDBIN2, IPU, JRU, BIN, LPRBIN, NOUT)
IPOWL = - JMAX
IPOWU = IPU
CALL POWA(NDZOMP, IPOWL, IPOWU, ZOM, LPRZOM, NOUT,
1        ZOMPPOW, NZOMOF)
DO 68 M1 = 1, JMAX
  JR = M1 - 2
  ZZZ51 = BIN(-1+3, JR+1+1) * ZOMPPOW(-JR-2+NZOMOF)
  DO 22 I = 1, MM
    DO 20 J = 1, MM
      PP(J, I, M1) = ZERO
20    CONTINUE
22    CONTINUE
    DO 24 I = 1, MM
      PP(I, I, M1) = ZZZ51
24    CONTINUE
    IF (ZOM .LE. ZUW) THEN
      IPXL = JR + 1 + IPOFF
      IF (IPXL .LE. IPXU) THEN
        DO 34 IPX = IPXL, IPXU
          IP = IPX - IPOFF
          ZZZ52 = - BIN(IP+3, JR+1+1)
1          * ZOMPPOW(IP-JR-1+NZOMOF)
2          * ZZZ4 ** (IP+1)
          DO 32 I = 1, MM
            DO 30 J = 1, MM
              PP(J, I, M1) = PP(J, I, M1)
1              + ZZZ52 * WD(J, I, IPX)
30            CONTINUE
32          CONTINUE
34        CONTINUE

```

```

32             CONTINUE
34             CONTINUE
              ENDIF
            ENDIF
            DO 42 I = 1,MM
              DO 40 J = 1,MM
                QQ(J,I,M1) = ZERO
40             CONTINUE
42             CONTINUE
            IF (JR .LT. 0) GO TO 66
              IF (JR .EQ. 0) THEN
                ZZZ61 = -0.25D0
                DO 50 I = 1,MM
                  QQ(I,I,M1) = ZZZ61
50             CONTINUE
              ENDIF
              IF (JR .GE. 0) THEN
                ZZZ62 = -BIN(-2+3,JR+1) * ZOMPOW(-JR-2+NZOMOF)
                DO 52 I = 1,MM
                  QQ(I,I,M1) = QQ(I,I,M1) + ZZZ62 * MU(I) ** 2
52             CONTINUE
              ENDIF
            IF (ZOM .GT. ZUW) GO TO 66
              IPXL = -1 + IPOFF
              IF (IPXL .GT. IPXU) CALL ERR2(NAME, 31, 1, NOUT)
              DO 64 IPX = IPXL,IPXU
                IP = IPX - IPOFF
                IF (IP .GE. 0 .AND. JR .GT. IP) GO TO 64
                ZZZ63 = - BIN(IP+3,JR+1) * ZOMPOW(IP-JR+NZOMOF)
                * ZZZ4 ** (IP+2)
1              DO 62 I = 1,MM
                DO 60 J = 1,MM
                  QQ(J,I,M1) = QQ(J,I,M1) + ZZZ63 * WS(J,I,IPX)
60             CONTINUE
62             CONTINUE
64             CONTINUE
66             CONTINUE
68             CONTINUE
            DO 124 N1 = 3,JMAX1
              DO 72 J = 1,MM
                DO 70 I = 1,MM
                  CNT(I,J,N1) = ZERO
70             CONTINUE
72             CONTINUE
              JP = N1 - 1
              JP1 = JP - 1
              DO 90 M1 = 1,JP1
                JR = M1 - 2
                ZZZ72 = JP - JR - 2
                DO 82 K = 1,MM
                  DO 80 J = 1,MM
                    RR(J,K) = ZZZ72 * PP(J,K,M1) + QQ(J,K,M1)
80             CONTINUE
82             CONTINUE
                DO 88 J = 1,MM
                  DO 86 I = 1,MM
                    DO 84 K = 1,MM
                      CNT(I,J,N1) = CNT(I,J,N1)
                      + CNT(I,K,N1-JR-2) * RR(J,K)
1              CONTINUE
84             CONTINUE
86             CONTINUE
88             CONTINUE
90             CONTINUE
              M1 = JP
              JR = M1 - 2
              ZZZ72 = JP - JR - 2
              DO 104 K = 1,MM
                DO 102 J = 1,MM
                  RR(J,K) = ZZZ72 * PP(J,K,M1) + QQ(J,K,M1)
102             CONTINUE
104             CONTINUE
            DO 108 J = 1,MM

```

```

                DO 106 I = 1,MM
                  CNT(I,J,N1) = CNT(I,J,N1) + RR(J,I)
106             CONTINUE
108             CONTINUE
                ZZZ71 = - ONE / DFLOAT(JP * (JP - 1))
                DO 122 J = 1,MM
                  DO 120 I = 1,MM
                    CNT(I,J,N1) = ZZZ71 * CNT(I,J,N1)
120             CONTINUE
122             CONTINUE
124             CONTINUE
                IF (.NOT.LTEST) RETURN
                WRITE (NOUT,4100) NAME, ZOM
                DO 132 K = 1,JMAX1
                  WRITE (NOUT,4110) K
                  DO 130 I = 1,MM
                    WRITE (NOUT,4120) (CNT(I,J,K), J = 1,MM)
130             CONTINUE
132             CONTINUE
                RETURN
4000            FORMAT (
                A 2H -, A6, 1H-, A60)
4100            FORMAT (//, 1H , 80(1H-), /,
                A 1H , 1H-, 2A4, 1H-, 4HZOM , F12.6)
4110            FORMAT (/,
                A 1H , 4H K , I4)
4120            FORMAT (
                A (1H , 8X, 4F16.8))
                END

```

File: rrpasm_4.0.fnoc

```
-----
SUBROUTINE  RRPSM(NCDS, NCDP, NCDCN, NDBIN1, NDBIN2,
1           WS, WD, MM, MU, IPXU, IPOFF, ZOM, JMAX, AA,
2           RHOEW, PP, QQ, RR, BIN,
3           LTEST, NOUT, CNT)
  IMPLICIT  REAL*8 (A - H, O - Z)
  LOGICAL   LTEST
  DIMENSION WS(NCDS,NCDS,NCDP), WD(NCDS,NCDS,NCDP),
1           MU(NCDS),
2           PP(NCDS,NCDS,NCDCN), QQ(NCDS,NCDS,NCDCN),
3           RR(NCDS,NCDS), BIN(NDBIN1,NDBIN2),
4           CNT(NCDS,NCDS,NCDCN)
  CHARACTER*6 NAME / 'RRPSM' /
  CHARACTER*60 VERS
*/ ' 4.0, 95/10/08 -M_3.0 ' /
  PARAMETER (ZERO = 0.D0, ONE = 1.D0, TWO = 2.D0)
  PARAMETER (NPDS = 49, NPDCN = 22)
  DIMENSION CNTX(NPDS,NPDCN)
  LOGICAL   LCALL0
  DATA     LCALL0 / .TRUE. /
  IF (LCALL0) WRITE (NOUT,4000) NAME, VERS
  IF (MM .GT. NCDS) CALL ERR2(NAME, 1, 1, NOUT)
  IF (IPXU .GT. NCDP) CALL ERR2(NAME, 2, 1, NOUT)
  IF (JMAX+1 .GT. NCDCN) CALL ERR2(NAME, 3, 1, NOUT)
  IF (ABS(AA) .LT. CDXTOL()) CALL ERR2(NAME, 4, 1, NOUT)
  IF (NPDS .NE. NCDS) CALL ERR2(NAME, 5, 1, NOUT)
  IF (NPDCN .NE. NCDCN) CALL ERR2(NAME, 6, 1, NOUT)
  IF (LCALL0 .AND. IPOFF .GT. 2) CALL ERR2(NAME, 11, 0, NOUT)
  IF (LCALL0 .AND. JMAX .LT. 2) CALL ERR2(NAME, 21, 0, NOUT)
  IF (LCALL0) LCALL0 = .FALSE.
  IF (JMAX .LT. 2) RETURN
  IF (RHOEW .GE. ZERO) ZUW = TWO * AA * RHOEW
  IF (RHOEW .LT. ZERO) ZUW = -RHOEW
  JMAX1 = JMAX + 1
  RHO0 = ZOM / (TWO * AA)
  DO 68 M1 = 1, JMAX
    JR = M1 - 2
    ZOMIR2 = ONE / (ZOM ** (JR + 2))
    ZZZA = BIN(-1+3, JR+1+1) * ZOMIR2
    DO 22 I = 1, MM
      DO 20 J = 1, MM
        PP(J, I, M1) = ZERO
20      CONTINUE
22      CONTINUE
    DO 24 I = 1, MM
      PP(I, I, M1) = ZZZA
24      CONTINUE
      IF (ZOM .LE. ZUW) THEN
        IPXL = JR + 1 + IPOFF
        IF (IPXL .LE. IPXU) THEN
          ZZZB0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 1)
          DO 34 IPX = IPXL, IPXU
            IP = IPX - IPOFF
            ZZZB = - BIN(IP+3, JR+1+1) * ZZZB0
            DO 32 I = 1, MM
              DO 30 J = 1, MM
                PP(J, I, M1) = PP(J, I, M1)
1                + ZZZB * WD(J, I, IPX)
30              CONTINUE
32              CONTINUE
            ZZZB0 = ZZZB0 * RHO0
34            CONTINUE
          ENDDIF
        ENDDIF
        DO 42 I = 1, MM
          DO 40 J = 1, MM
            QQ(J, I, M1) = ZERO
40          CONTINUE
42          CONTINUE
```

```

IF (JR .LT. 0) GO TO 66
  IF (JR .EQ. 0) THEN
    ZZZC = -0.25D0
    DO 50 I = 1,MM
      QQ(I,I,M1) = ZZZC
50    CONTINUE
  ENDIF
  IF (JR .GE. 0) THEN
    ZZZD = -BIN(-2+3,JR+1) * ZOMIR2
    DO 52 I = 1,MM
      QQ(I,I,M1) = QQ(I,I,M1) + ZZZD * MU(I) ** 2
52    CONTINUE
  ENDIF
IF (ZOM .GT. ZUW) GO TO 66
  IPXL = -1 + IPOFF
  IF (IPXL .GT. IPXU) CALL ERR2(NAME, 31, 1, NOUT)
  ZZZE0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 2)
  DO 65 IPX = IPXL,IPXU
    IP = IPX - IPOFF
    IF (IP .GE. 0 .AND. JR .GT. IP) GO TO 64
    ZZZE = - BIN(IP+3,JR+1) * ZZZE0
    DO 62 I = 1,MM
      DO 60 J = 1,MM
        QQ(J,I,M1) = QQ(J,I,M1)
&          + ZZZE * WS(J,I,IPX)
60      CONTINUE
62      CONTINUE
64      CONTINUE
        ZZZE0 = ZZZE0 * RHO0
65      CONTINUE
66      CONTINUE
68      CONTINUE
        DO 122 I = 1,MM
          DO 70 J = 1,MM
            CNTX(J,2) = CNT(I,J,2)
70          CONTINUE
          DO 120 N1 = 3,JMAX1
            JP = N1 - 1
            DO 72 J = 1,MM
              CNTX(J,N1) = ZERO
72          CONTINUE
              JP1 = JP - 1
              DO 90 M1 = 1,JP1
                JR = M1 - 2
                ZZZ72 = JP - JR - 2
                DO 82 K = 1,MM
                  DO 80 J = 1,MM
                    RR(J,K) = ZZZ72 * PP(J,K,M1) + QQ(J,K,M1)
80          CONTINUE
82          CONTINUE
              DO 86 K = 1,MM
                DO 84 J = 1,MM
                  CNTX(J,N1) = CNTX(J,N1)
1          + RR(J,K) * CNTX(K,N1-JR-2)
84          CONTINUE
86          CONTINUE
90          CONTINUE
              M1 = JP
              DO 92 J = 1,MM
                CNTX(J,N1) = CNTX(J,N1) + QQ(J,I,M1)
92          CONTINUE
              ZZZ71 = - ONE / DFLOAT(JP * (JP - 1))
              DO 100 J = 1,MM
                CNTX(J,N1) = ZZZ71 * CNTX(J,N1)
100         CONTINUE
              DO 110 J = 1,MM
                CNT(I,J,N1) = CNTX(J,N1)
110        CONTINUE
120        CONTINUE
122        CONTINUE
        IF (.NOT.LTEST) RETURN
        WRITE (NOUT,4100) NAME, ZOM

```

```
      DO 132 K = 1,JMAX1
        WRITE (NOUT,4110) K
        DO 130 I = 1,MM
          WRITE (NOUT,4120) (CNT(I,J,K), J = 1,MM)
130     CONTINUE
132 CONTINUE
      RETURN
4000 FORMAT (
      A 2H -, A6, 1H-, A60)
4100 FORMAT (//, 1H , 80(1H-), /,
      A 1H , 1H-, 2A4, 1H-, 4HZ0M , F12.6)
4110 FORMAT (/,
      A 1H , 4H K , I4)
4120 FORMAT (
      A (1H , 8X, 4F16.8))
      END
```

File: rrpasm_4.1P1.fnoc

```
-----
SUBROUTINE  RRPSM(NCDS, NCDP, NCDCN, NDBIN1, NDBIN2,
1           WS, WD, MM, MU, IPXU, IPOFF, ZOM, JMAX, AA,
2           RHO, PP, QQ, RR, BIN,
3           LTEST, NOUT, CNT)
  IMPLICIT  REAL*8 (A - H, O - Z)
  LOGICAL   LTEST
  DIMENSION WS(NCDS,NCDS,NCDS), WD(NCDS,NCDS,NCDS),
1           MU(NCDS),
2           PP(NCDS,NCDS,NCDCN), QQ(NCDS,NCDS,NCDCN),
3           RR(NCDS,NCDS), BIN(NDBIN1,NDBIN2),
4           CNT(NCDS,NCDS,NCDCN)
  CHARACTER*6 NAME / 'RRPSM' /
  CHARACTER*60 VERS
  * / ' 4.1P1, 95/10/19 -M_4.1 (SEE _4.2P1). ' /
  PARAMETER (ZERO = 0.D0, ONE = 1.D0, TWO = 2.D0)
  PARAMETER (NPDS = 49, NPDCN = 22)
  DIMENSION CNTX(NPDS,NPDCN), CNTY(NPDS,NPDCN)
  LOGICAL   LCALL0
  DATA     LCALL0 / .TRUE. /
  IF (LCALL0) WRITE (NOUT,4000) NAME, VERS
  IF (MM .GT. NCDS) CALL ERR2(NAME, 1, 1, NOUT)
  IF (IPXU .GT. NCDP) CALL ERR2(NAME, 2, 1, NOUT)
  IF (JMAX+1 .GT. NCDCN) CALL ERR2(NAME, 3, 1, NOUT)
  IF (ABS(AA) .LT. CDXTOL()) CALL ERR2(NAME, 4, 1, NOUT)
  IF (NPDS .NE. NCDS) CALL ERR2(NAME, 5, 1, NOUT)
  IF (NPDCN .NE. NCDCN) CALL ERR2(NAME, 6, 1, NOUT)
  IF (LCALL0 .AND. IPOFF .GT. 2) CALL ERR2(NAME, 11, 0, NOUT)
  IF (LCALL0 .AND. JMAX .LT. 2) CALL ERR2(NAME, 21, 0, NOUT)
  IF (LCALL0) LCALL0 = .FALSE.
  IF (JMAX .LT. 2) RETURN
  IF (RHO .GE. ZERO) ZUW = TWO * AA * RHO
  IF (RHO .LT. ZERO) ZUW = -RHO
  JMAX1 = JMAX + 1
  RHO0 = ZOM / (TWO * AA)
C$DIR NO_PARALLEL
  DO 68 M1 = 1, JMAX
    JR = M1 - 2
    ZOMIR2 = ONE / (ZOM ** (JR + 2))
    ZZZA = BIN(-1+3, JR+1+1) * ZOMIR2
C$DIR NO_PARALLEL
    DO 22 I = 1, MM
C$DIR NO_PARALLEL
      DO 20 J = 1, MM
        PP(J, I, M1) = ZERO
      20 CONTINUE
    22 CONTINUE
C$DIR NO_PARALLEL
    DO 24 I = 1, MM
      PP(I, I, M1) = ZZZA
    24 CONTINUE
      IF (ZOM .LE. ZUW) THEN
        IPXL = JR + 1 + IPOFF
        IF (IPXL .LE. IPXU) THEN
          ZZB0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 1)
C$DIR NO_PARALLEL
          DO 34 IPX = IPXL, IPXU
            IP = IPX - IPOFF
            ZZB = - BIN(IP+3, JR+1+1) * ZZB0
C$DIR NO_PARALLEL
          DO 32 I = 1, MM
C$DIR NO_PARALLEL
            DO 30 J = 1, MM
              PP(J, I, M1) = PP(J, I, M1)
                + ZZB * WD(J, I, IPX)
            30 CONTINUE
          32 CONTINUE
          ZZB0 = ZZB0 * RHO0
        34 CONTINUE
```



```

        ENDIF
    ENDIF
C$DIR NO_PARALLEL
    DO 42 I = 1,MM
C$DIR NO_PARALLEL
    DO 40 J = 1,MM
        QQ(J,I,M1) = ZERO
    40    CONTINUE
    42    CONTINUE
        IF (JR .LT. 0) GO TO 66
        IF (JR .EQ. 0) THEN
            ZZZC = -0.25D0
C$DIR NO_PARALLEL
            DO 50 I = 1,MM
                QQ(I,I,M1) = ZZZC
            50    CONTINUE
            ENDIF
            IF (JR .GE. 0) THEN
                ZZZD = -BIN(-2+3,JR+1) * ZOMIR2
C$DIR NO_PARALLEL
                DO 52 I = 1,MM
                    QQ(I,I,M1) = QQ(I,I,M1) + ZZZD * MU(I) ** 2
                52    CONTINUE
            ENDIF
            IF (ZOM .GT. ZUW) GO TO 66
            IPXL = -1 + IPOFF
            IF (IPXL .GT. IPXU) CALL ERR2(NAME, 31, 1, NOUT)
            ZZZE0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 2)
C$DIR NO_PARALLEL
            DO 65 IPX = IPXL,IPXU
                IP = IPX - IPOFF
                IF (IP .GE. 0 .AND. JR .GT. IP) GO TO 64
                ZZZE = - BIN(IP+3,JR+1) * ZZZE0
C$DIR NO_PARALLEL
            DO 62 I = 1,MM
C$DIR NO_PARALLEL
                DO 60 J = 1,MM
                    QQ(J,I,M1) = QQ(J,I,M1)
                    & + ZZZE * WS(J,I,IPX)
                60    CONTINUE
                62    CONTINUE
                64    CONTINUE
                    ZZZE0 = ZZZE0 * RHO0
                65    CONTINUE
                66    CONTINUE
                68    CONTINUE
C$DIR LOOP_PARALLEL
C$DIR LOOP_PRIVATE(CNTX,CNTY,J,N1,JP,JP1,M1,JR,K,ZZZ71)
    DO 122 I = 1,MM
C$DIR NO_PARALLEL
        DO 70 J = 1,MM
            CNTX(J,2) = CNT(I,J,2)
        70    CONTINUE
C$DIR NO_PARALLEL
        DO 71 J = 1,MM
            CNTY(J,2) = CNTX(J,2)
        71    CONTINUE
C$DIR NO_PARALLEL
        DO 120 N1 = 3,JMAX1
            JP = N1 - 1
C$DIR NO_PARALLEL
            DO 72 J = 1,MM
                CNTX(J,N1) = ZERO
            72    CONTINUE
            JP1 = JP - 1
C$DIR NO_PARALLEL
            DO 90 M1 = 1,JP1
                JR = M1 - 2
C$DIR NO_PARALLEL
            DO 82 K = 1,MM
C$DIR NO_PARALLEL
            DO 80 J = 1,MM

```

```

          CNTX(J,N1) = CNTX(J,N1)
1          + PP(J,K,M1) * CNTY(K,N1-JR-2)
80         CONTINUE
82         CONTINUE
C$DIR NO_PARALLEL
          DO 86 K = 1,MM
C$DIR NO_PARALLEL
          DO 84 J = 1,MM
          CNTX(J,N1) = CNTX(J,N1)
1          + QQ(J,K,M1) * CNTX(K,N1-JR-2)
84         CONTINUE
86         CONTINUE
90         CONTINUE
          M1 = JP
C$DIR NO_PARALLEL
          DO 92 J = 1,MM
          CNTX(J,N1) = CNTX(J,N1) + QQ(J,I,M1)
92         CONTINUE
          ZZZ71 = - ONE / DFLOAT(JP * (JP - 1))
C$DIR NO_PARALLEL
          DO 100 J = 1,MM
          CNTX(J,N1) = ZZZ71 * CNTX(J,N1)
100        CONTINUE
C$DIR NO_PARALLEL
          DO 102 J = 1,MM
          CNTY(J,N1) = (N1 - 1) * CNTX(J,N1)
102        CONTINUE
C$DIR NO_PARALLEL
          DO 110 J = 1,MM
          CNT(I,J,N1) = CNTX(J,N1)
110        CONTINUE
120        CONTINUE
122        CONTINUE
          IF (.NOT.LTEST) RETURN
          WRITE (NOUT,4100) NAME, ZOM
C$DIR NO_PARALLEL
          DO 132 K = 1,JMAX1
          WRITE (NOUT,4110) K
C$DIR NO_PARALLEL
          DO 130 I = 1,MM
          WRITE (NOUT,4120) (CNT(I,J,K), J = 1,MM)
130        CONTINUE
132        CONTINUE
          RETURN
4000       FORMAT (
          A 2H -, A6, 1H-, A60)
4100       FORMAT (//, 1H , 80(1H-), /,
          A 1H , 1H-, A6, 1H-, 4HZOM , F12.6)
4110       FORMAT (/,
          A 1H , 4H K , I4)
4120       FORMAT (
          A (1H , 8X, 4F16.8))
6000       FORMAT (
          A 1H , 1H-, A6, 1H-, 4H I, I8, 8H THREAD, I8)
          END

```

File: rrpsm_4.2P1.fnoc

```
-----
SUBROUTINE RRPSM(NCDS, NCDP, NCDCN, NDBIN1, NDBIN2,
1          WS, WD, MM, MU, IPXU, IPOFF, ZOM, JMAX, AA,
2          RHOEW, PP, QQ, RR, BIN,
3          LTEST, NOUT, CNT)
  IMPLICIT REAL*8 (A - H, O - Z)
  LOGICAL LTEST
  DIMENSION WS(NCDS,NCDS,NCDP), WD(NCDS,NCDS,NCDP),
1          MU(NCDS),
2          PP(NCDS,NCDS,NCDCN), QQ(NCDS,NCDS,NCDCN),
3          RR(NCDS,NCDS), BIN(NDBIN1,NDBIN2),
4          CNT(NCDS,NCDS,NCDCN)
  CHARACTER*6 NAME / 'RRPSM' /
  CHARACTER*60 VERS
*/ ' 4.2P1, 95/10/13 -M_4.2 C$DIR 122 ' /
  PARAMETER (ZERO = 0.D0, ONE = 1.D0, TWO = 2.D0)
  PARAMETER (NPDS = 49, NPDCN = 22)
  DIMENSION CNTX(NPDS,NPDCN), RRX(NPDS,NPDS,NPDCN,NPDCN)
  LOGICAL LCALL0
  DATA LCALL0 / .TRUE. /
  IF (LCALL0) WRITE (NOUT,4000) NAME, VERS
  IF (MM .GT. NCDS) CALL ERR2(NAME, 1, 1, NOUT)
  IF (IPXU .GT. NCDP) CALL ERR2(NAME, 2, 1, NOUT)
  IF (JMAX+1 .GT. NCDCN) CALL ERR2(NAME, 3, 1, NOUT)
  IF (ABS(AA) .LT. CDXTOL()) CALL ERR2(NAME, 4, 1, NOUT)
  IF (NPDS .NE. NCDS) CALL ERR2(NAME, 5, 1, NOUT)
  IF (NPDCN .NE. NCDCN) CALL ERR2(NAME, 6, 1, NOUT)
  IF (LCALL0 .AND. IPOFF .GT. 2) CALL ERR2(NAME, 11, 0, NOUT)
  IF (LCALL0 .AND. JMAX .LT. 2) CALL ERR2(NAME, 21, 0, NOUT)
  IF (LCALL0) LCALL0 = .FALSE.
  IF (JMAX .LT. 2) RETURN
  IF (RHOEW .GE. ZERO) ZUW = TWO * AA * RHOEW
  IF (RHOEW .LT. ZERO) ZUW = -RHOEW
  JMAX1 = JMAX + 1
  RHO0 = ZOM / (TWO * AA)
C$DIR NO_PARALLEL
  DO 68 M1 = 1, JMAX
    JR = M1 - 2
    ZOMIR2 = ONE / (ZOM ** (JR + 2))
    ZZZA = BIN(-1+3, JR+1+1) * ZOMIR2
C$DIR NO_PARALLEL
    DO 22 I = 1, MM
C$DIR NO_PARALLEL
      DO 20 J = 1, MM
        PP(J, I, M1) = ZERO
      20 CONTINUE
    22 CONTINUE
C$DIR NO_PARALLEL
    DO 24 I = 1, MM
      PP(I, I, M1) = ZZZA
    24 CONTINUE
      IF (ZOM .LE. ZUW) THEN
        IPXL = JR + 1 + IPOFF
        IF (IPXL .LE. IPXU) THEN
          ZZZB0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 1)
C$DIR NO_PARALLEL
          DO 34 IPX = IPXL, IPXU
            IP = IPX - IPOFF
            ZZZB = - BIN(IP+3, JR+1+1) * ZZZB0
C$DIR NO_PARALLEL
          DO 32 I = 1, MM
C$DIR NO_PARALLEL
            DO 30 J = 1, MM
              PP(J, I, M1) = PP(J, I, M1)
                + ZZZB * WD(J, I, IPX)
            30 CONTINUE
          32 CONTINUE
          ZZZB0 = ZZZB0 * RHO0
        34 CONTINUE
```

```

        ENDIF
    ENDIF
C$DIR NO_PARALLEL
    DO 42 I = 1,MM
C$DIR NO_PARALLEL
    DO 40 J = 1,MM
        QQ(J,I,M1) = ZERO
    40    CONTINUE
    42    CONTINUE
        IF (JR .LT. 0) GO TO 66
        IF (JR .EQ. 0) THEN
            ZZZC = -0.25D0
C$DIR NO_PARALLEL
            DO 50 I = 1,MM
                QQ(I,I,M1) = ZZZC
            50    CONTINUE
            ENDIF
            IF (JR .GE. 0) THEN
                ZZZD = -BIN(-2+3,JR+1) * ZOMIR2
C$DIR NO_PARALLEL
                DO 52 I = 1,MM
                    QQ(I,I,M1) = QQ(I,I,M1) + ZZZD * MU(I) ** 2
                52    CONTINUE
            ENDIF
            IF (ZOM .GT. ZUW) GO TO 66
            IPXL = -1 + IPOFF
            IF (IPXL .GT. IPXU) CALL ERR2(NAME, 31, 1, NOUT)
            ZZZE0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 2)
C$DIR NO_PARALLEL
            DO 65 IPX = IPXL,IPXU
                IP = IPX - IPOFF
                IF (IP .GE. 0 .AND. JR .GT. IP) GO TO 64
                ZZZE = - BIN(IP+3,JR+1) * ZZZE0
C$DIR NO_PARALLEL
            DO 62 I = 1,MM
C$DIR NO_PARALLEL
                DO 60 J = 1,MM
                    QQ(J,I,M1) = QQ(J,I,M1)
                    & + ZZZE * WS(J,I,IPX)
                60    CONTINUE
            62    CONTINUE
            64    CONTINUE
                ZZZE0 = ZZZE0 * RHO0
            65    CONTINUE
            66    CONTINUE
            68    CONTINUE
C$DIR NO_PARALLEL
            DO 206 N1 = 3,JMAX1
                JP = N1 - 1
                JP1 = JP - 1
C$DIR NO_PARALLEL
                DO 204 M1 = 1,JP1
                    JR = M1 - 2
                    ZZZP = JP - JR - 2
C$DIR NO_PARALLEL
                DO 202 K = 1,MM
C$DIR NO_PARALLEL
                    DO 200 J = 1,MM
                        RRX(J,K,M1,N1) = ZZZP * PP(J,K,M1) + QQ(J,K,M1)
                    200    CONTINUE
                202    CONTINUE
                204    CONTINUE
                206    CONTINUE
C$DIR LOOP_PARALLEL
C$DIR LOOP_PRIVATE(CNTX,J,N1,JP,JP1,M1,JR,K,ZZZ71)
            DO 122 I = 1,MM
C$DIR NO_PARALLEL
                DO 70 J = 1,MM
                    CNTX(J,2) = CNT(I,J,2)
                70    CONTINUE
C$DIR NO_PARALLEL
            DO 120 N1 = 3,JMAX1

```

```

                JP = N1 - 1
C$DIR NO_PARALLEL
                DO 72 J = 1,MM
                    CNTX(J,N1) = ZERO
72              CONTINUE
                JP1 = JP - 1
C$DIR NO_PARALLEL
                DO 90 M1 = 1,JP1
                    JR = M1 - 2
C$DIR NO_PARALLEL
C$DIR NO_PARALLEL
                    DO 86 K = 1,MM
                        DO 84 J = 1,MM
                            CNTX(J,N1) = CNTX(J,N1)
                                + RRX(J,K,M1,N1) * CNTX(K,N1-JR-2)
84              CONTINUE
86              CONTINUE
90              CONTINUE
                M1 = JP
C$DIR NO_PARALLEL
                DO 92 J = 1,MM
                    CNTX(J,N1) = CNTX(J,N1) + QQ(J,I,M1)
92              CONTINUE
                    ZZZ71 = - ONE / DFLOAT(JP * (JP - 1))
C$DIR NO_PARALLEL
                DO 100 J = 1,MM
                    CNTX(J,N1) = ZZZ71 * CNTX(J,N1)
100             CONTINUE
C$DIR NO_PARALLEL
                DO 110 J = 1,MM
                    CNT(I,J,N1) = CNTX(J,N1)
110             CONTINUE
120             CONTINUE
122             CONTINUE
                IF (.NOT.LTEST) RETURN
                WRITE (NOUT,4100) NAME, ZOM
C$DIR NO_PARALLEL
                DO 132 K = 1,JMAX1
                    WRITE (NOUT,4110) K
C$DIR NO_PARALLEL
                DO 130 I = 1,MM
                    WRITE (NOUT,4120) (CNT(I,J,K), J = 1,MM)
130             CONTINUE
132             CONTINUE
                RETURN
4000            FORMAT (
A 2H -, A6, 1H-, A60)
4100            FORMAT (//, 1H , 80(1H-), /,
A 1H , 1H-, 2A4, 1H-, 4HZOM , F12.6)
4110            FORMAT (/,
A 1H , 4H K , I4)
4120            FORMAT (
A (1H , 8X, 4F16.8))
                END

```

File: rrpsm_4.1PV1.fnoc

```
-----
SUBROUTINE  RRPSM(NCDS, NCDP, NCDCN, NDBIN1, NDBIN2,
1           WS, WD, MM, MU, IPXU, IPOFF, ZOM, JMAX, AA,
2           RHO, PP, QQ, RR, BIN,
3           LTEST, NOUT, CNT)
  IMPLICIT  REAL*8 (A - H, O - Z)
  LOGICAL   LTEST
  DIMENSION WS(NCDS,NCDS,NCDS), WD(NCDS,NCDS,NCDS),
1           MU(NCDS),
2           PP(NCDS,NCDS,NCDCN), QQ(NCDS,NCDS,NCDCN),
3           RR(NCDS,NCDS), BIN(NDBIN1,NDBIN2),
4           CNT(NCDS,NCDS,NCDCN)
  CHARACTER*6 NAME / 'RRPSM' /
  CHARACTER*60 VERS
  * / ' 4.1PV1, 95/10/20 -M_4.1P1 (DGEMV) ' /
  PARAMETER (ZERO = 0.D0, ONE = 1.D0, TWO = 2.D0)
  PARAMETER (NPDS = 49, NPDCN = 22)
  DIMENSION CNTX(NPDS,NPDCN), CNTY(NPDS,NPDCN)
  LOGICAL   LCALL0
  DATA     LCALL0 / .TRUE. /
  IF (LCALL0) WRITE (NOUT,4000) NAME, VERS
  IF (MM .GT. NCDS)      CALL ERR2(NAME, 1, 1, NOUT)
  IF (IPXU .GT. NCDP)    CALL ERR2(NAME, 2, 1, NOUT)
  IF (JMAX+1 .GT. NCDCN) CALL ERR2(NAME, 3, 1, NOUT)
  IF (ABS(AA) .LT. CDXTOL()) CALL ERR2(NAME, 4, 1, NOUT)
  IF (NPDS .NE. NCDS)    CALL ERR2(NAME, 5, 1, NOUT)
  IF (NPDCN .NE. NCDCN)  CALL ERR2(NAME, 6, 1, NOUT)
  IF (LCALL0 .AND. IPOFF .GT. 2) CALL ERR2(NAME, 11, 0, NOUT)
  IF (LCALL0 .AND. JMAX .LT. 2) CALL ERR2(NAME, 21, 0, NOUT)
  IF (LCALL0) LCALL0 = .FALSE.
  IF (JMAX .LT. 2) RETURN
  IF (RHO .GE. ZERO) ZUW = TWO * AA * RHO
  IF (RHO .LT. ZERO) ZUW = -RHO
  JMAX1 = JMAX + 1
  RHO0 = ZOM / (TWO * AA)
C$DIR NO_PARALLEL
  DO 68 M1 = 1, JMAX
    JR = M1 - 2
    ZOMIR2 = ONE / (ZOM ** (JR + 2))
    ZZZA = BIN(-1+3, JR+1+1) * ZOMIR2
C$DIR NO_PARALLEL
    DO 22 I = 1, MM
C$DIR NO_PARALLEL
      DO 20 J = 1, MM
        PP(J, I, M1) = ZERO
      20 CONTINUE
    22 CONTINUE
C$DIR NO_PARALLEL
    DO 24 I = 1, MM
      PP(I, I, M1) = ZZZA
    24 CONTINUE
      IF (ZOM .LE. ZUW) THEN
        IPXL = JR + 1 + IPOFF
        IF (IPXL .LE. IPXU) THEN
          ZZB0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 1)
C$DIR NO_PARALLEL
          DO 34 IPX = IPXL, IPXU
            IP = IPX - IPOFF
            ZZB = - BIN(IP+3, JR+1+1) * ZZB0
C$DIR NO_PARALLEL
          DO 32 I = 1, MM
C$DIR NO_PARALLEL
            DO 30 J = 1, MM
              PP(J, I, M1) = PP(J, I, M1)
                1 + ZZB * WD(J, I, IPX)
            30 CONTINUE
          32 CONTINUE
          ZZB0 = ZZB0 * RHO0
        34 CONTINUE
```

```

        ENDIF
    ENDIF
C$DIR NO_PARALLEL
    DO 42 I = 1,MM
C$DIR NO_PARALLEL
    DO 40 J = 1,MM
        QQ(J,I,M1) = ZERO
    40    CONTINUE
    42    CONTINUE
        IF (JR .LT. 0) GO TO 66
        IF (JR .EQ. 0) THEN
            ZZZC = -0.25D0
C$DIR NO_PARALLEL
            DO 50 I = 1,MM
                QQ(I,I,M1) = ZZZC
            50    CONTINUE
            ENDIF
            IF (JR .GE. 0) THEN
                ZZZD = -BIN(-2+3,JR+1) * ZOMIR2
C$DIR NO_PARALLEL
                DO 52 I = 1,MM
                    QQ(I,I,M1) = QQ(I,I,M1) + ZZZD * MU(I) ** 2
                52    CONTINUE
            ENDIF
            IF (ZOM .GT. ZUW) GO TO 66
            IPXL = -1 + IPOFF
            IF (IPXL .GT. IPXU) CALL ERR2(NAME, 31, 1, NOUT)
            ZZZE0 = ZOMIR2 * RHO0 ** (IPXL - IPOFF + 2)
C$DIR NO_PARALLEL
            DO 65 IPX = IPXL,IPXU
                IP = IPX - IPOFF
                IF (IP .GE. 0 .AND. JR .GT. IP) GO TO 64
                ZZZE = - BIN(IP+3,JR+1) * ZZZE0
C$DIR NO_PARALLEL
            DO 62 I = 1,MM
C$DIR NO_PARALLEL
                DO 60 J = 1,MM
                    QQ(J,I,M1) = QQ(J,I,M1)
                    & + ZZZE * WS(J,I,IPX)
                60    CONTINUE
            62    CONTINUE
            64    CONTINUE
                ZZZE0 = ZZZE0 * RHO0
            65    CONTINUE
            66    CONTINUE
            68 CONTINUE
C$DIR LOOP_PARALLEL
C$DIR LOOP_PRIVATE(CNTX,CNTY,J,N1,JP,JP1,M1,JR,K,ZZZ71)
    DO 122 I = 1,MM
C$DIR NO_PARALLEL
        DO 70 J = 1,MM
            CNTX(J,2) = CNT(I,J,2)
        70    CONTINUE
C$DIR NO_PARALLEL
        DO 71 J = 1,MM
            CNTY(J,2) = CNTX(J,2)
        71    CONTINUE
C$DIR NO_PARALLEL
        DO 120 N1 = 3,JMAX1
            JP = N1 - 1
C$DIR NO_PARALLEL
            DO 72 J = 1,MM
                CNTX(J,N1) = ZERO
            72    CONTINUE
            JP1 = JP - 1
C$DIR NO_PARALLEL
            DO 90 M1 = 1,JP1
                JR = M1 - 2
                CALL DGEMV('N', MM, MM, ONE, PP(1,1,M1), NCDS,
                    & CNTY(1,N1-JR-2), 1,
                    & ONE, CNTX(1,N1), 1)
                CALL DGEMV('N', MM, MM, ONE, QQ(1,1,M1), NCDS,

```

```

&          CNTX(1,N1-JR-2), 1,
&          ONE, CNTX(1,N1), 1)
90          CONTINUE
           M1 = JP
C$DIR NO_PARALLEL
           DO 92 J = 1,MM
             CNTX(J,N1) = CNTX(J,N1) + QQ(J,I,M1)
92          CONTINUE
           ZZZ71 = - ONE / DFLOAT(JP * (JP - 1))
C$DIR NO_PARALLEL
           DO 100 J = 1,MM
             CNTX(J,N1) = ZZZ71 * CNTX(J,N1)
100         CONTINUE
C$DIR NO_PARALLEL
           DO 102 J = 1,MM
             CNTY(J,N1) = (N1 - 1) * CNTX(J,N1)
102        CONTINUE
C$DIR NO_PARALLEL
           DO 110 J = 1,MM
             CNT(I,J,N1) = CNTX(J,N1)
110        CONTINUE
120        CONTINUE
122        CONTINUE
           IF (.NOT.LTEST) RETURN
           WRITE (NOUT,4100) NAME, ZOM
C$DIR NO_PARALLEL
           DO 132 K = 1,JMAX1
             WRITE (NOUT,4110) K
C$DIR NO_PARALLEL
           DO 130 I = 1,MM
             WRITE (NOUT,4120) (CNT(I,J,K), J = 1,MM)
130        CONTINUE
132        CONTINUE
           RETURN
4000       FORMAT (
           A 2H -, A6, 1H-, A60)
4100       FORMAT (//, 1H , 80(1H-), /,
           A 1H , 1H-, A6, 1H-, 4HZOM , F12.6)
4110       FORMAT (/,
           A 1H , 4H K , I4)
4120       FORMAT (
           A (1H , 8X, 4F16.8))
6000       FORMAT (
           A 1H , 1H-, A6, 1H-, 4H I, I8, 8H THREAD, I8)
           END

```