Doubly charm tetraquark and its quark mass dependence

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both on N_f=2+1, CLS ensembles, $m_\pi pprox 280~{
m MeV}$

$$ccd\bar{u} = T_{cc}$$

Padmanath, S.P.: 2202.101101, Phys.Rev.Lett. 129 (2022) 3, 032002 & subsequent studies with S. Collins



The longest lived exotic hadron ever discovered

LHCb July 2021, 2109.01038, 2109.01056

The doubly charmed tetraquark T_{cc}^+ , I = 0 and favours $J^P = 1^+$. No states observed in $D^0D^+\pi^+$: eliminates possibility of I = 1. Near-threshold state: Demands pole identification to confirm existence.



Omitting $D^* \to D\pi$, $T_{cc} \to DD\pi$ T_{cc} would be a bound state

$$\begin{split} \delta m_{\rm pole} &= -360 \pm 40^{+4}_{-0} \,\, {\rm keV}/c^2 \,, \\ \Gamma_{\rm pole} &= 48 \pm 2^{+0}_{-14} \,\, {\rm keV} \,, \end{split}$$

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closer-to physical m_c

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 $D^* \to D\pi$ omitting

 $T_{cc} \rightarrow DD\pi$

Definitions: bound state, virtual bound state & resonance

$$T(E) \propto \frac{1}{E^2 - m^2}$$
 $T(E) \propto \frac{1}{E^2 - m^2 + iE\Gamma}$





$$E = \sqrt{m_1^2 + p^2} + \sqrt{m_2^2 + (-p)^2} < m_1 + m_2$$

Possible binding mechanisms of T_{cc}

molecular likely dominant [e.g. Janc, Rosina 2003]



"molecular"

Molecular component: dependence on m_{u/d}

exchanged particles: light mesons $\pi, \rho, ...$

increasing m_{u/d} increasing m_{ex} decreasing R or decreasing attraction |V| Yukava-like potential

SP=0+

SP=1+

 $|ar{u}d|$

|cc|

$$V(r) \propto -\frac{e^{-m_{ex}r}}{r}$$

analogous conclusion for any fully attractive

$$V(r) = -V_0 f(r/R)$$

$$f = e^{-r/R}, e^{-r^2/R^2}, \theta(R-r), \dots$$



subsequent lattice study: CLQCD, Chen et al. 2206.06185 comparison of I=0,1 : attraction in I=0 channel arises mainly from *Q* exchange

Simplest Example: scattering in square-well potential in QM



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increasing $m_{u/d}$, decreasing attraction V_0 (or decreasing R)

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All fully attractive potentials lead to analogous conclusions





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Molecular component: dependence on m_c

V(r) independent on m_c ,

m_c decreases : reduced mass m_r of D,D* system decreases





decreasing m_c and m_r



lattice results

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[QQ][ud] dominated state: dependence on m_Q and $m_{u,d}$ known only for a bound state well bellow threshold



 $bbd\bar{u}$

 $I = 0, J^P = 1^+$

Conclusion on the doubly charm tetraquark



- The longest lived exotic hadron ever discovered
- It lies very close to DD* threshold: t(E) has to be extracted
- virtual bound state pole slightly below DD* at m_{u/d}>m_{u/d}^{phy}
 virtual bound state pole further below th. as m_c is decreased:

consistent with expectations from dominant molecular Fock comp. (this alone does not rule out the presence of other Fock components or other binding mechanisms)



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current study: **

 $m_{\pi} \simeq 280 \text{ MeV}$: $D^* \not\rightarrow D\pi, \ T_{cc} \not\rightarrow DD\pi$ $DD\pi$ above analyzed region

one of the future challenges •

 m_{π}^{phy} : $D^* \to D\pi, T_{cc} \to DD\pi$

[Blanton, Sharpe, Lopez,

Three-particle finite-volume formalism for $\pi^+\pi^+K^+$ and related systems

formalisms developed by three groups, particularly suitable for $DD\pi$:

2105.12094, 2111.12734, talk by S. Sharpe]

Implementing the three-particle quantization condition for $\pi^+\pi^+K^+$ and related systems



S.P., Collins, Padmanath, Mohler, Piemonte 2011.02541 JHEP, 1905.03506 PRD, 2111.02934

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Charmonium(like) resonances and bound states



32

L/a



Charmonium(like) resonances and bound states



q=u,d,s I=0

θ

θ

 $\chi_{c2}(1P)$

 2^{++}

 $\chi_{c2}(3930)$

4.0

3.9

3.8

3.7

-3.6

-3.5

3.4

θ

X(3842)

3⁻⁻

 $m(D_s^+D_s^-)$ [GeV]

12

 $2m_{Ds}$

 $2m_D$

Exp

θ

 $\Theta \ \psi(28)$

1

july 2022

φ

θ



LHCb X(3960) 9 fb⁻¹ preliminary 4.2 4.4 4.8

indico.cern.ch/event/1176505/

Backup

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Lattice details

CLS ensembles with u/d, s dynamical quarks $a \simeq 0.086 \text{ fm}$ N_L=24, 32

lat exp $m_{u/d} > m_{u/d}^{exp}$ $m_s < m_s^{exp}$ $m_u + m_d + m_s = m_u^{exp} + m_d^{exp} + m_s^{exp}$

$$m_c \gtrsim m_c^{exp}$$

m [MeV]	lat	ехр
mπ	280(3)	137
m _D	1927(2)	1867
m _{Ds}	1981(1)	1968
M _{av}	3103(3)	3068

separation between DD and DsDs threshols smaller than in exp

Wick contractions evaluated with distillation or stochastic distillation method.

Lattice results

	$m_D [{ m MeV}]$	m_{D^*} [MeV]	M_{av} [MeV]	$a_{l=0}^{(J=1)}$ [fm]	$r_{l=0}^{(J=1)}~[{ m fm}]$	$\delta m_{T_{cc}}$ [MeV]	T_{cc}
lat. $(m_{\pi} \simeq 280 \text{ MeV}, m_c^{(h)})$	1927(1)	2049(2)	3103(3)	1.04(29)	$0.96(^{+0.18}_{-0.20})$	$-9.9^{+3.6}_{-7.2}$	virtual bound st.
lat. $(m_{\pi} \simeq 280 \text{ MeV}, m_c^{(l)})$	1762(1)	1898(2)	2820(3)	0.86(0.22)	$0.92(^{+0.17}_{-0.19})$	$-15.0(^{+4.6}_{-9.3})$	virtual bound st.
exp. 2, 37	1864.85(5)	2010.26(5)	3068.6(1)	-7.15(51)	[-11.9(16.9),0]	-0.36(4)	bound st.



Interpolators

Example: P=0

 $J^{P}=1^{+}$ -> cubic irrep T_{1}^{+}

$$\begin{split} O^{l=0} &= P(\{0,0,0\})V_z(\{0,0,0\})\\ O^{l=0} &= P(\{1,0,0\})V_z(\{-1,0,0\}) + P(\{-1,0,0\})V_z(\{1,0,0\})\\ &+ P(\{0,1,0\})V_z(\{0,-1,0\}) + P(\{0,-1,0\})V_z(\{0,1,0\})\\ &+ P(\{0,0,1\})V_z(\{0,0,-1\}) + P(\{0,0,-1\})V_z(\{0,0,1\})]\\ O^{l=2} &= P(\{1,0,0\})V_z(\{-1,0,0\}) + P(\{-1,0,0\})V_z(\{1,0,0\})\\ &+ P(\{0,1,0\})V_z(\{0,-1,0\}) + P(\{0,-1,0\})V_z(\{0,1,0\})\\ &- 2[P(\{0,0,1\})V_z(\{0,0,-1\}) + P(\{0,0,-1\})V_z(\{0,0,1\})]\\ O^{l=0} &= V_{1x}[0,0,0]V_{2y}[0,0,0] - V_{1y}[0,0,0]V_{2x}[0,0,0] \end{split}$$





s-wave scattering on spherical potential well



$$\chi^{2}(\{a\}) = \sum_{L} \sum_{\vec{P} \Lambda n} \sum_{\vec{P}' \Lambda' n'} dE_{cm}(L, \vec{P} \Lambda n; \{a\})$$
(1)
$$\mathcal{C}^{-1}(L; \vec{P} \Lambda n; \vec{P}' \Lambda' n') dE_{cm}(L, \vec{P}' \Lambda' n'; \{a\}) .$$

Here

$$dE_{cm}(L, \vec{P}\Lambda n; \{a\}) = E_{cm}(L, \vec{P}\Lambda n) - E_{cm}^{an}(L, \vec{P}\Lambda n; \{a\})$$

$$(t_l^{(J)})^{-1} = \frac{2(\tilde{K}_l^{(J)})^{-1}}{E_{cm}p^{2l}} - i\frac{2p}{E_{cm}}, \quad (\tilde{K}_l^{(J)})^{-1} = p^{2l+1}\cot\delta_l^{(J)}$$
(5)

We parametrize it with the effective range expansion

$$\tilde{K}^{-1} = \begin{bmatrix} \frac{1}{a_0^{(1)}} + \frac{r_0^{(1)}p^2}{2} & 0 & 0\\ 0 & \frac{1}{a_1^{(0)}} + \frac{r_1^{(0)}p^2}{2} & 0\\ 0 & 0 & \frac{1}{a_1^{(2)}} \end{bmatrix}.$$
 (6)

other lattice studies of Tcc

Previous lattice QCD study of T_{cc} channel

Junnarkar, Mathur, Padmanath, PRD 99, 034507 (2019), 1810.12285



lowest finite-volume eigen-energy for P=0, J^P=1⁺, I=0

- Study performed on LQCD ensembles with different lattice spacings. Single volume and only rest frame finite-volume irreps considered.
- Including a meson-meson and diquark-antidiquark interpolator. Diquark-antidiquark interpolators do not influence the low energy spectrum.
- **t** The ground state energy subjected to chiral and continuum extrapolations.
- ✿ A finite-volume energy level 23(11) MeV below DD* threshold.
 No rigorous scattering analysis and no pole structure determined.



- Single volume rest frame study on a relatively coarse lattice $(a_s \sim 0.12 \text{ fm})$.
- Large basis of meson-meson and diquark-antidiquark interpolators.
- Diquark-antidiquark interpolators do not influence the low energy spectrum.
- ✿ No statistically significant energy shifts observed near DD^* threshold.
 ⇒ No scattering amplitude extraction.

Subsequent lattice QCD study of T_{cc} channel

CLQCD, Chen et al. 2206.06185

comparison of I=0,1 : attraction in I=0 channel arises mainly from *e* exchange



 $C^{(I)}(p,t) = D - C_1(\pi/\rho) + (-)^{I+1} \left(D' - C_2(\rho) \right)$

Phenomenological theoretical predictions

- ✤ Phenomenological approaches →
 - * Janc & Rosina , Few Body Syst. 35, 175 (2004), hep-ph/0405208

one of the most sophisticated quark model predictions:

V_{ii} between all pairs of quarks, ground state energy of four-body problem

 $\delta m = -1.6 \pm 1.0 \text{ MeV}$



(references at the back)

Resonances from coupled-channel scattering

most results by HadSpec. coll.: mostly light meson sector



slide by Mikhashenko, Hadron Spectrum in Confinement, aug 2022







- Assuming to be the same, $\mathcal{B}(\chi_{c0} \to D^+D^-)/\mathcal{B}(\chi_{c0} \to D_s^+D_s^-P) \sim 0.3$ large molecular component, or large tetraquark component, $T_{\psi\phi}$
- [JHEP 06 (2021) 035] finds a state coupled to $D_s^+D_s^-$ on the lattice

Mishe Mildesonles (ODICING Cluster) Tetranucula and Daste such 2000	- nd	
Misha Mikhasenko (ORIGINS Cluster)	August 2 nd	13/21



slide by Mikhashenko, Hadron Spectrum in Confinement, aug 2022





• Belle sees a clean state in $J/\psi\omega$ with $J^P = 0^+$ • The $D_s^+ D_s^-$ signal might be a tail of the $\chi_{c0}(3915)$ state Misha Mikhasenko (ORIGINS Cluster) Tetraquarks and Pentaguarks 2022 August 2nd 14/21